

# Crystallization from solutions

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# **Thermodynamics & Kinetics of crystallization - nucleation**

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Prof. Dr.-Ing. Dr. h.c. Joachim Ulrich





Thermodynamically stable phases of organic and inorganic substances depend on:

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- Temperature
- Pressure
- surrounding media:
  - air (relative humidity)
  - solvent (solubility)
- additional: mechanical stress (e.g. grinding)

# Phase diagrams

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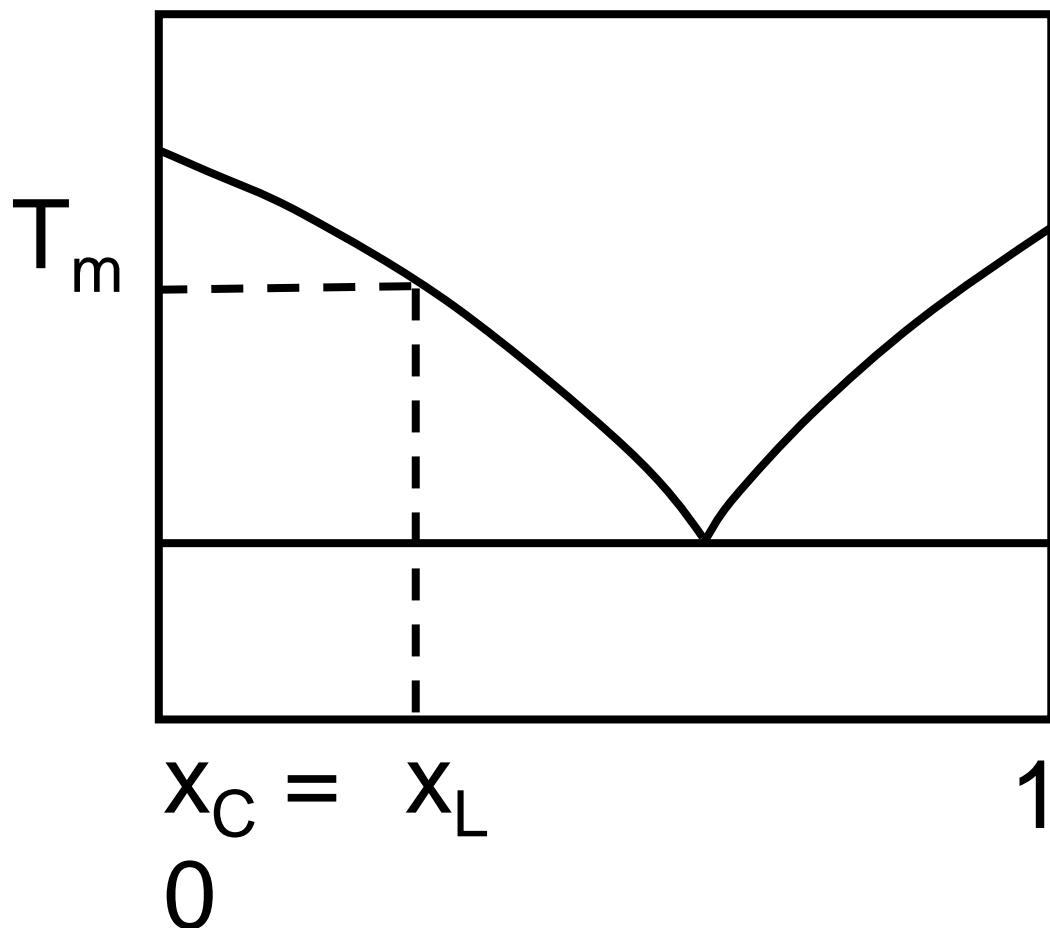
“A phase diagram graphically represents (in two or three dimensions) the equilibria between various phases of a system in a wide range of temperature, pressure and concentration/composition.

It specifies the equilibrium conditions ( $T$ ,  $p$  and  $x$ ) and the corresponding phase present at this state.

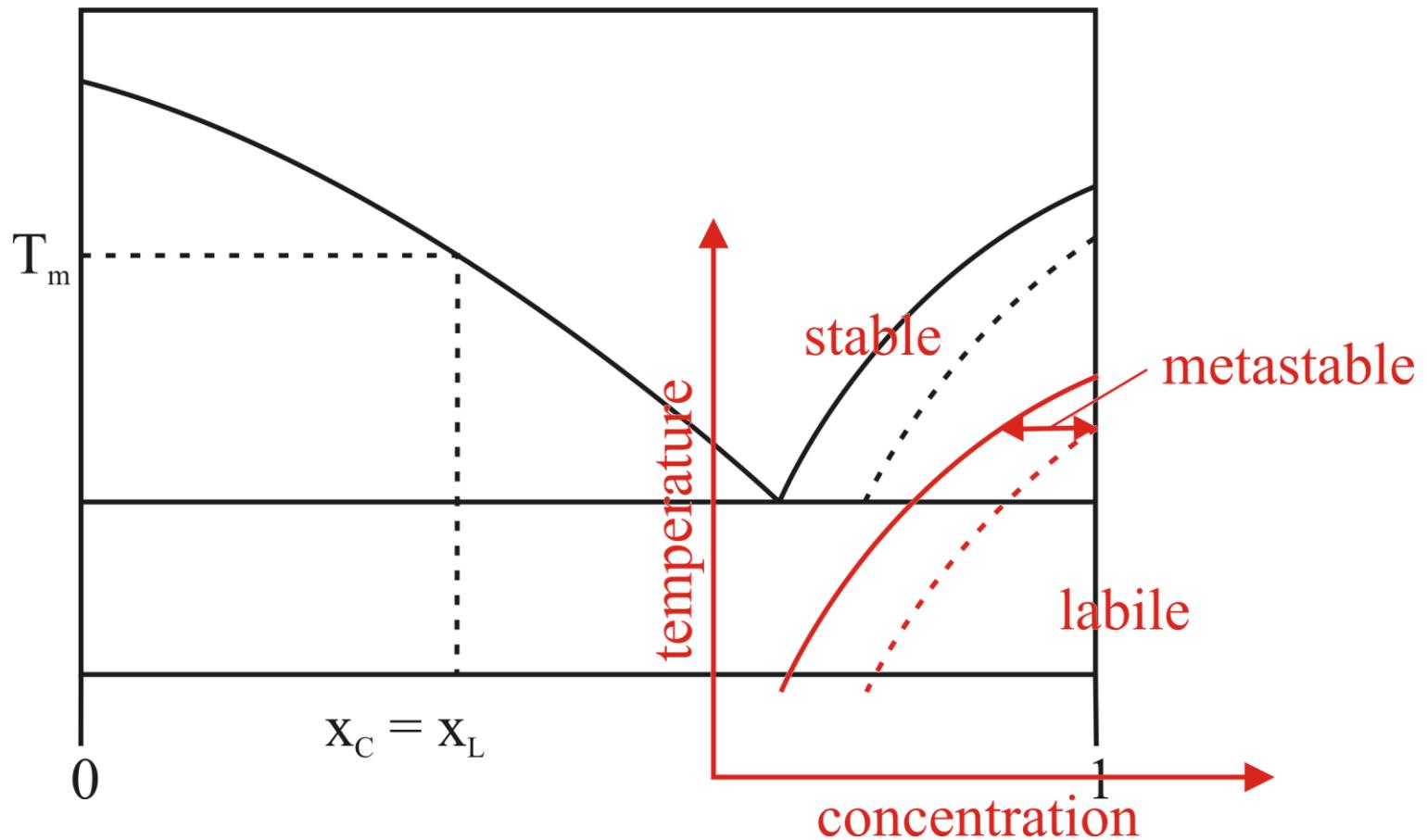
Thus, in case of SLE, the phase diagram also tells about the solid phases occurring in a system, such as polymorphs, solvates or intermediate compounds” [LOR13].

## Phase diagram - melts

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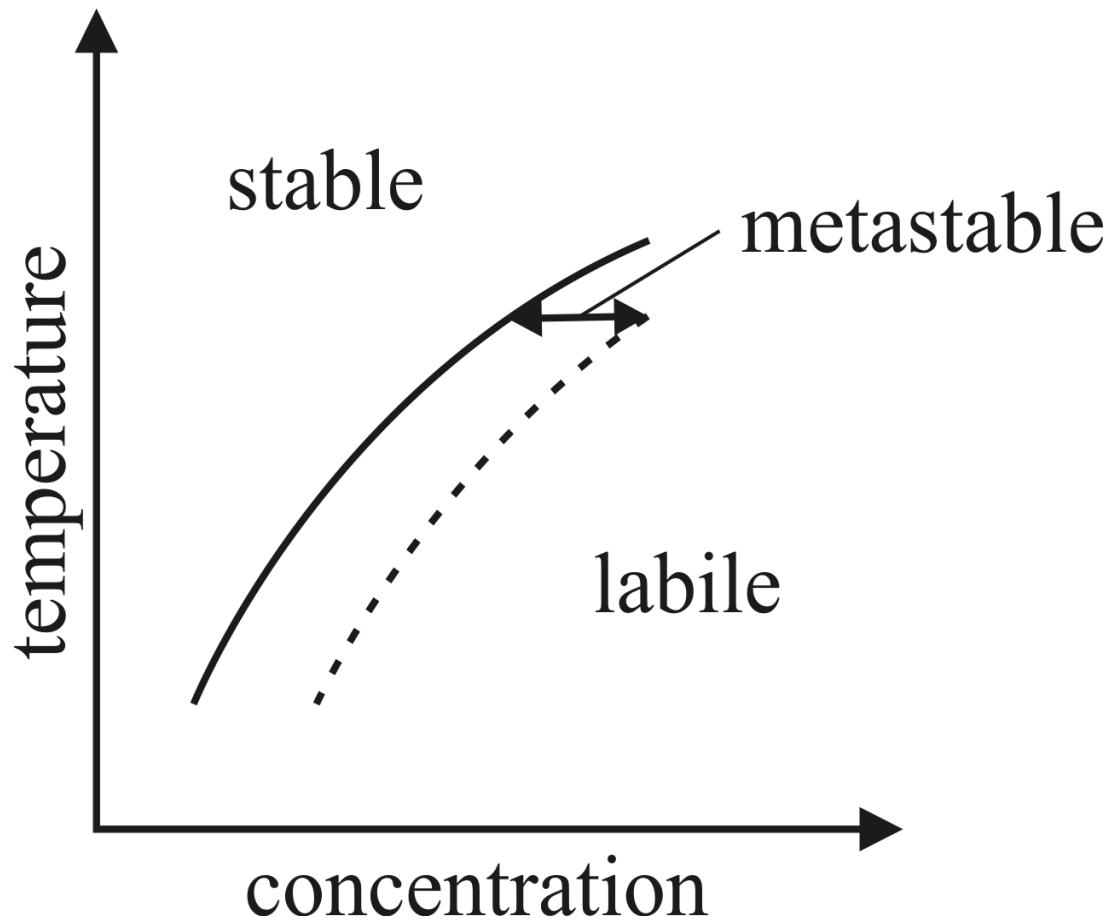


# Phase diagram overlapped by the „wrong plotted“ solubility diagram



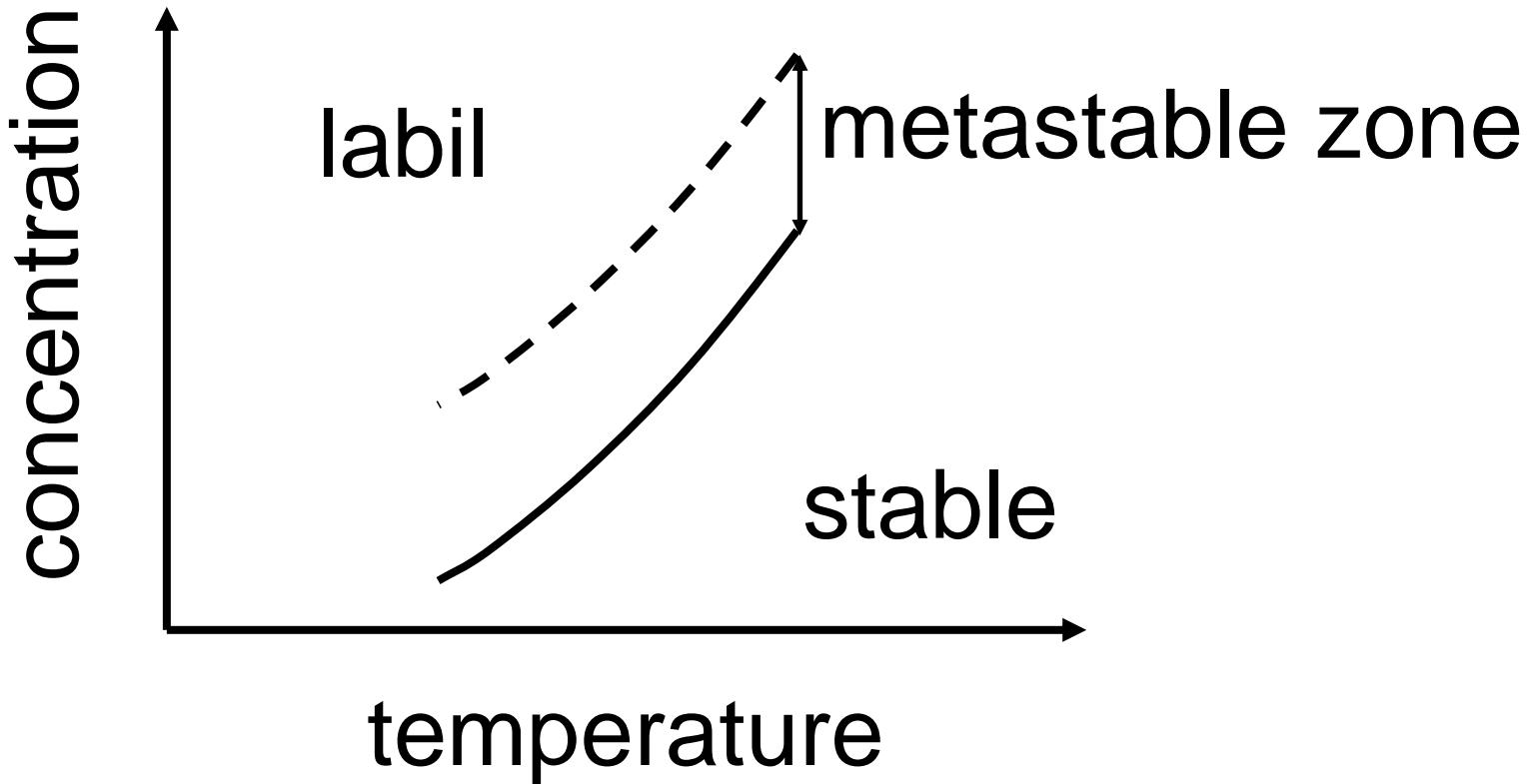
## Solubility diagram – „wrong plotted“

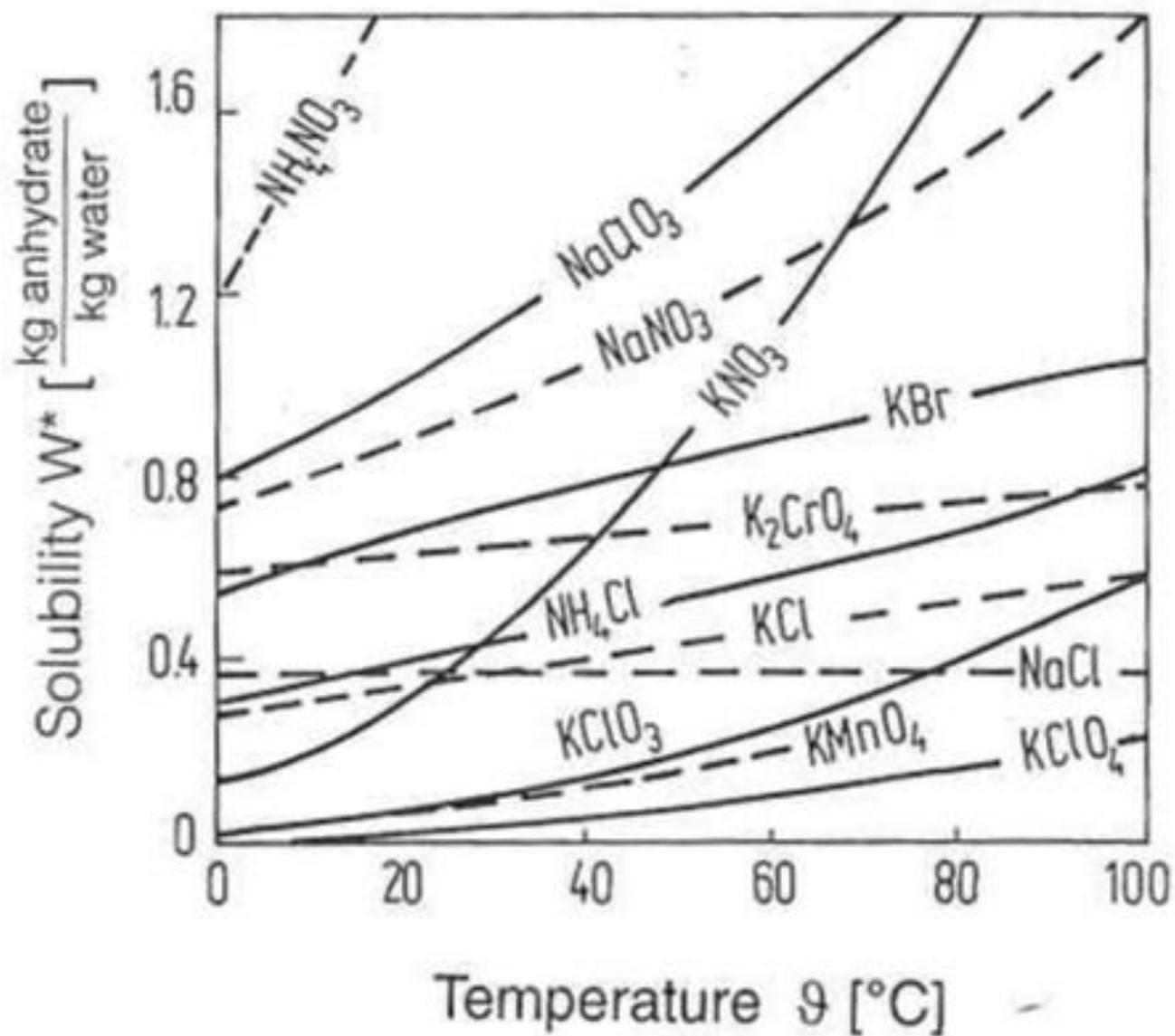
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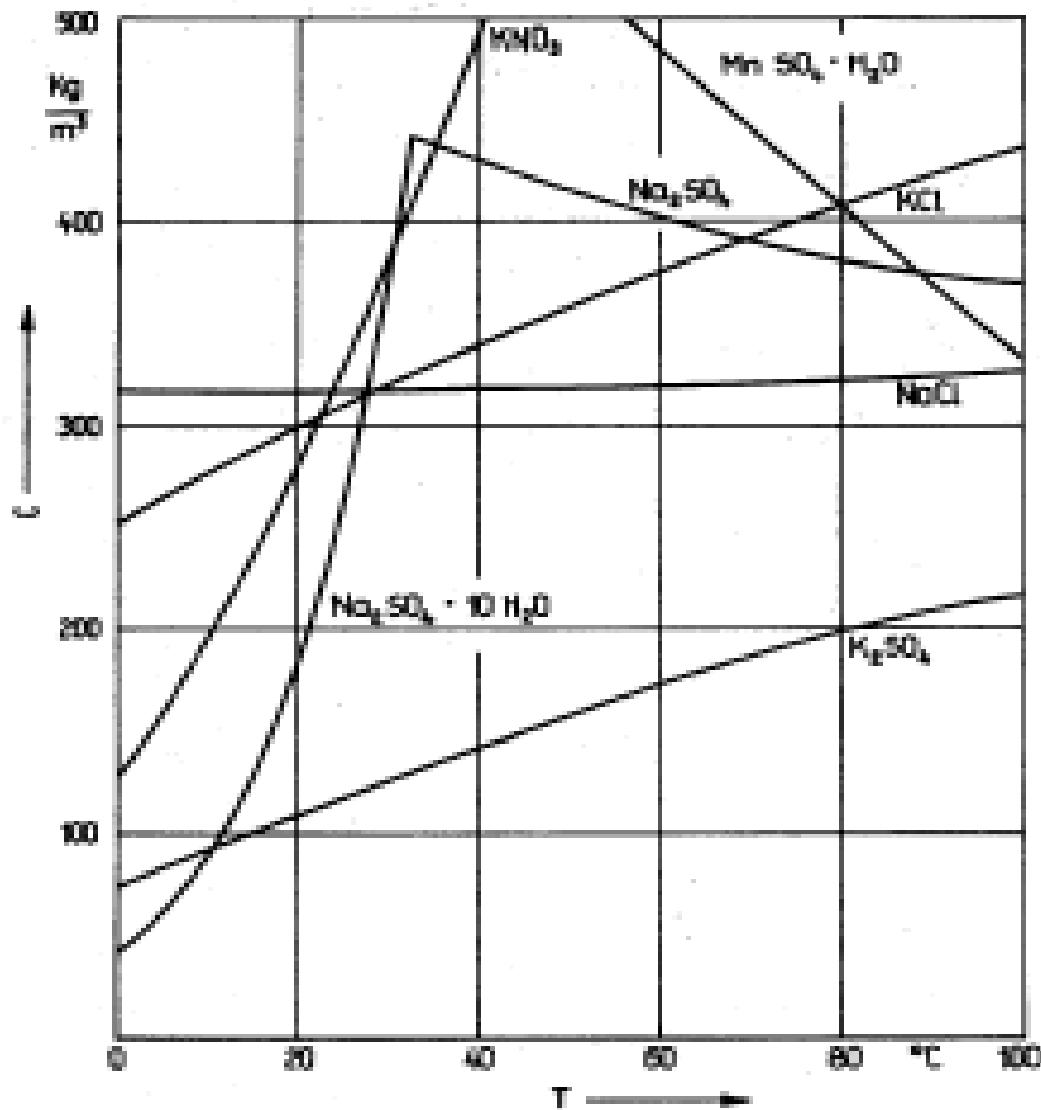
## Solubility diagram - solutions

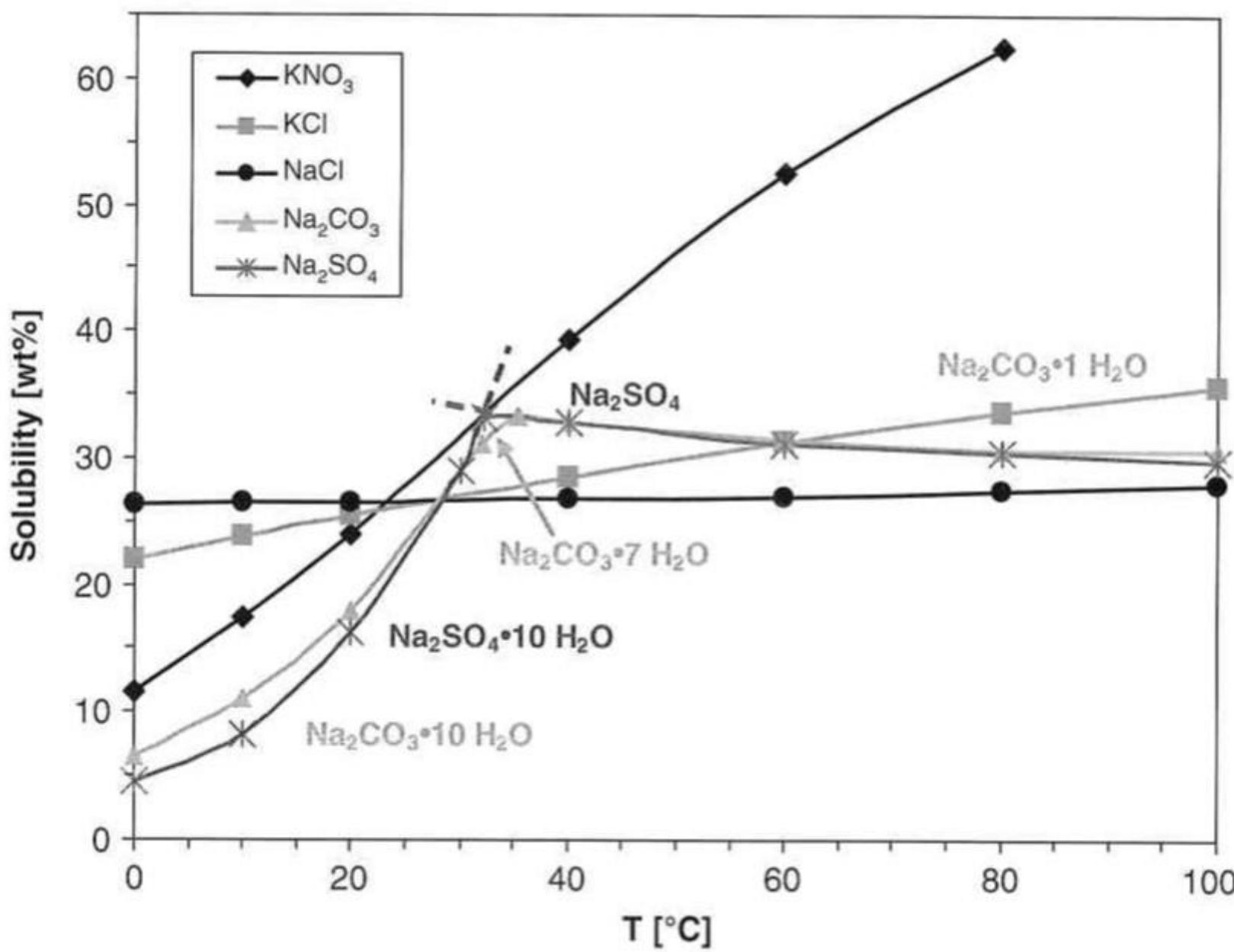
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# Temperature-Solubility-Diagram





kg hydrate / kg solution

kg anhydrous / kg solution

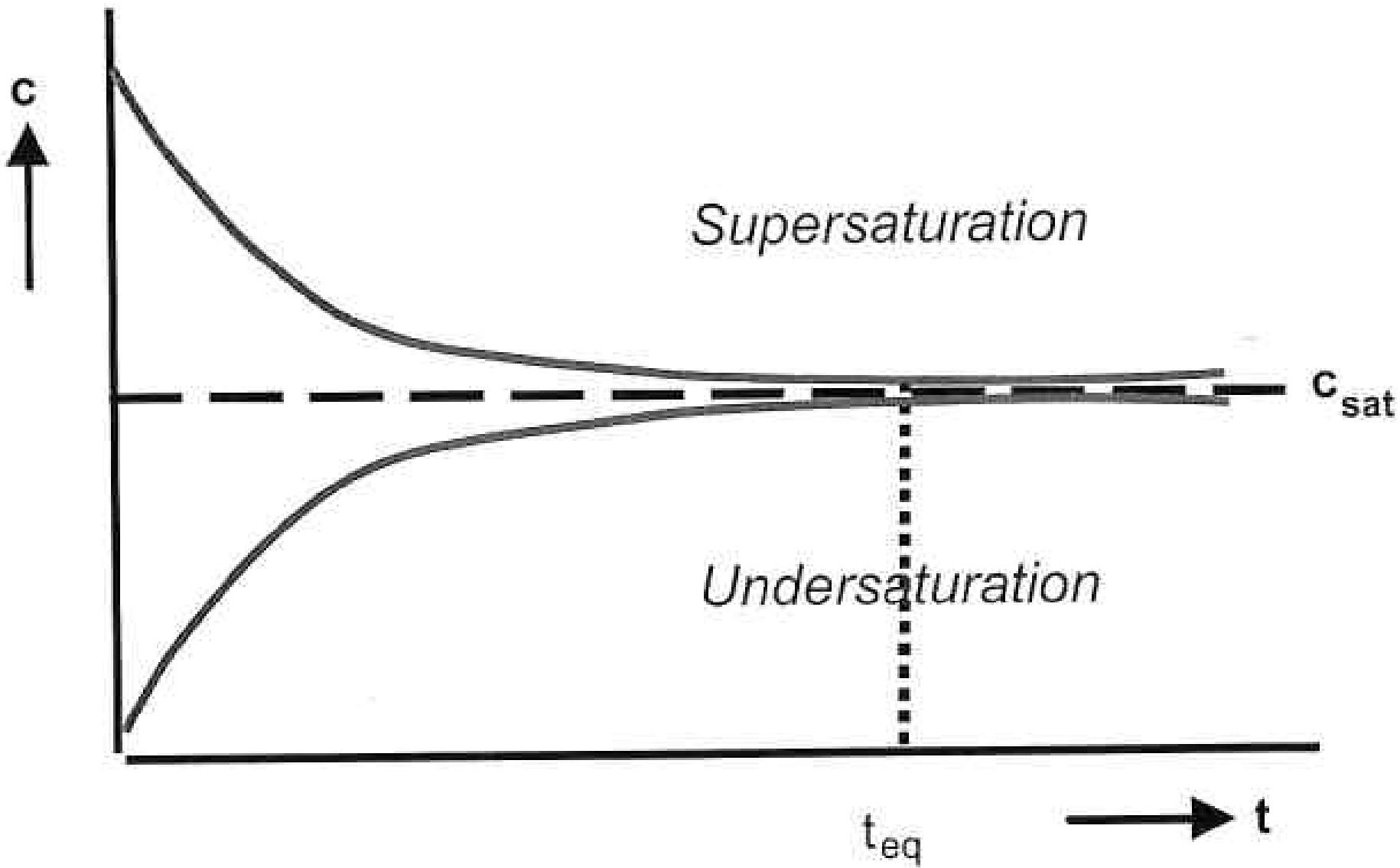
kg hydrate / kg solvent

kg anhydrous / kg solvent

kg hydrate / m<sup>3</sup> solvent

kg hydrate / m<sup>3</sup> solution

mole hydrate / mole solution etc.

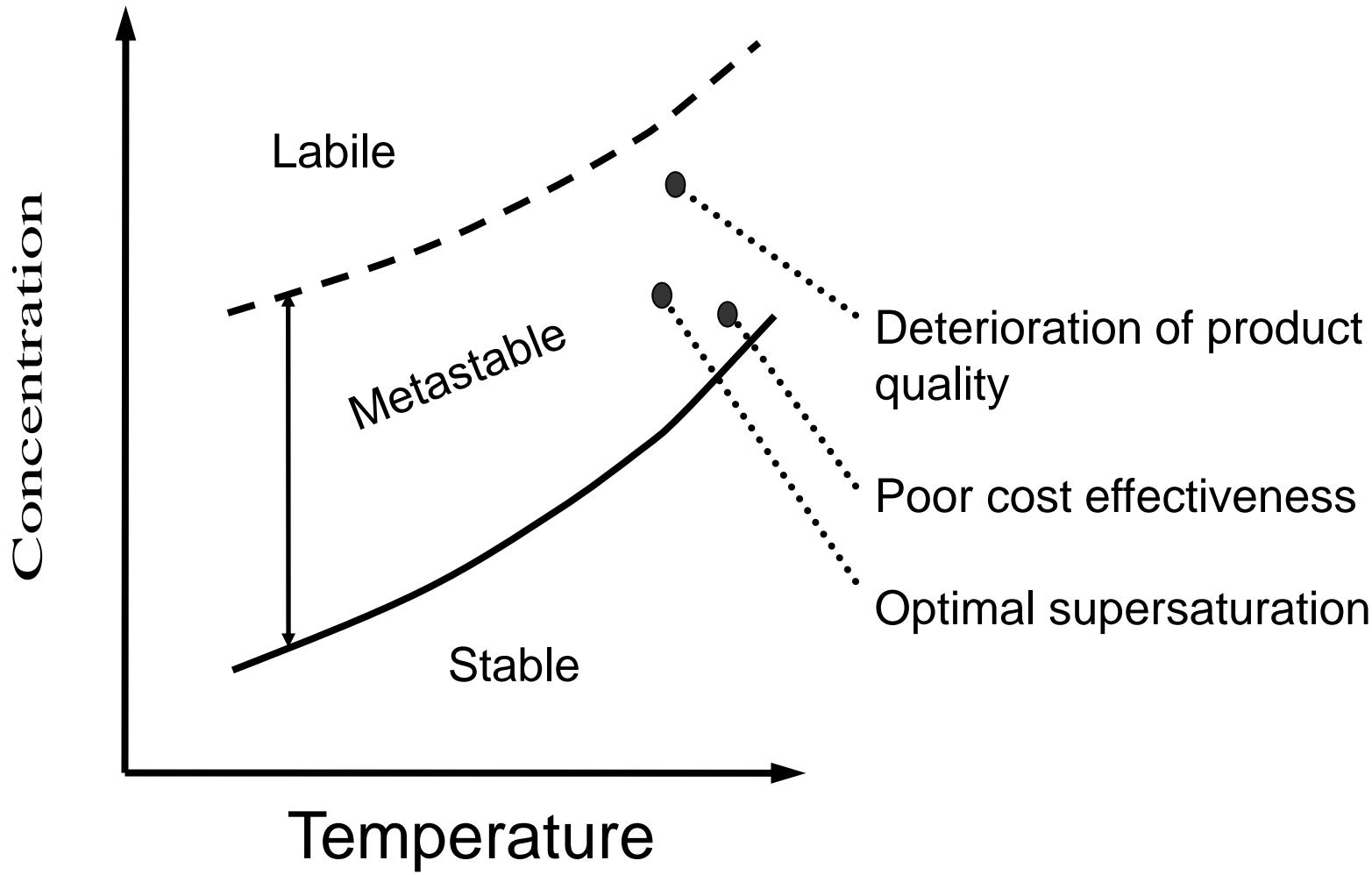


# Metastable zone width

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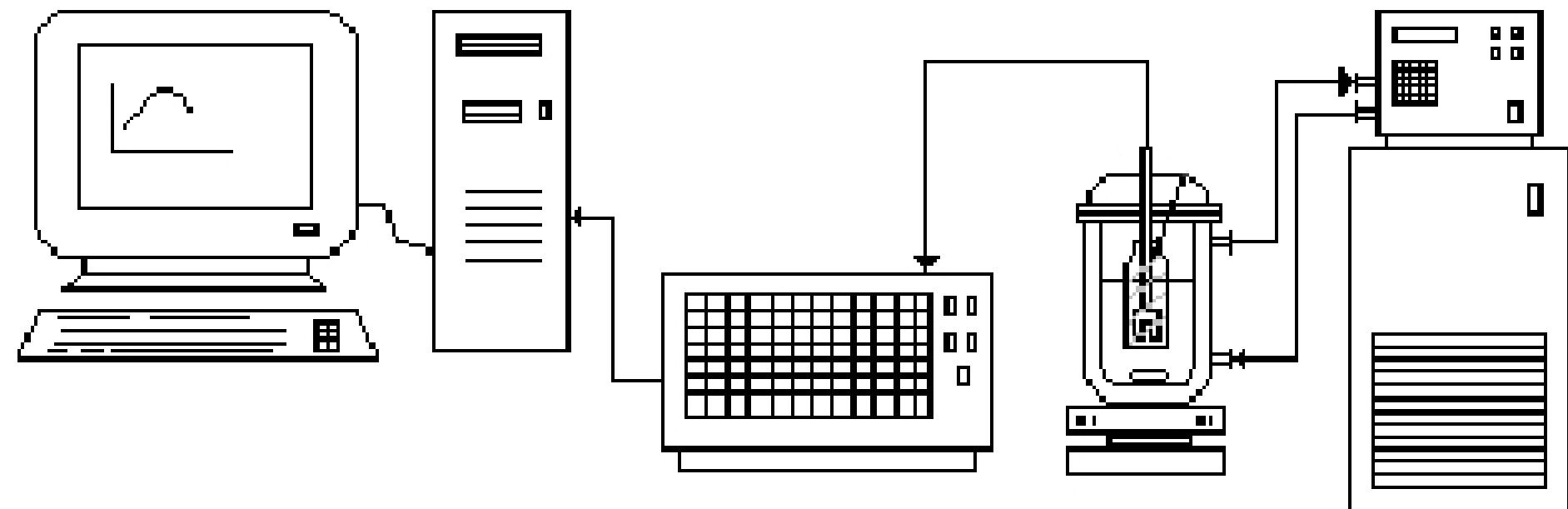
- What is it ?
- How to determine ?
- How to influence ?
- Why important ?

# Metastable zone



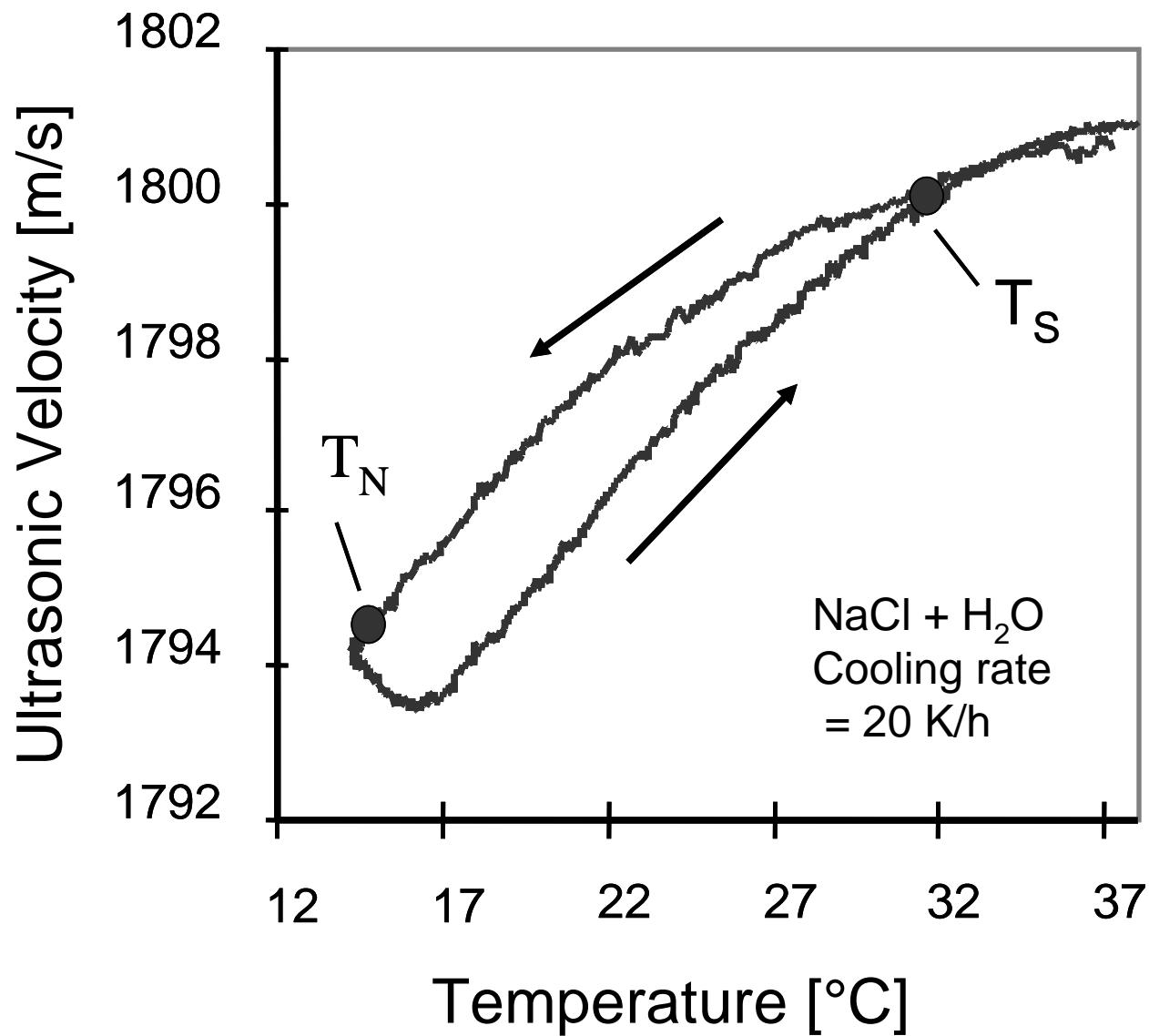
# In line process control ultrasonic sensor

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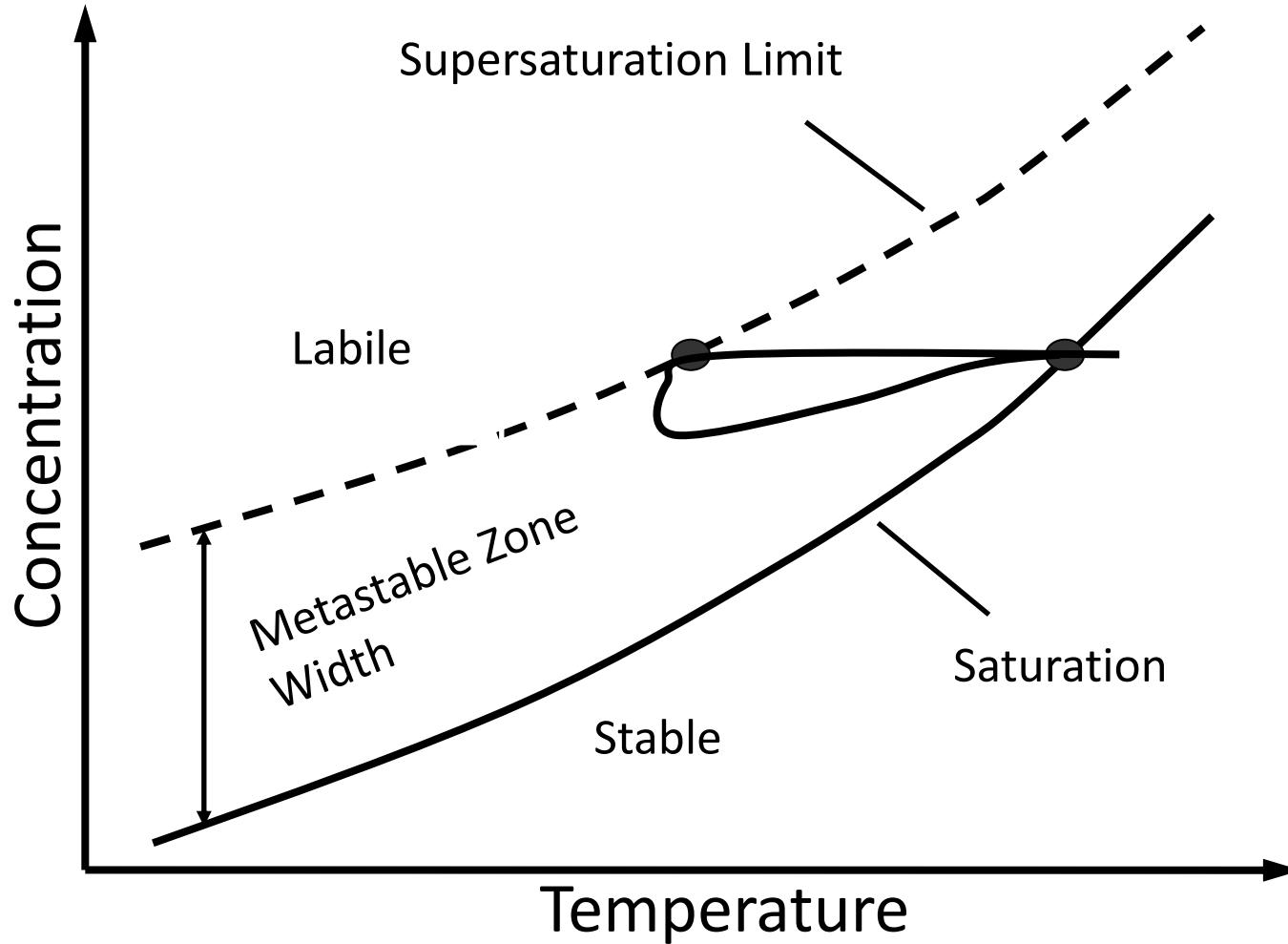
# Process parameters

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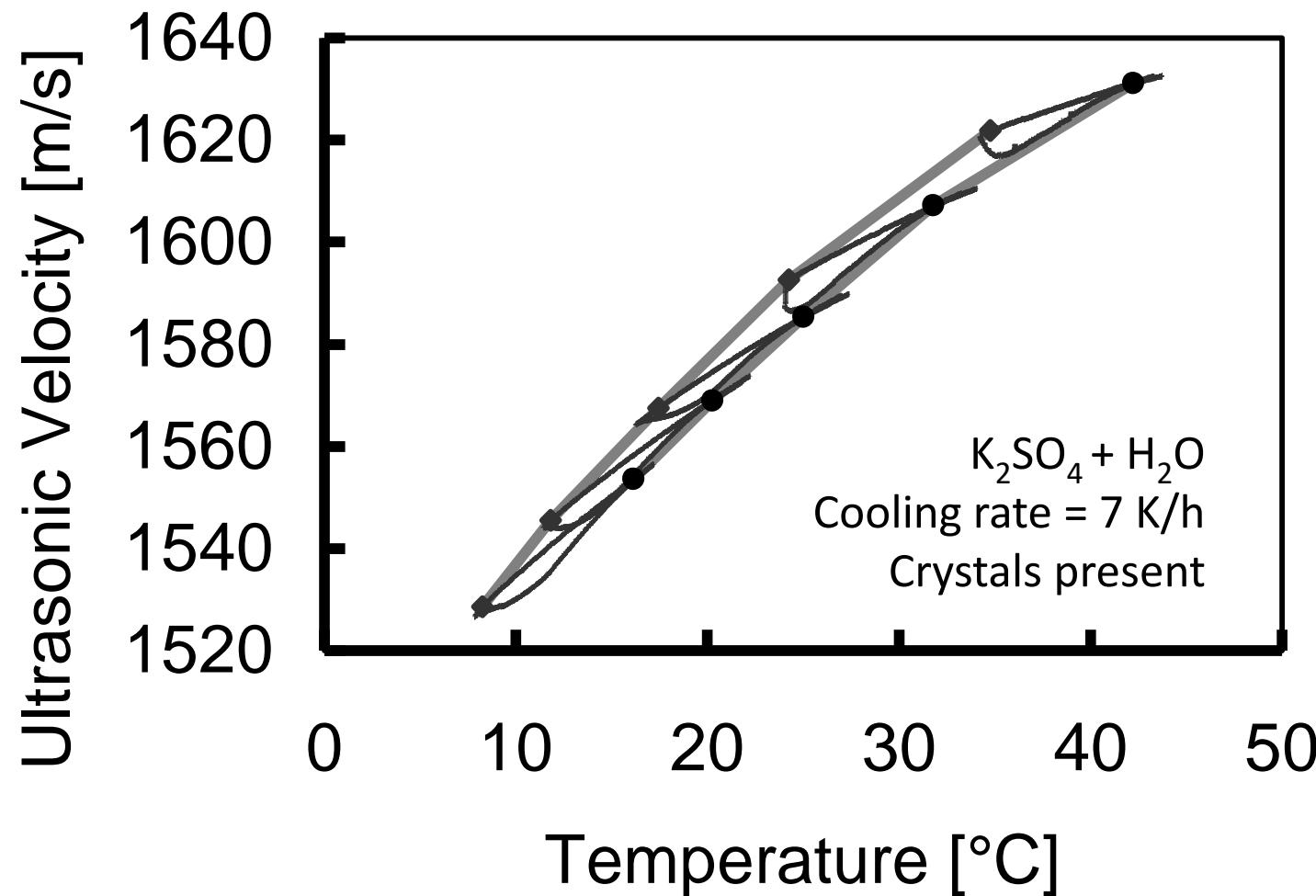
# Determination of metastable zone width I

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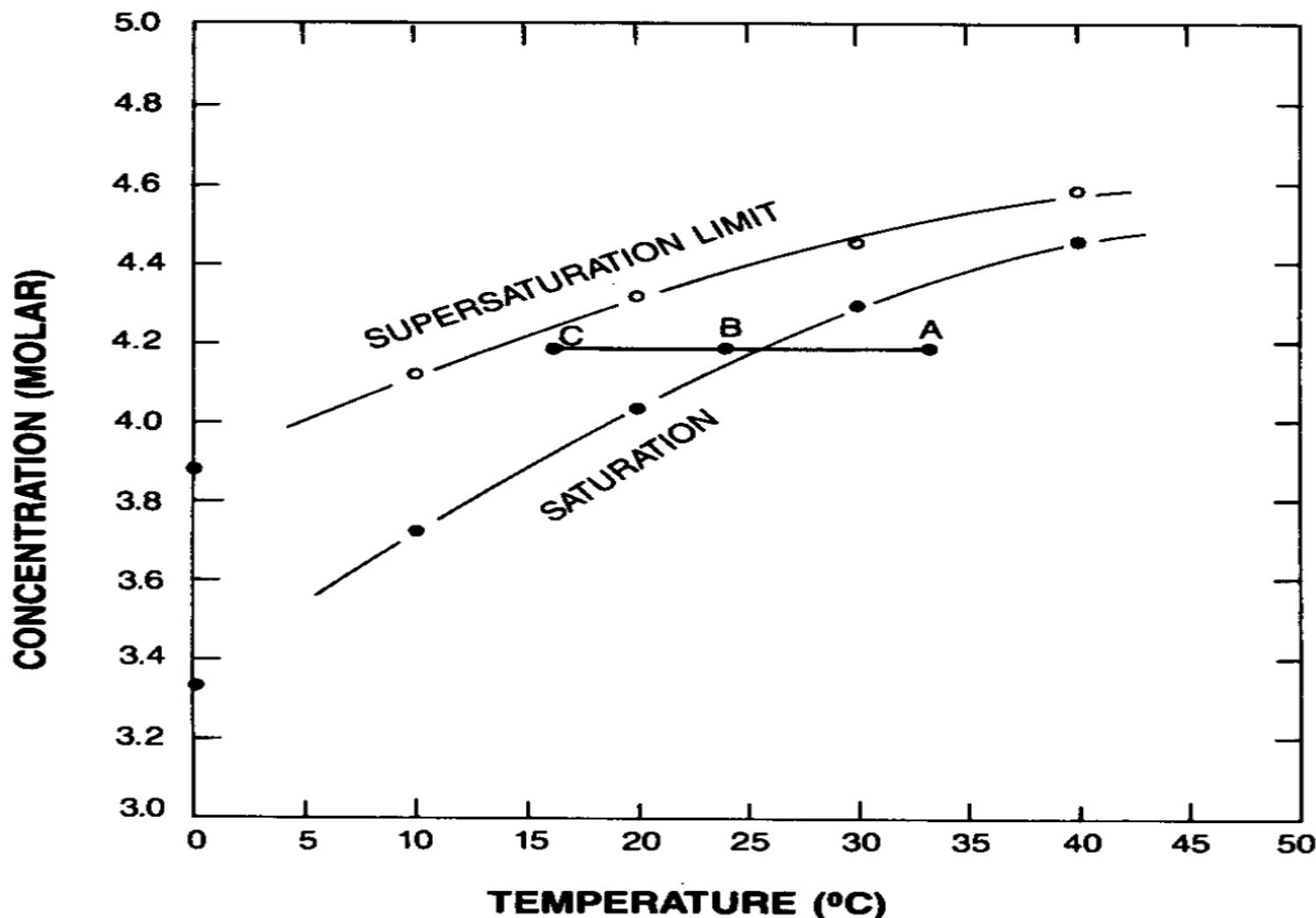


# Determination of metastable zone width II

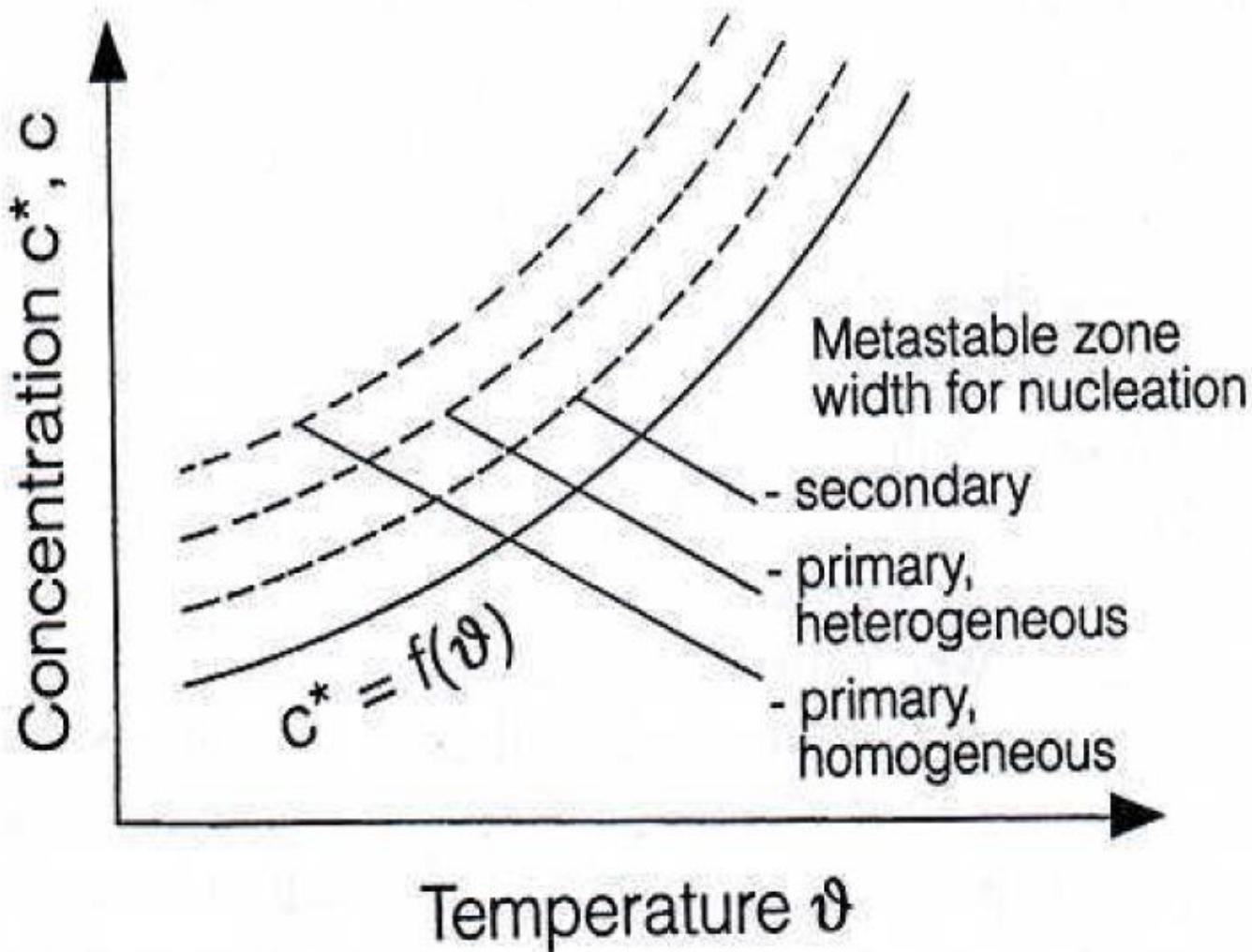
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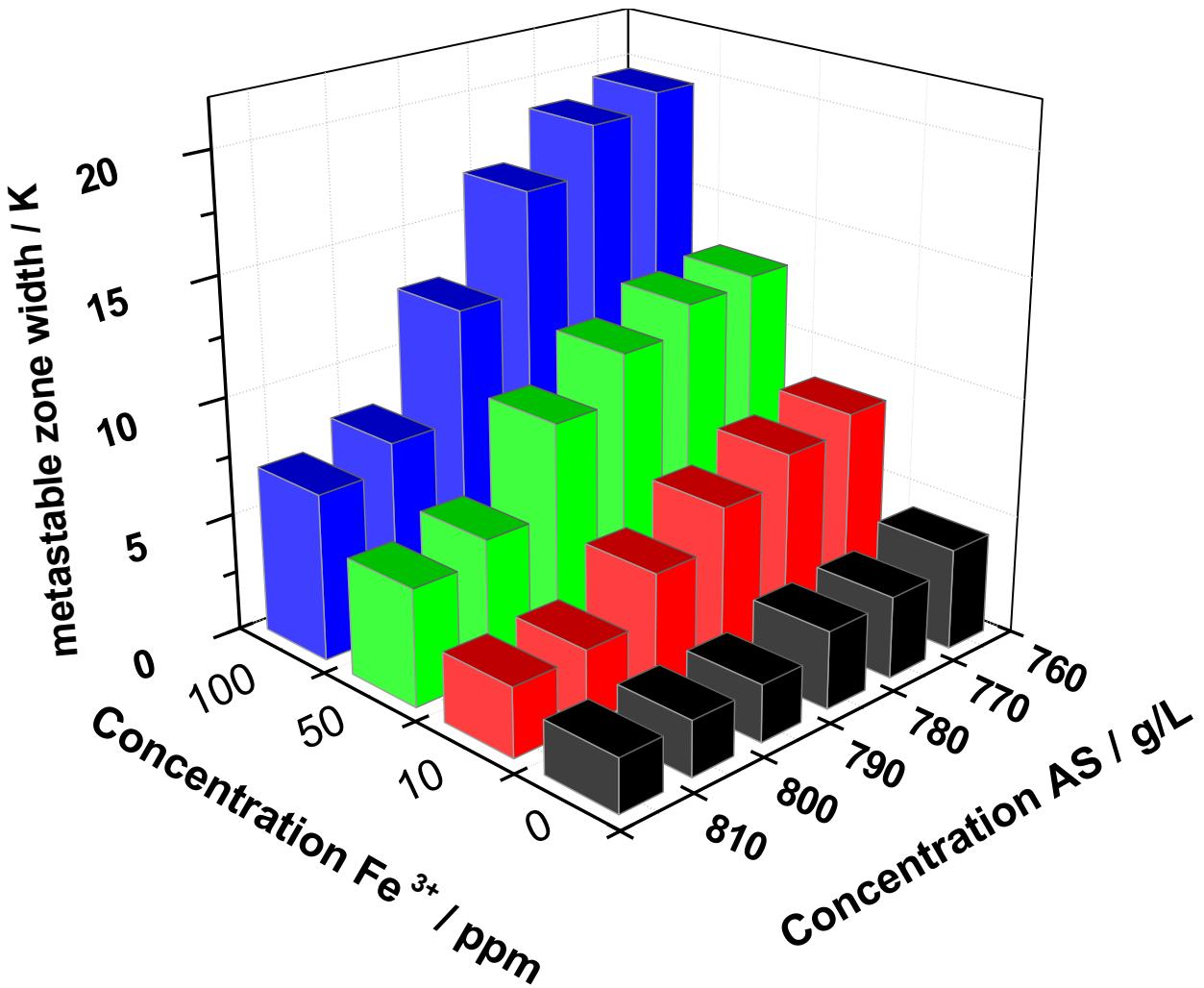
## Metastable zone width for KCl-water system (Chang 1984)



## Metastable zone width for nucleation



# Effects on Metastable Zone Width



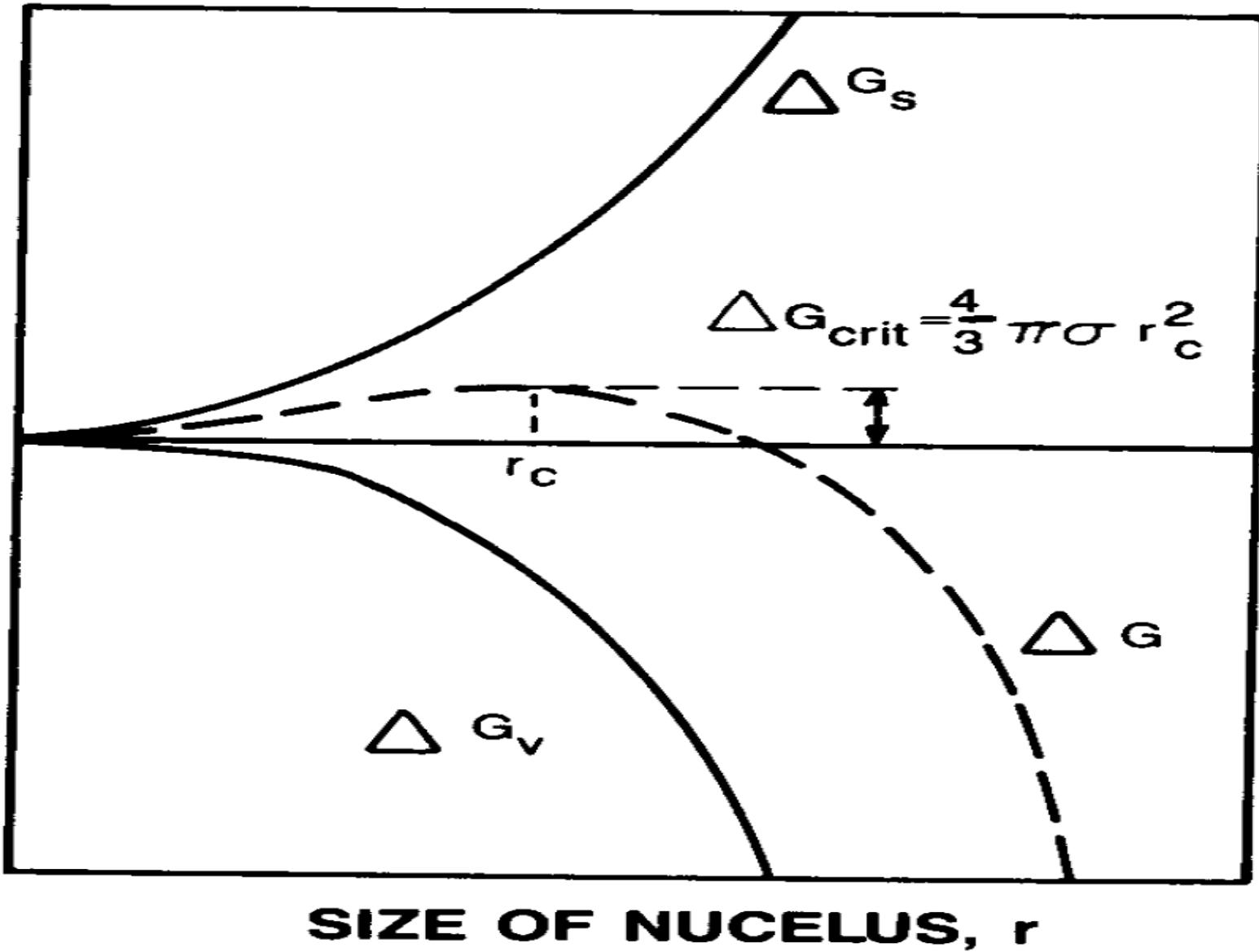
Effect of  $\text{Fe}^{3+}$  on the metastable zone width of ammonium sulfate at pH 4

Solute	Dimensionless solubility $C^*/C_C$	Solubility parameter $d(\ln C^*)$ $\over d(\ln T)$	Maximum detectable subcooling $\Delta T_{\text{met,exp}}$ in K for $dT/dt =$		
			2 K/h	5 K/h	20 K/h
Calcium nitrate	0.71	2.0	0.6	0.9	1.5
Boric acid	0.04	7.9	1.3	1.9	3.1
Potassium bromide	0.20	1.4	1.1	1.6	2.7
Potassium iodide	0.33	0.6	0.6	0.8	1.2
Potassium nitrite	0.62	0.3	0.9	1.2	1.8
Potassium nitrate	0.18	7.0	0.4	0.5	0.7
Sodium sulfite	0.39	6.6	0.56	0.6	0.7
Sodium bromide	0.48	1.2	1.0	1.4	2.3
Sodium iodide	0.64	0.7	1.2	1.4	2.0
Sodium nitrite	0.29	1.2	1.4	1.8	2.6

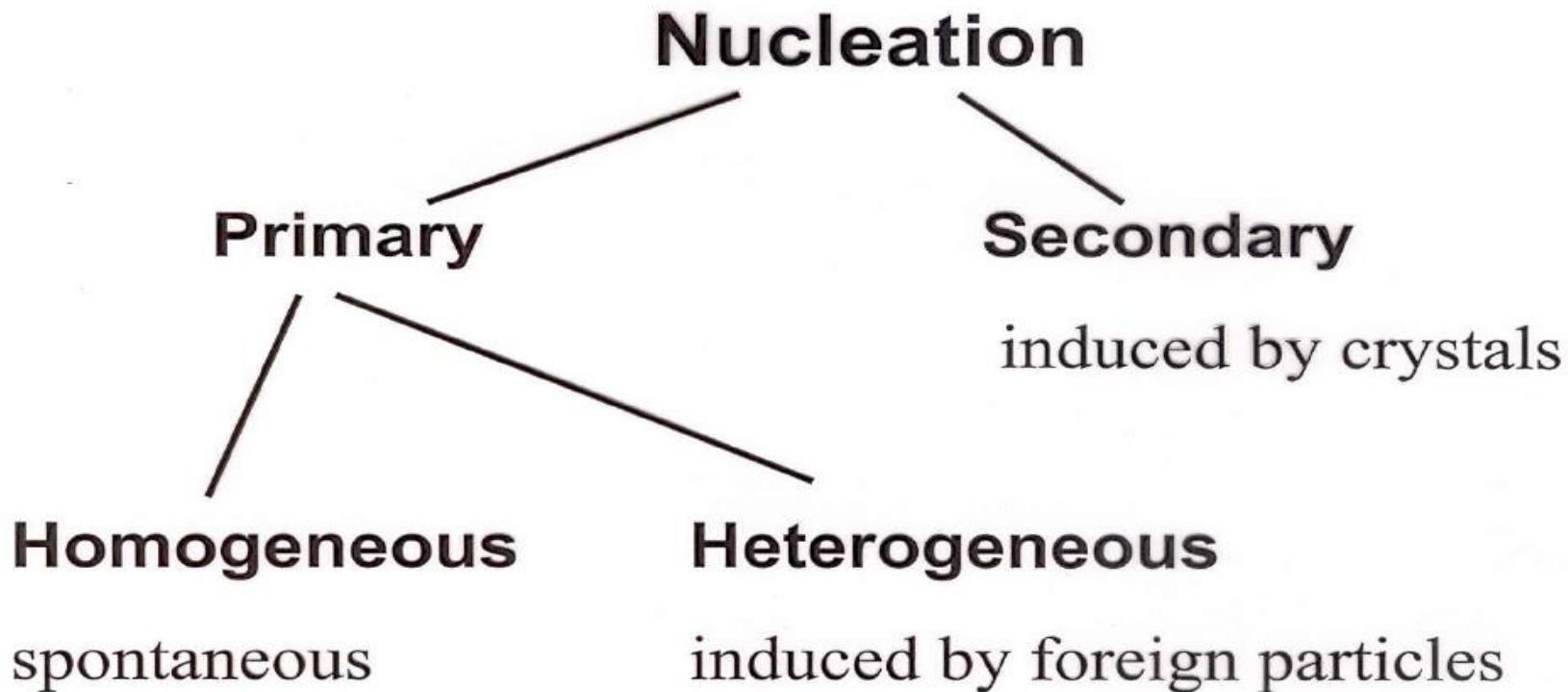
No.	Solute	Formula	Molar mass (Anh/Hyd)	$\tilde{M}$ [kg/kmol]	$h_{20}$ [-]	$\rho_c$ [kg/m <sup>3</sup> ]	$C_c$ [kmol/m <sup>3</sup> ]	Density (Hydrate)	Mass ratio (Hydrate)	Density	Solubility (Hydrate)	$C^*/C_c$ [-]	Heat of crystall.	No.	
<b>ALUMINIUM</b>															
1	chloride	AlCl <sub>3</sub>	133.34 241.432	6	2398	9.93		1.3068		1492	3.500	0.35		-13	1
2	hydroxide	Al(OH) <sub>3</sub>	77.99	0	2420	31.03		0.00012		998	0.002	5.0E-5			2
3	sulphate	Al <sub>2</sub> (SO <sub>4</sub> ) <sub>3</sub>	342.134 630.379	16	1690	2.68		1.0017		1321 1255	0.997	0.37		-64	3
<b>AMMONIUM</b>															
4	aluminium sulphate	(NH <sub>4</sub> ) <sub>2</sub> Al <sub>2</sub> (SO <sub>4</sub> ) <sub>4</sub>	474.306 906.672	24	1640	1.81		0.1107		1050 1039	0.115	0.06			4
5	bromide	NH <sub>4</sub> Br	97.942	0	2429	24.80		0.755		1300 1337	5.710	0.23		-15	5
6	chloride	NH <sub>4</sub> Cl	53.491	0	1527	28.55		0.372		1076 1102	5.454	0.19		16.2	6
7	dihydrogen phosphate	NH <sub>4</sub> H <sub>2</sub> PO <sub>4</sub>	115.025	0	1803	15.67		0.365		1160 1134	2.697	0.17			7
8	ferrous sulphate	(NH <sub>4</sub> ) <sub>2</sub> Fe(SO <sub>4</sub> ) <sub>2</sub>	284.038 392.13	6	1864	4.75		0.3798		1171 1145	0.803	0.17			8
9	hydrogen carbonate	NH <sub>4</sub> HCO <sub>3</sub>	79.055	0	1580	19.99		0.21		1066	2.341	0.12			9
10	nickel sulphate	(NH <sub>4</sub> ) <sub>2</sub> Ni(SO <sub>4</sub> ) <sub>2</sub>	286.908 395	6	1923	4.87				1052					10
11	nitrate	NH <sub>4</sub> NO <sub>3</sub>	80.043	0	1725	21.55		1.92		1310 1381	10.761	0.50		-12	11

Free energy versus cluster radius (Mullin 1972)

FREE ENERGY,  $\Delta G$

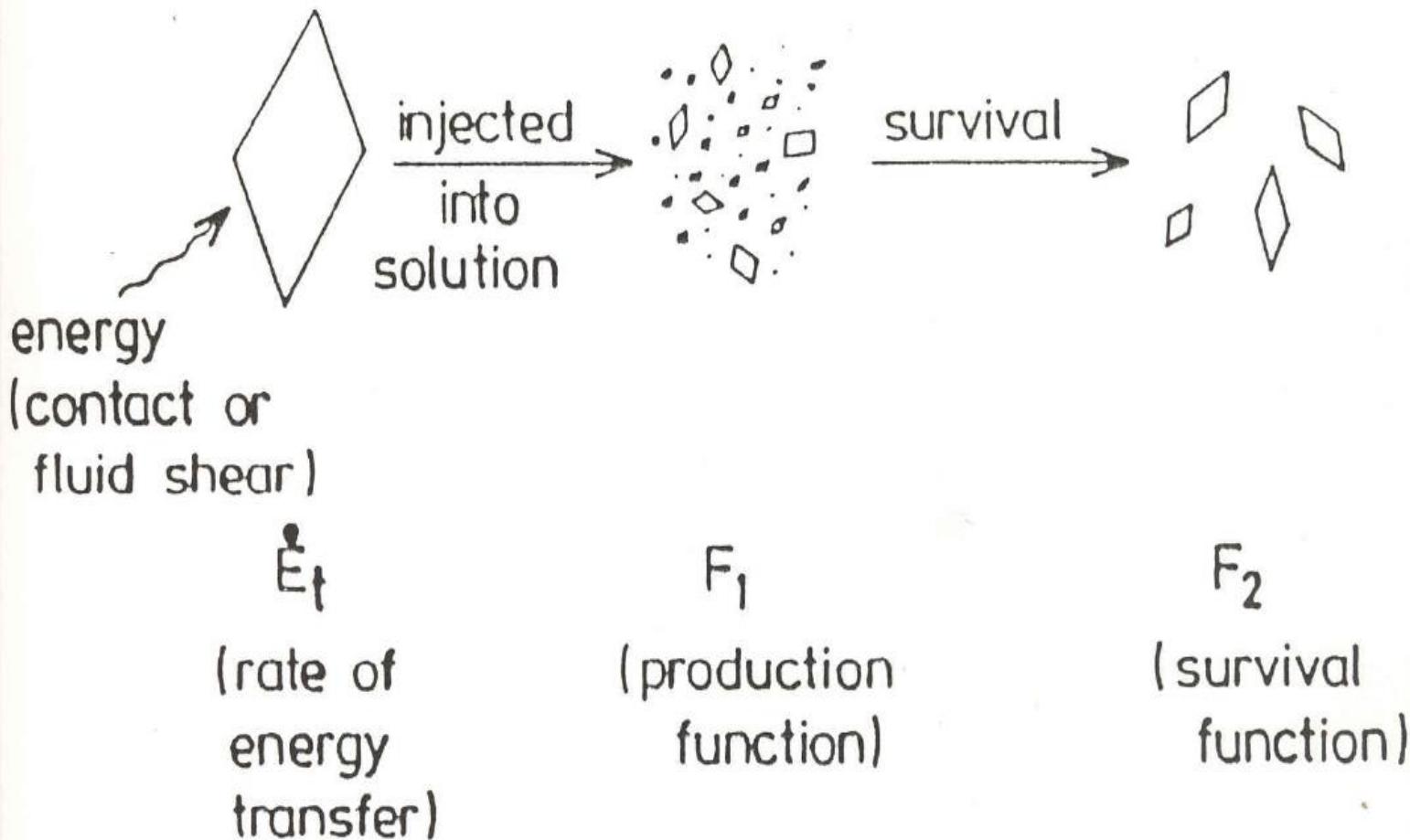


# Mechanisms of Nucleation

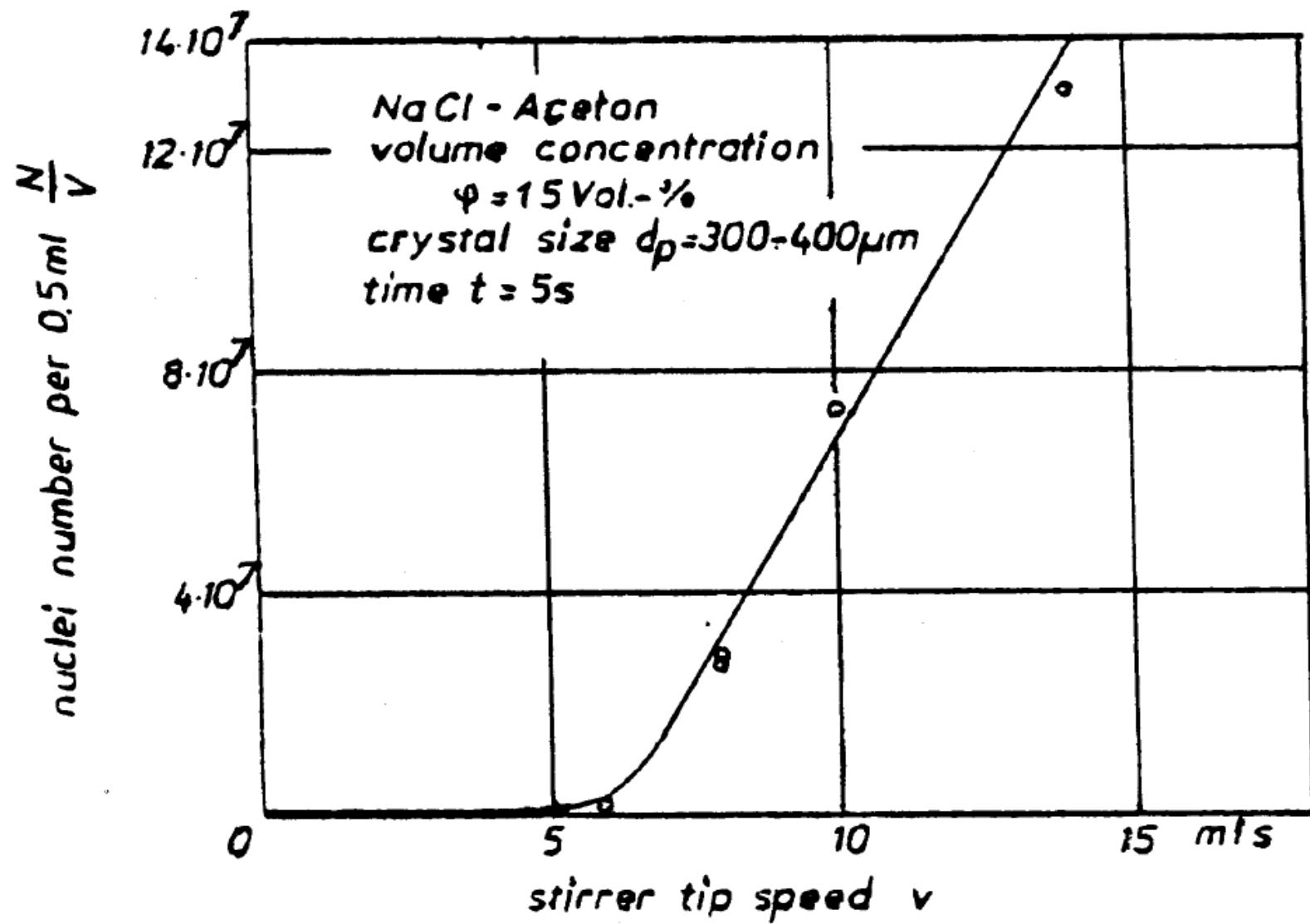


<u>Supersaturation S</u>	<u>Time</u>
1.0	Infinity
2.0	$10^{60}$ years
3.0	$10^3$ years
4.0	0.1 second
5.0	$10^{-13}$ second

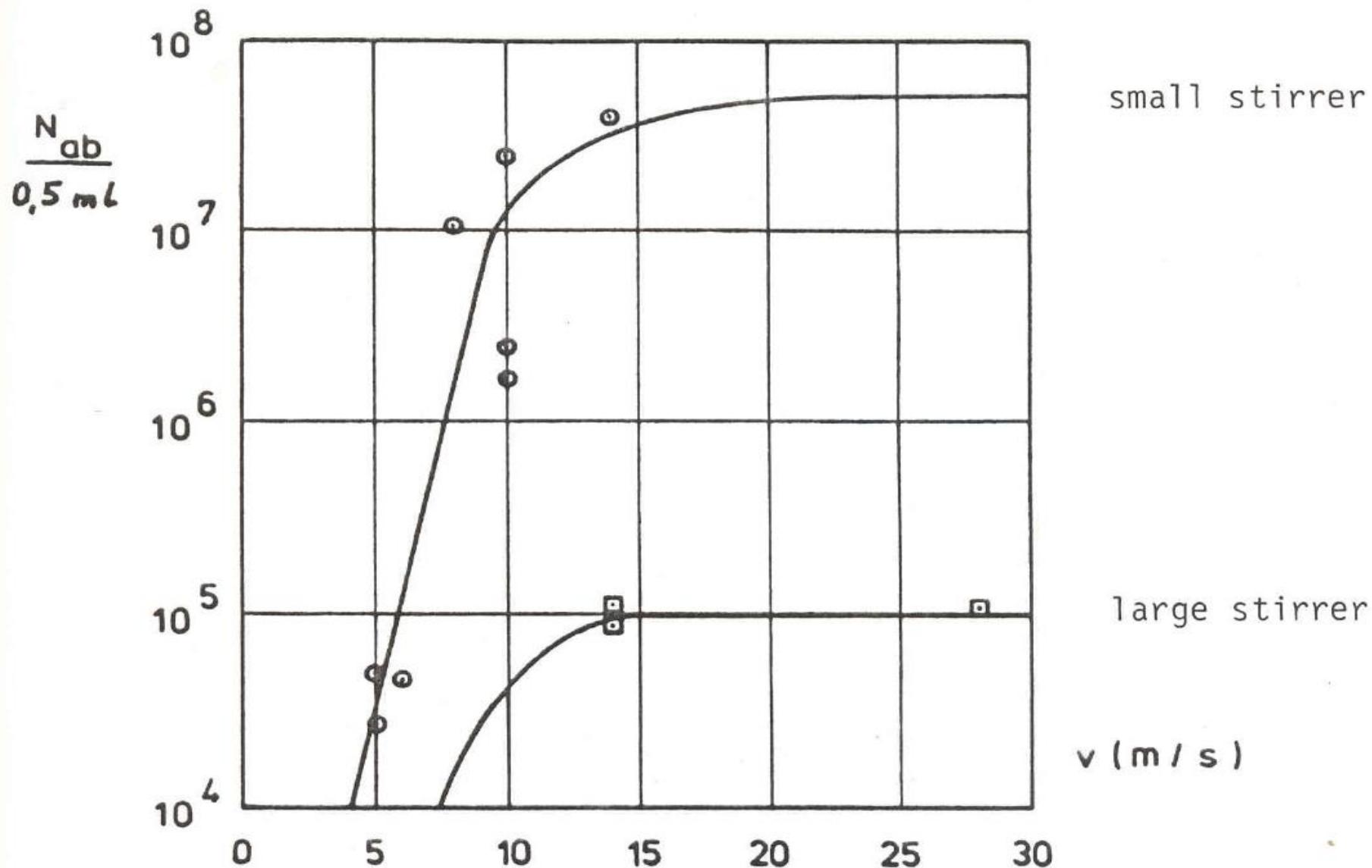
## Secondary nucleation in crystallizers



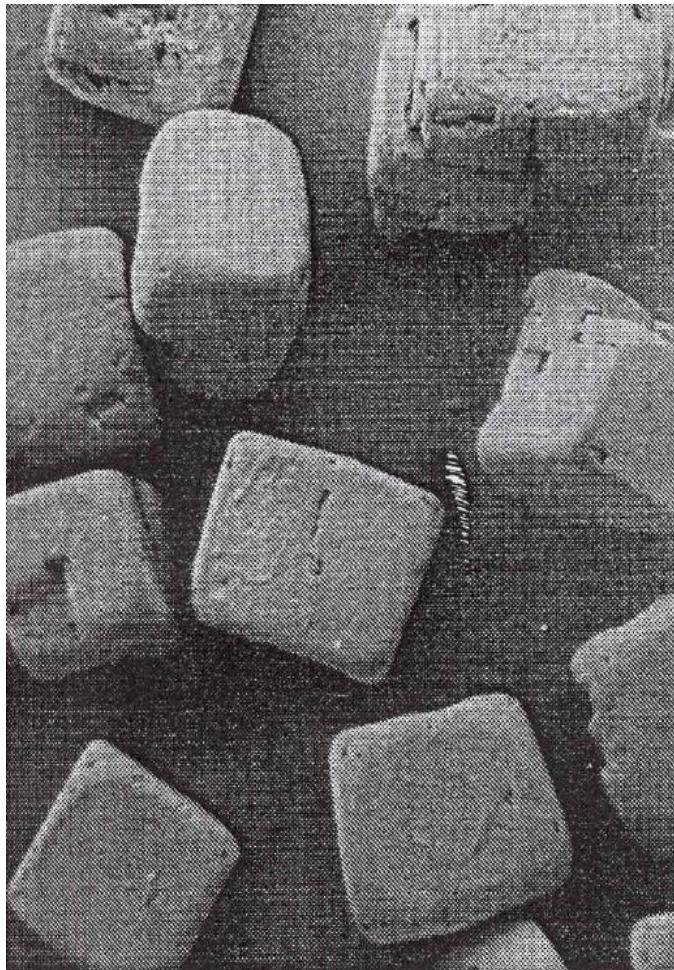
## Number of nucleiverses impeller tip speed



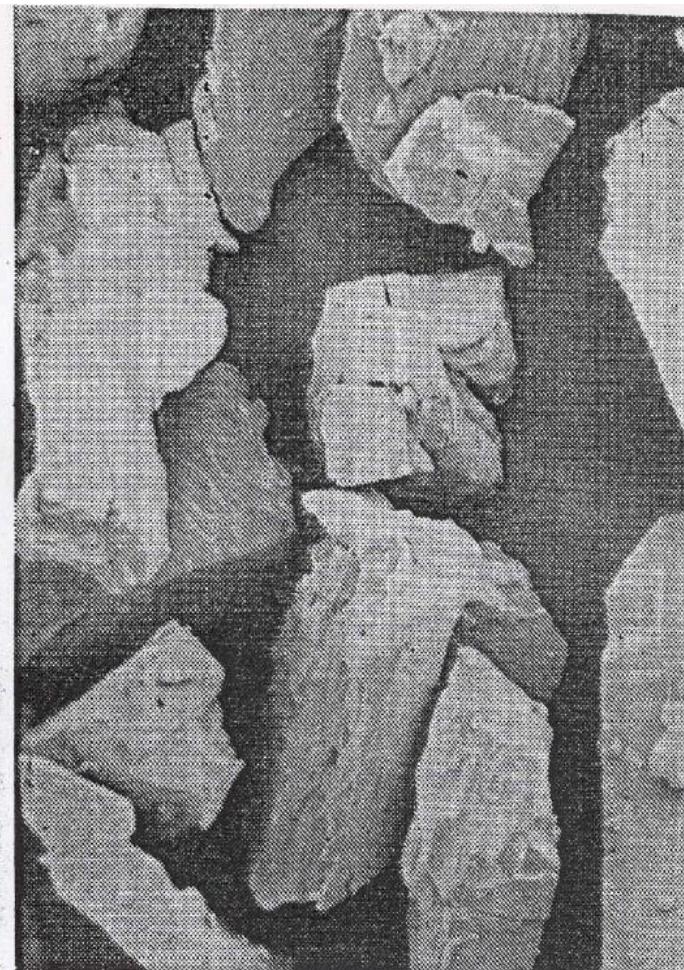
# Number of attrition particles depending on stirrer speed for two different size stirrers



Electron microscope photographs (1 mm radial clearance,  
 $M = 20 \text{ kg/m}^3$ ,  $N = 9 \text{ rps}$ , batch time = 120 s)



498–592  $\mu\text{m}$  (40  $\times$ ) Parent crystals

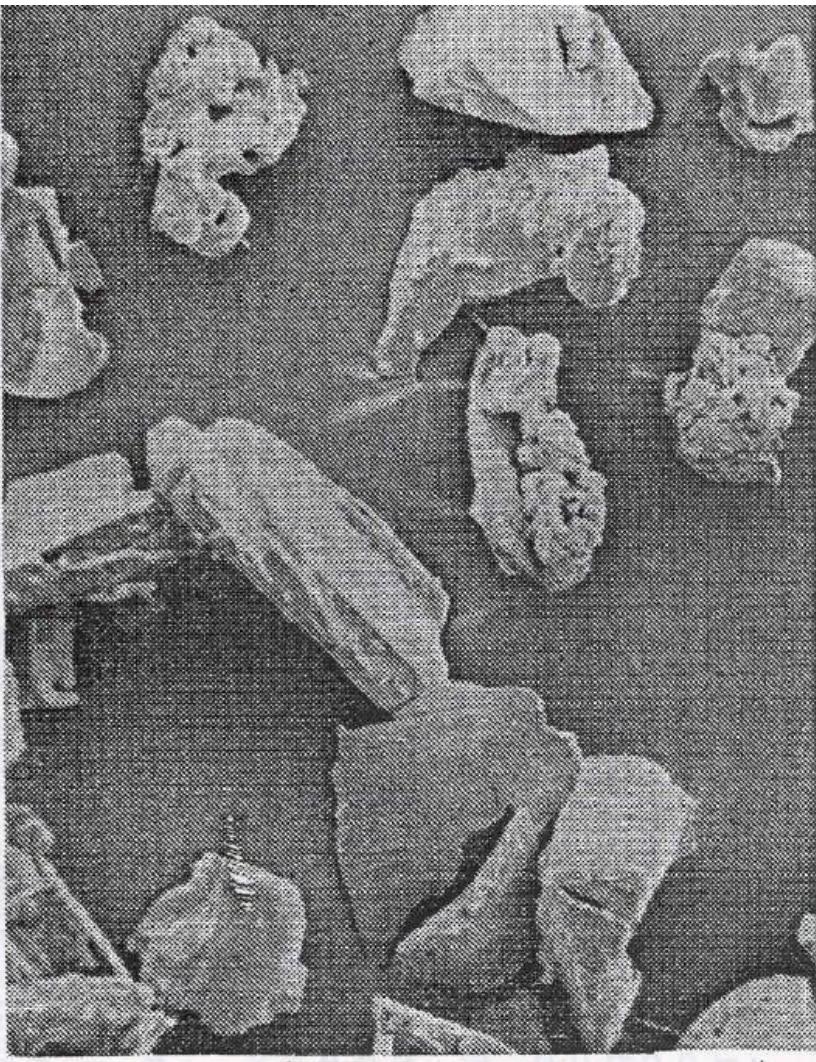


209–249  $\mu\text{m}$  (70  $\times$ )

Electron microscope photographs (1 mm radial clearance,  
 $M = 20 \text{ kg/m}^3$ ,  $N = 9 \text{ rps}$ , batch time = 120 s)



88-105  $\mu\text{m}$  (200  $\times$ )



62-74  $\mu\text{m}$  (200  $\times$ )

Thank you for your  
attention!



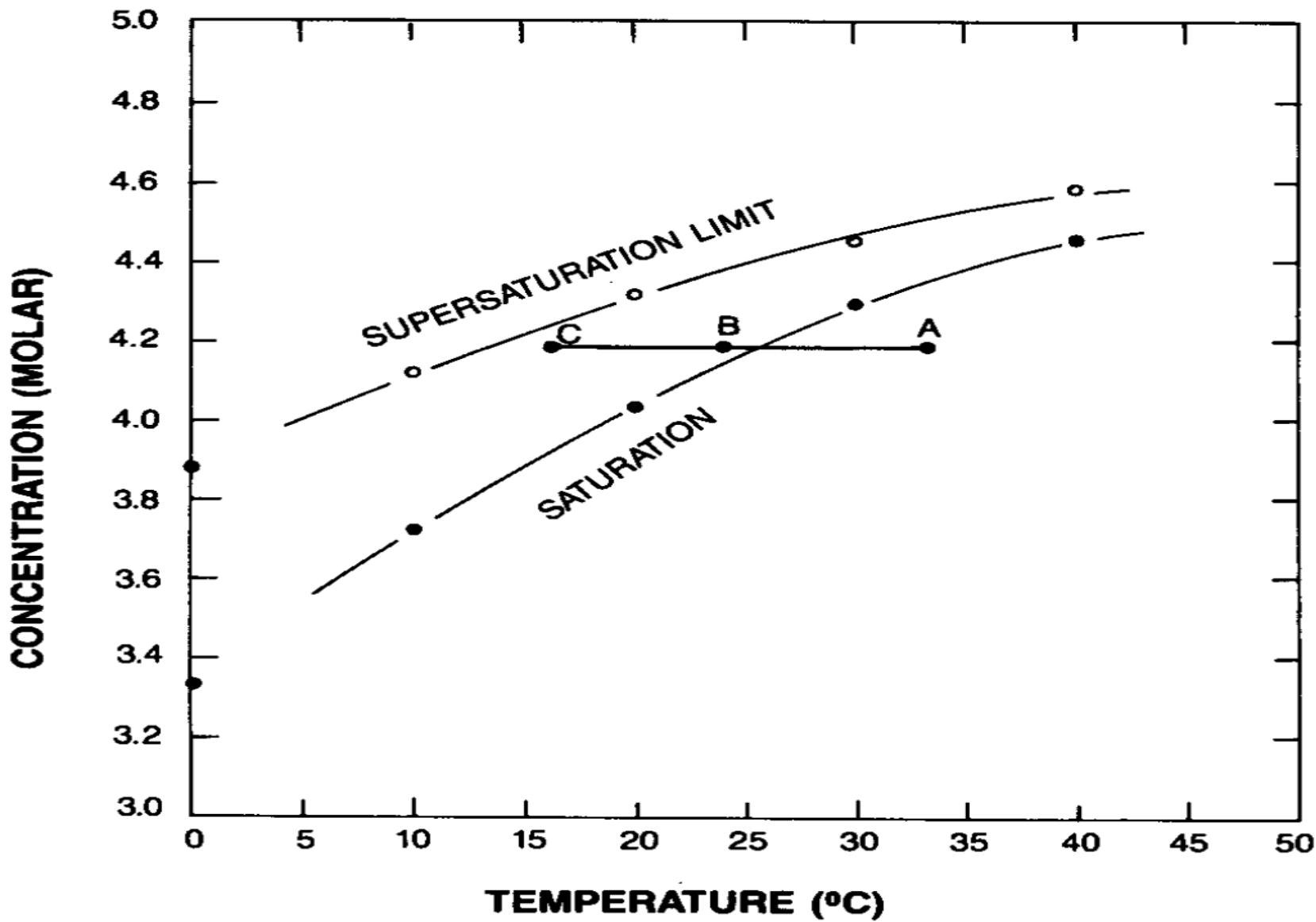
## **Kinetics of crystallization**

### **- crystal growth**

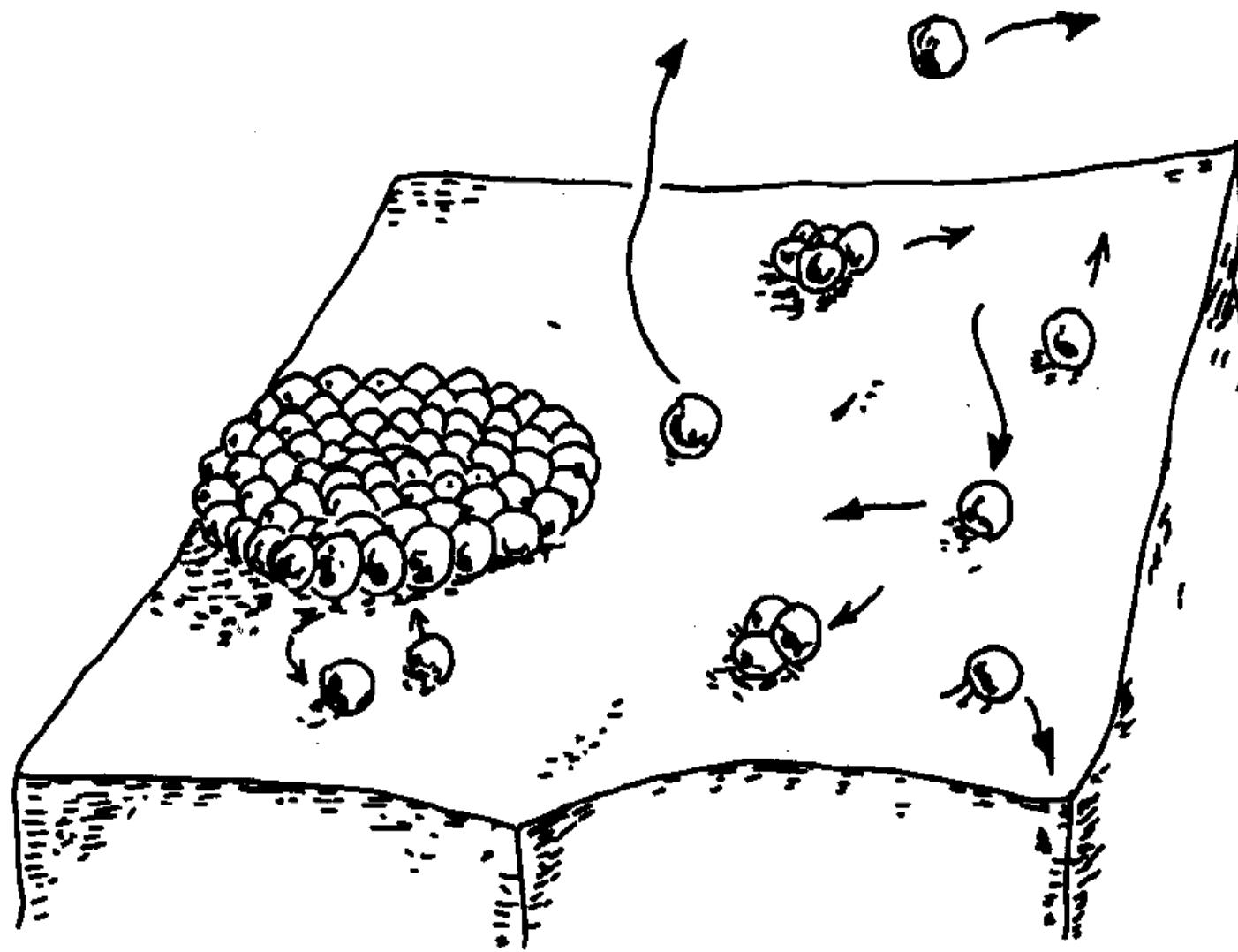
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# Metastable zone width for KCl-water system (Chang 1984)



Formation of two-dimensional critical nucleus on a crystal surface (M. Ohara and R.C. Reid)



# Crystal Growth Kinetics

## Controlled by Surface Integration: Two-Dimensional Nucleation

General form:

$$R_G = \alpha \sigma^P \exp\left(\frac{\beta}{\sigma}\right)$$

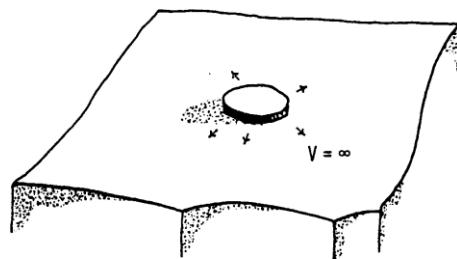
$R_G$ , growth rate

$\alpha, \beta, P$  constant

$\sigma$  relative supersaturation

- Mono-nuclear Model:

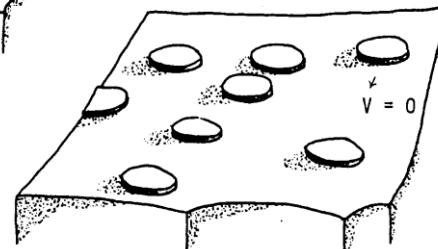
$V = \infty$  and  $P = 1/2$



(a) Mononuclear Model

- Poly-nuclear Model:

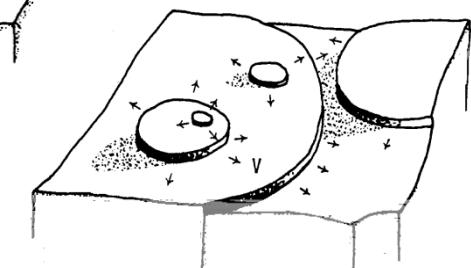
$V = 0$  and  $P = 3/2$



(b) Polynuclear Model

- Birth & Spread Model (B&S):

$V = \text{finite value}$  and  $P = 5/6$



(c) Birth and Spread Model

[8] Myerson, A.S., Handbook of Industrial Crystallization; Butterworth-Heinemann; Oxford, UK, 2001, 70-71.

# Crystal Growth Kinetics

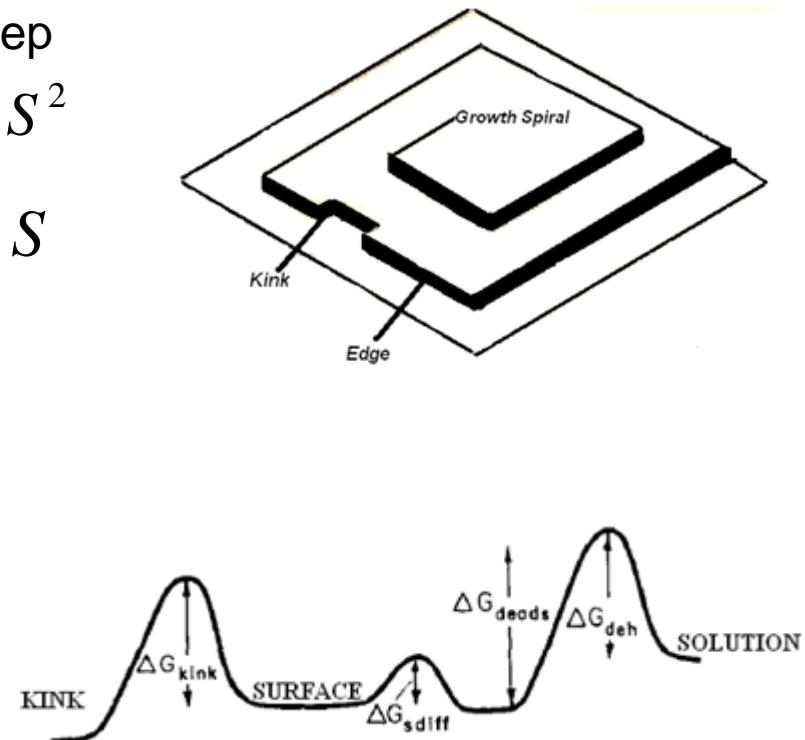
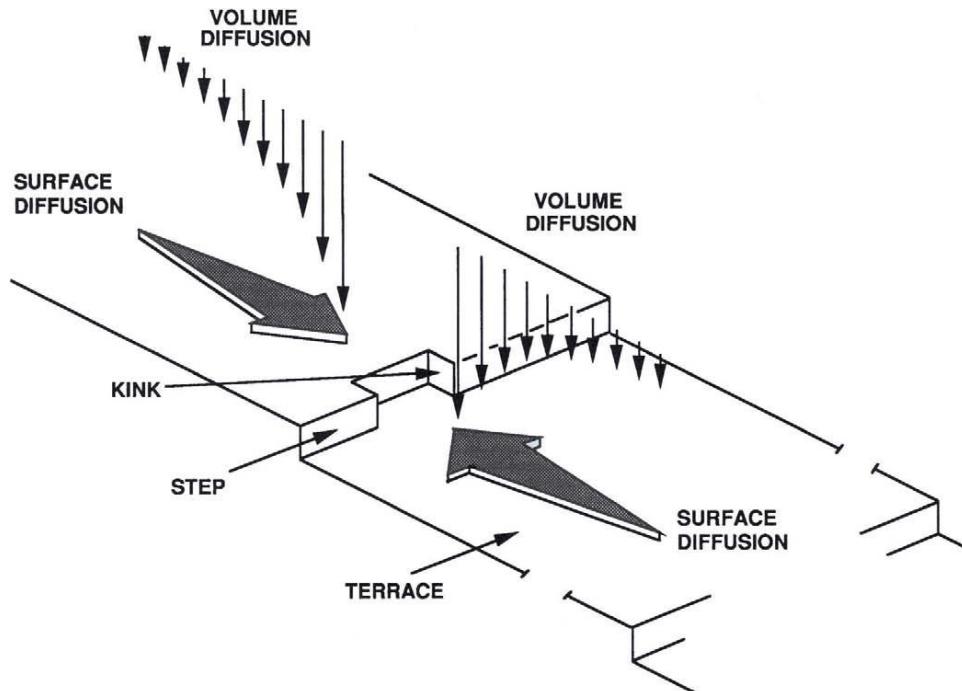
Controlled by Surface Integration: Burton-Cabrera-Frank (BCF) Model

Screw dislocations provide self perpetuating step

- low Supersaturations (BCF):
- high Supersaturations (RIG):

$$R_G \propto S^2$$

$$R_G \propto S$$

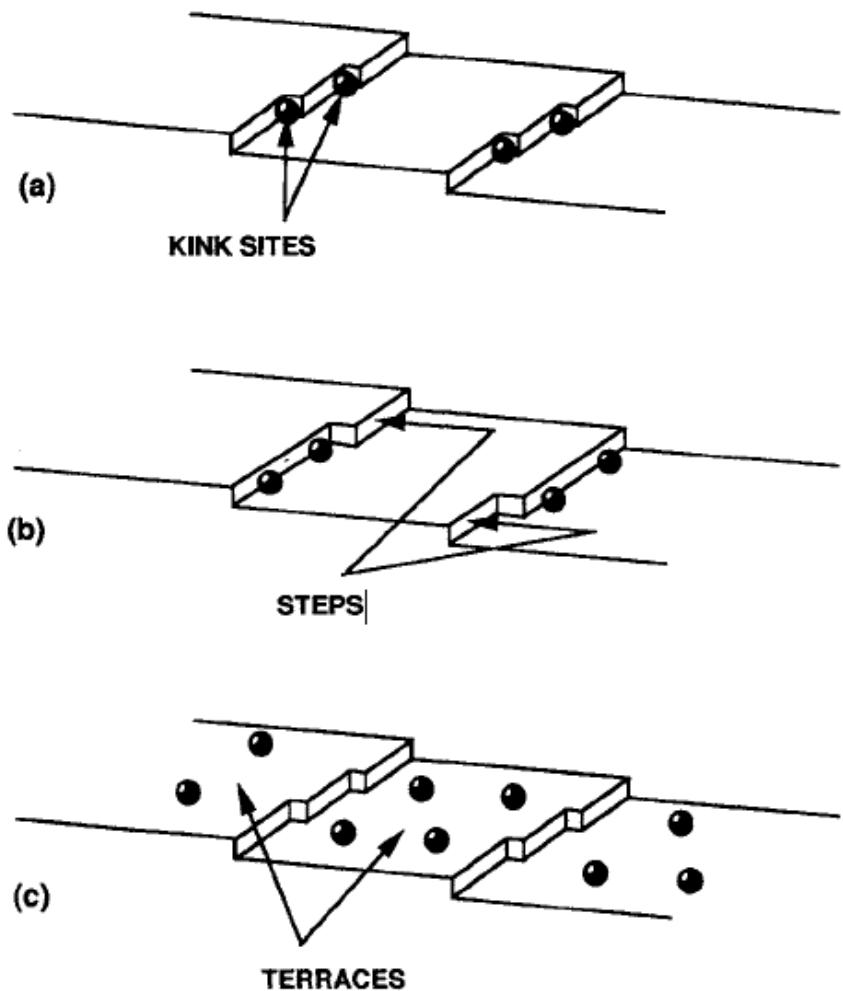
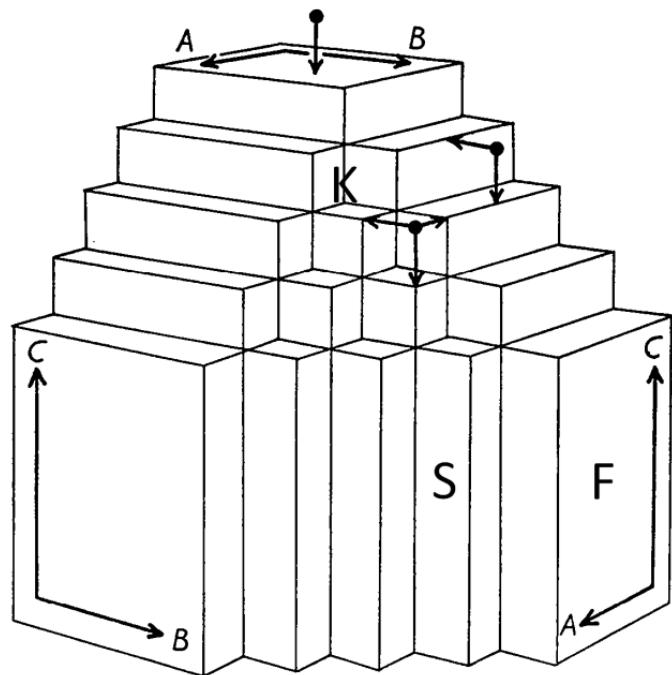


[8] Myerson, A.S., Handbook of Industrial Crystallization; Butterworth-Heinemann; Oxford, UK, 2001 ,70-71.

# Crystal Growth Kinetics

## Kossel Crystal

$$E_K^{att} \gg E_S^{att} \gg E_F^{att}$$



- [8] Myerson, A.S., Handbook of Industrial Crystallization; Butterworth-Heinemann; Oxford (2001) 70.  
[9] Mullin, J.W., Crystallization; Butterworth Heinemann, Oxford (2001) 271.

# Crystal Growth Kinetics

## Controlled by Mass Integration: Diffusion Layer Model

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- For one-dimensional case, rate of mass increase equated to diffusion rate through the boundary layer

$$\frac{dm_c}{dt} = DA \left( \frac{dC}{dx} \right) \quad R_G = \frac{\beta}{3\alpha\rho} \left( \frac{C - C_i}{\delta} \right) D \Rightarrow R_G \propto D$$

$A$ : surface area of the crystal

$D$ : diffusion coefficient

$dC/dx$ : concentration gradient in boundary layer

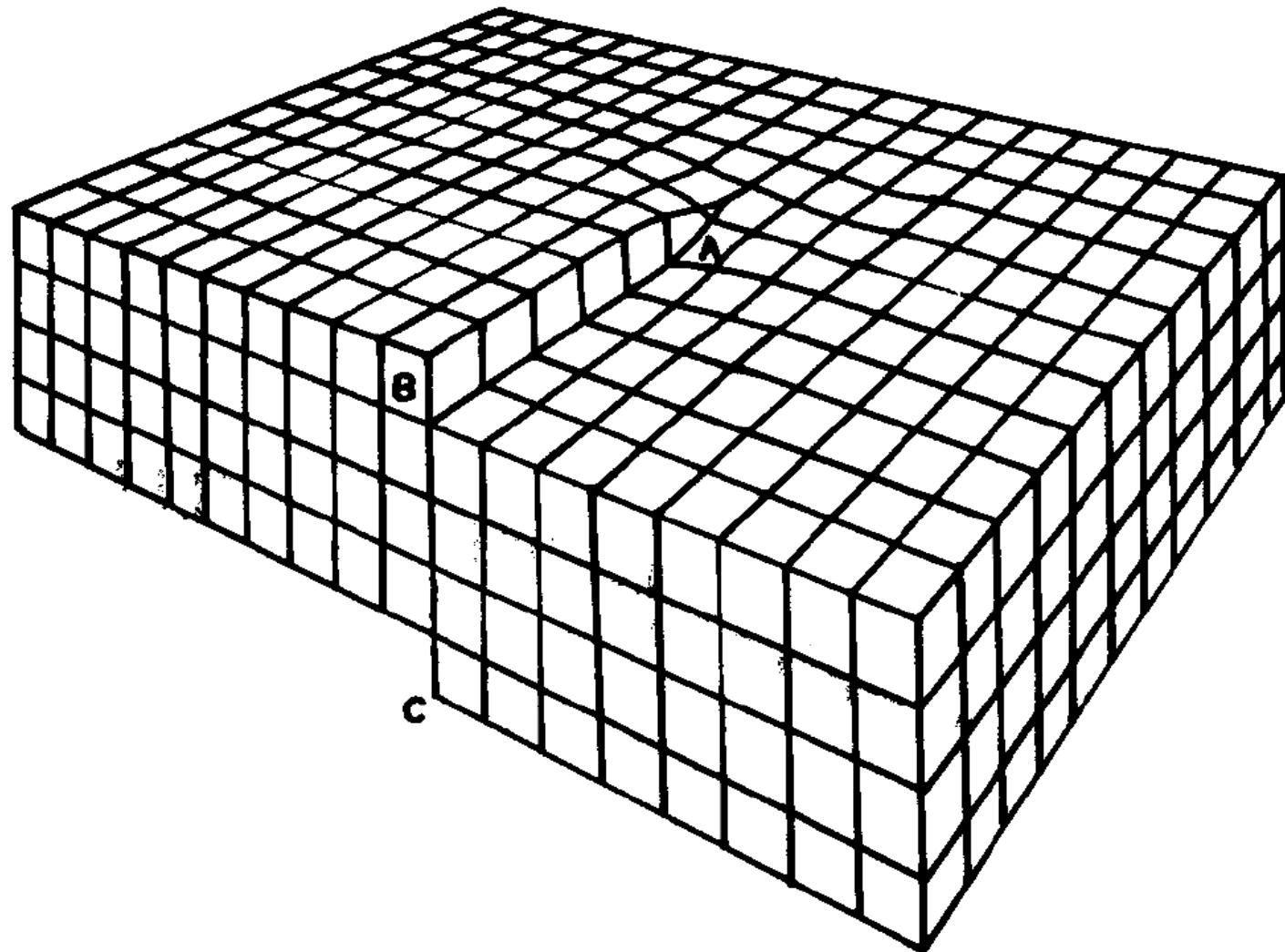
$\alpha, \beta$ : volume and area shape factors

$\rho$ : crystal density

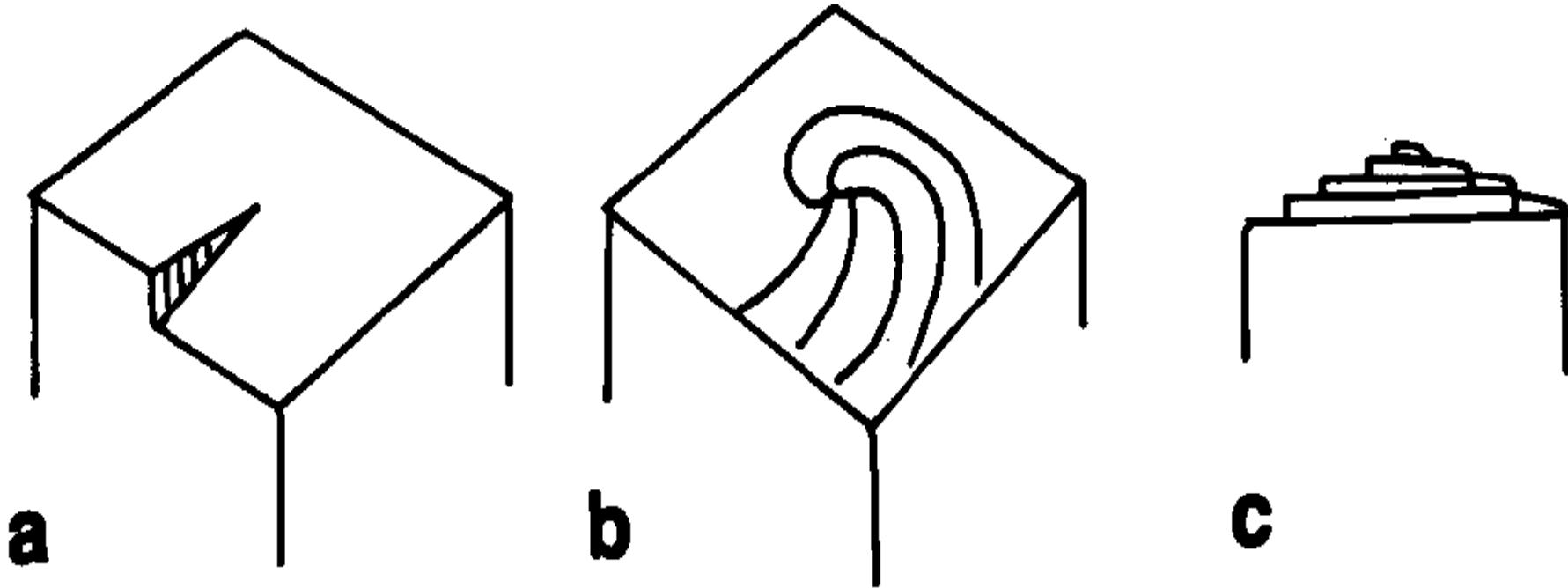
$\delta$ : boundary layer thickness

$c, c_i$ : bulk and interfacial concentration

A screw dislocation in a simple cubic crystal.  
(Strickland-Constable 1968)



Development of a growth spiral from a screw dislocation  
(Mullin 1972)



## Definition of growth rates

$$R_G = K_G \Delta c^n = \frac{1}{A} \frac{dm}{dt} = \frac{3\alpha}{\beta} \mathcal{S} G$$

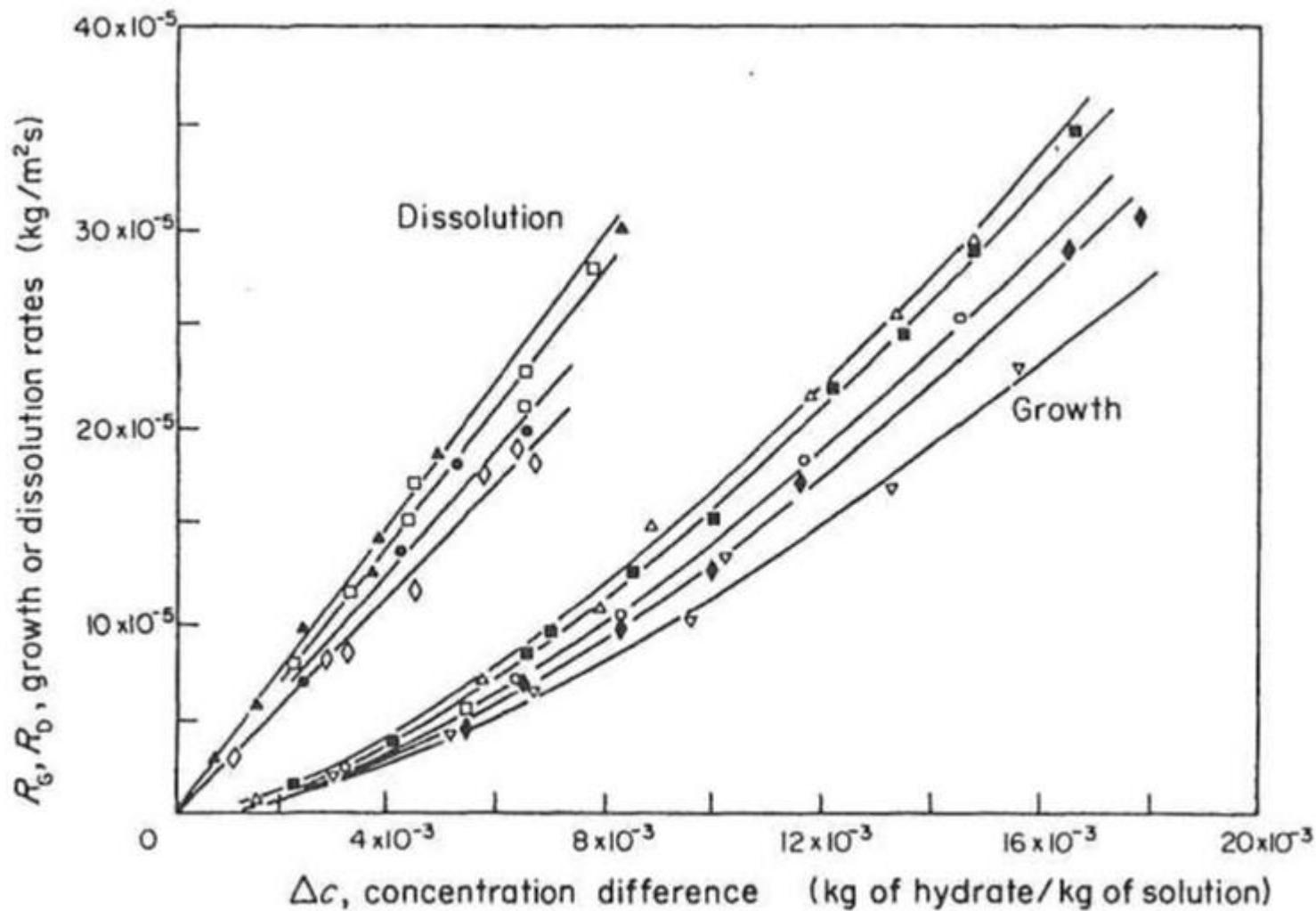
[ kg/m<sup>2</sup> s ] (mass growth rate)

with  $G = \frac{dL}{dt}$  [ m/s ] (linear growth rate)

with  $m = \propto \mathcal{S} L^3$  (mass)

with  $A = \beta L^2$  (area)

$$R_G = a L^{-m} \Delta c^n (modeled growth rate)$$



## A container of human interferon crystals



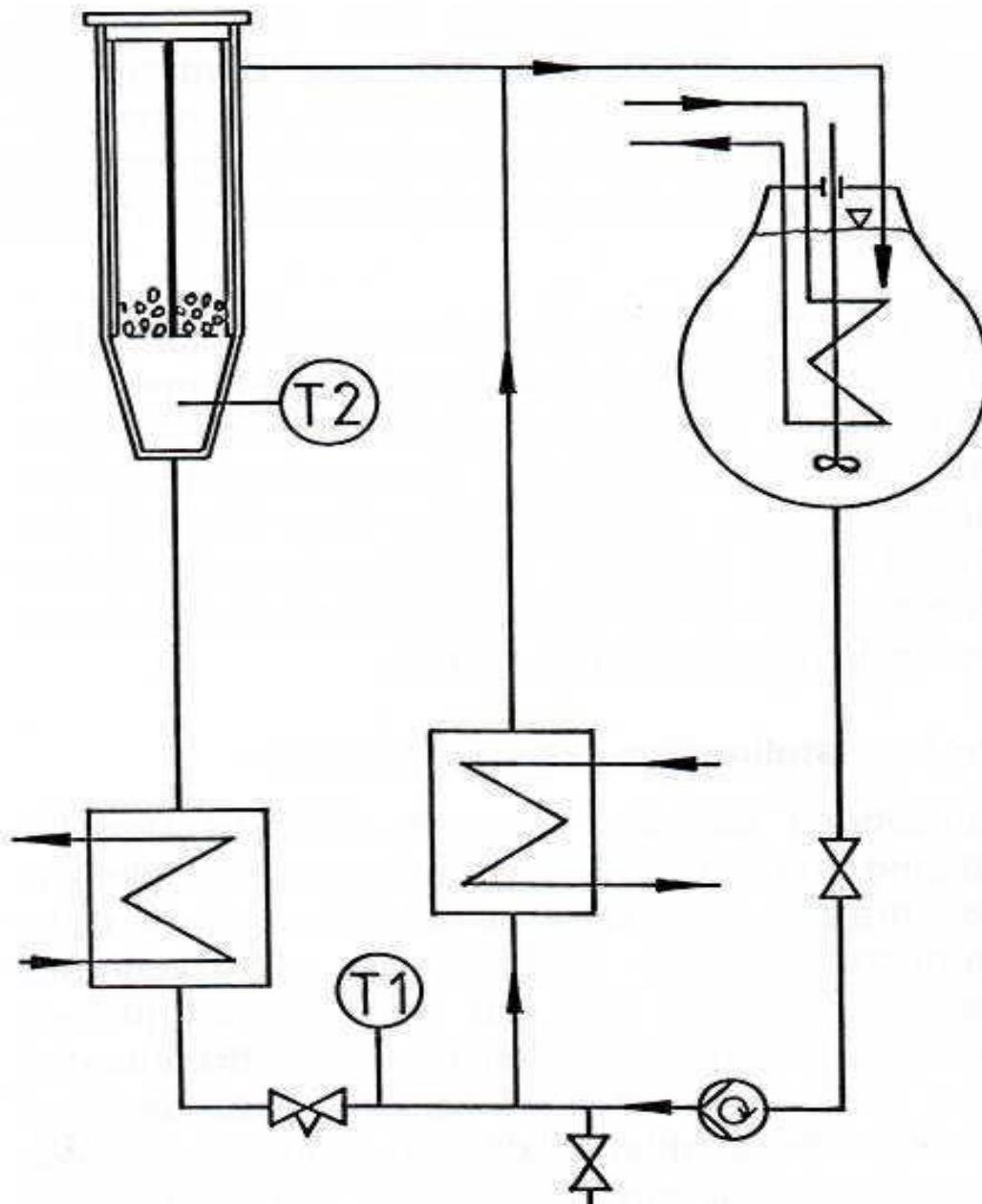
Photomicrograph of human interferon, magnification x 160



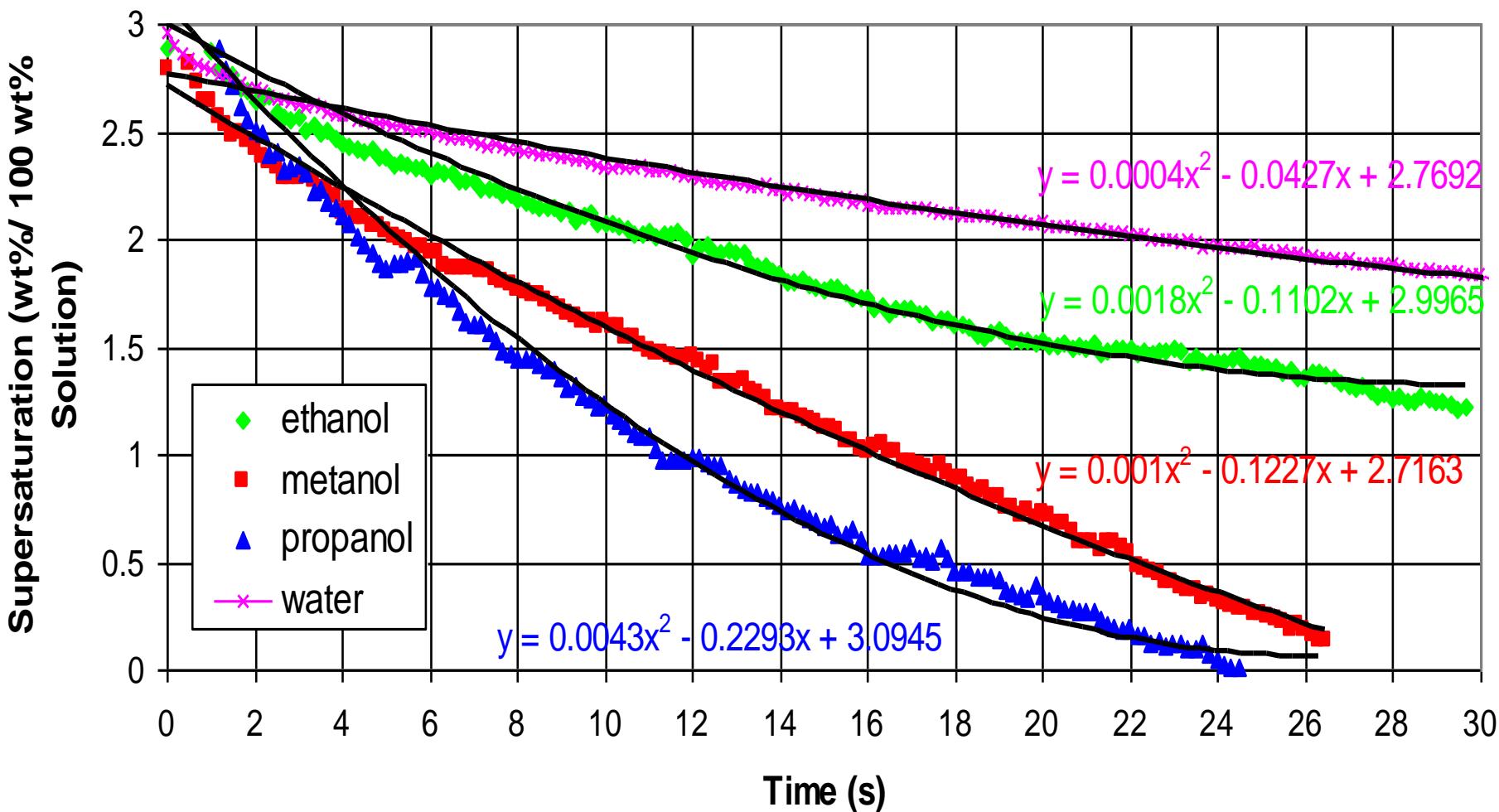
# Influence on the crystal growth rate

- supersaturation
- temperature level
- fluiddynamic constitutions
- (crystal size)
- crystal surface quality
- history of crystals (growth time)
- impurities, additives

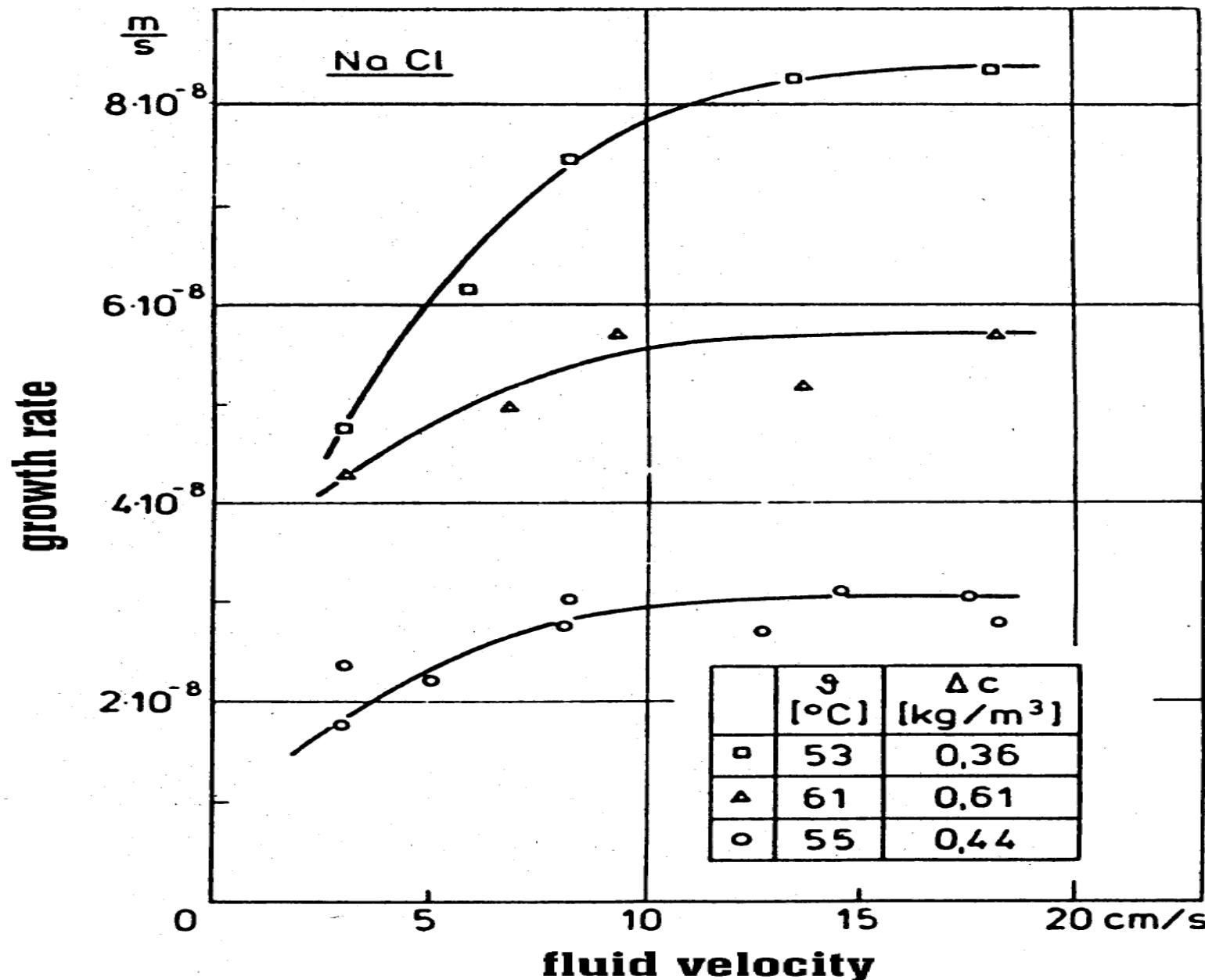
# Fluidized bed crystallizer



# Growth rates of NaCl crystals in a the fluidized

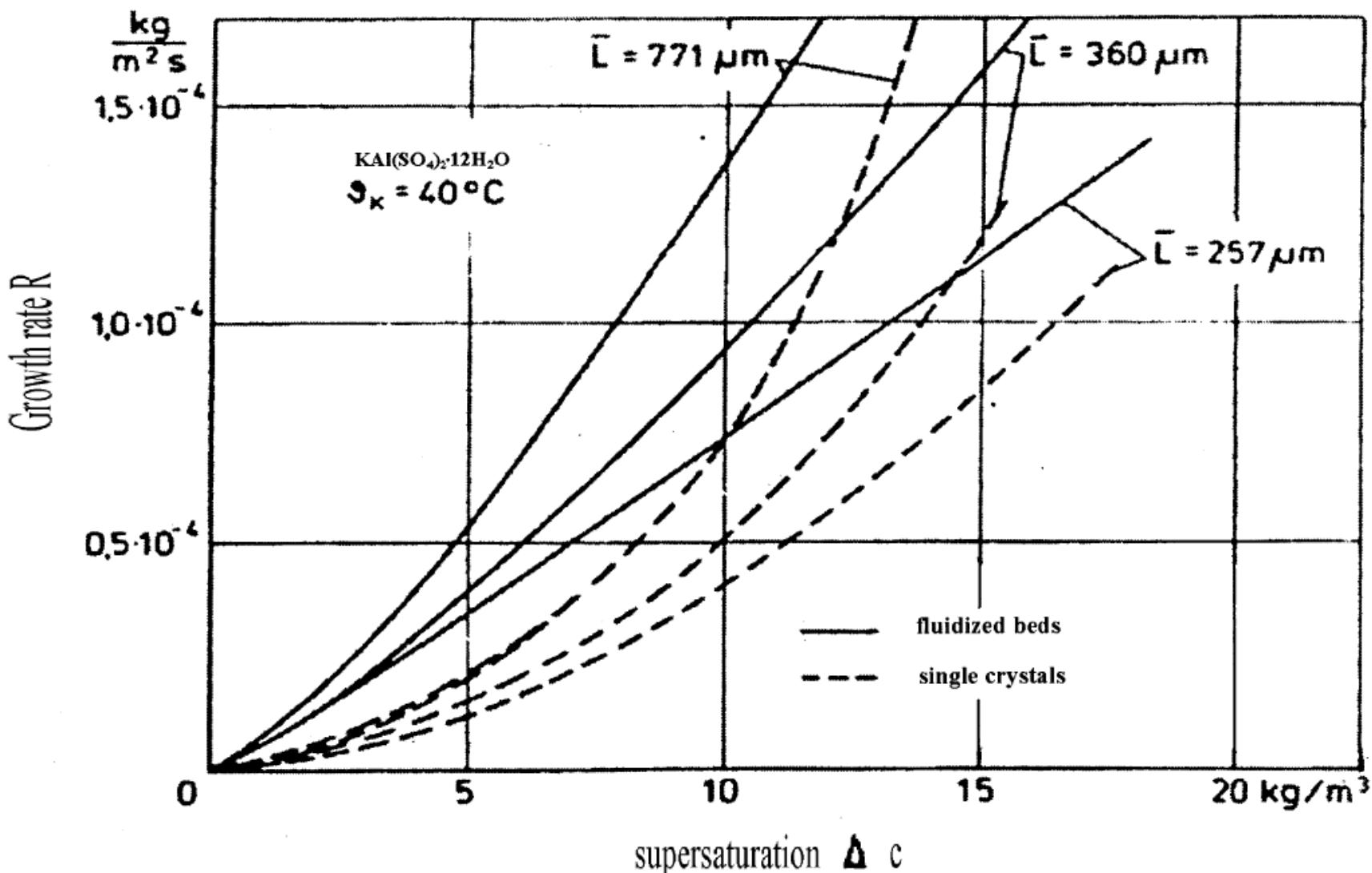


# Influence of fluid velocity on locally fixed NaCl crystals

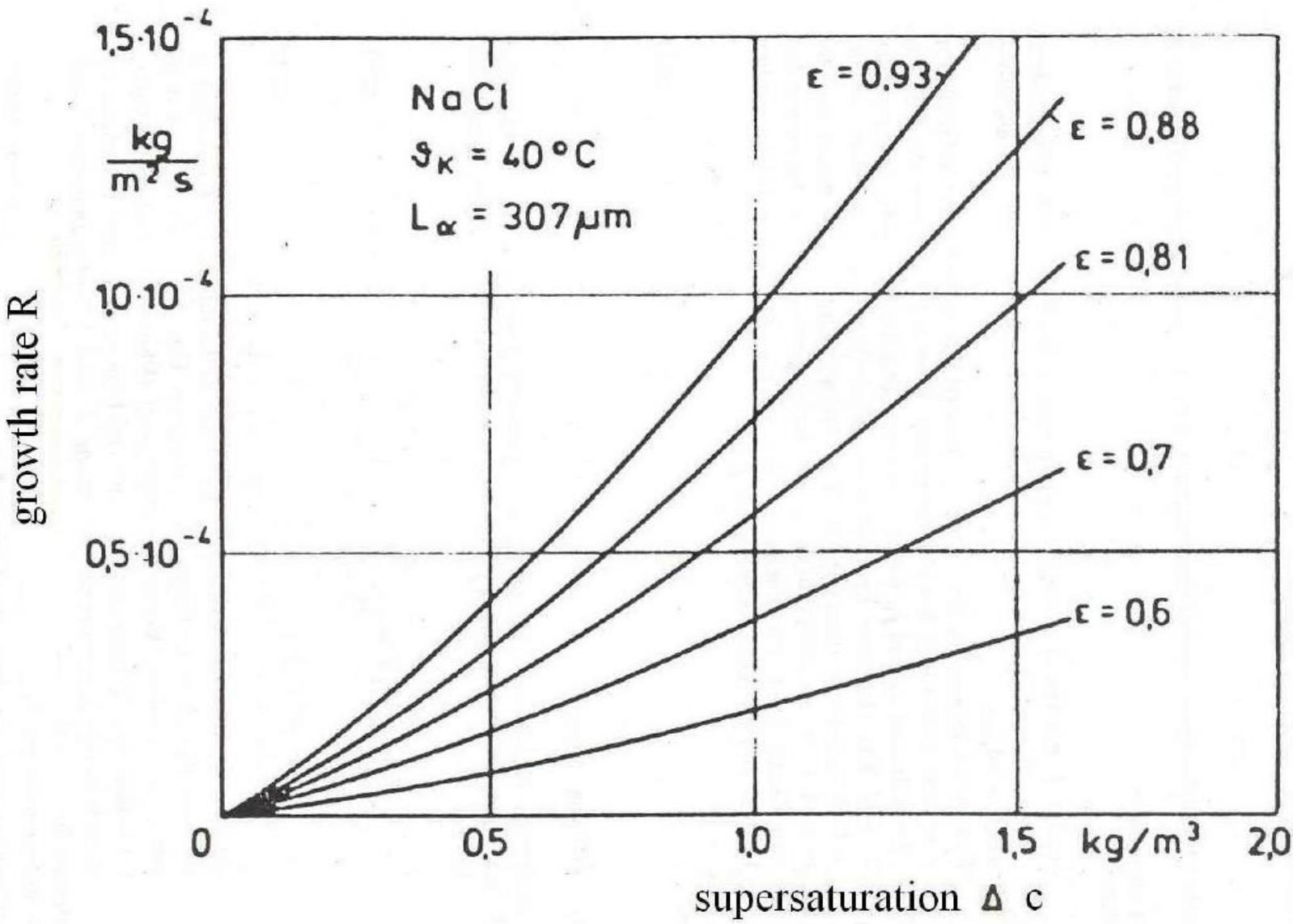


# Growth rates: Comparison of single free suspended crystals and crystals grown in an fluidized bed

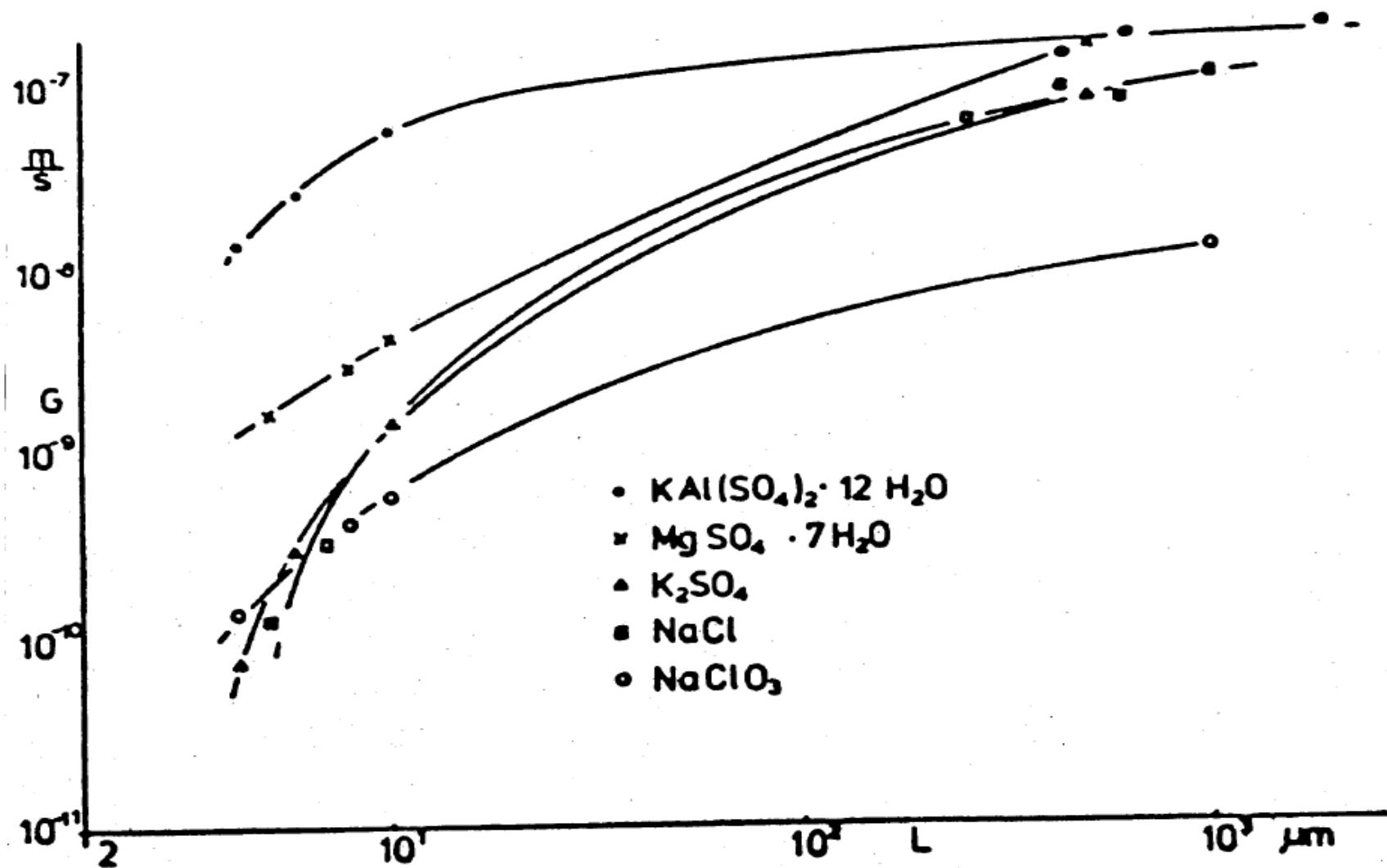
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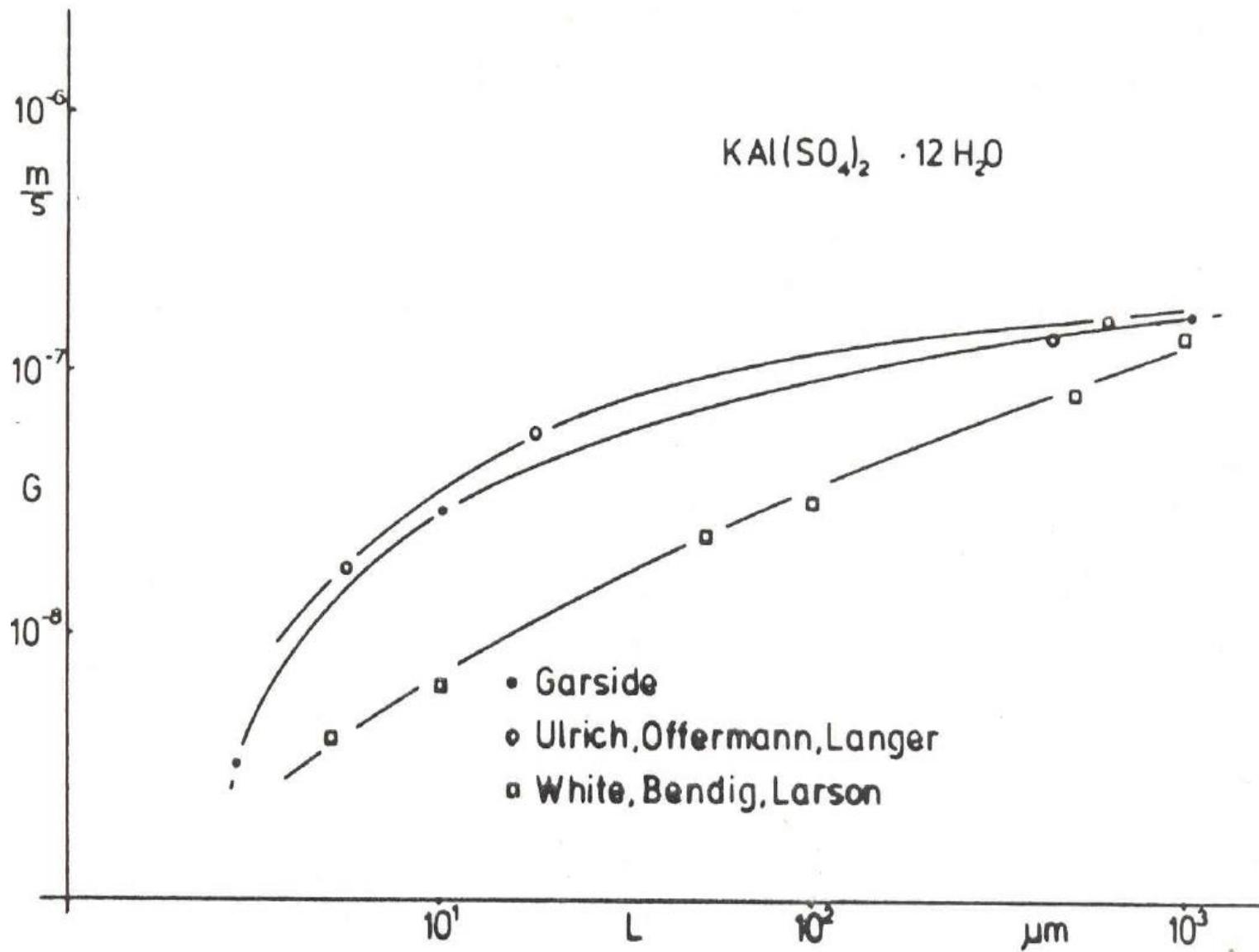
Growth rate of NaCl crystals in a fluidized bed, here: Influence of suspension density  $\epsilon$



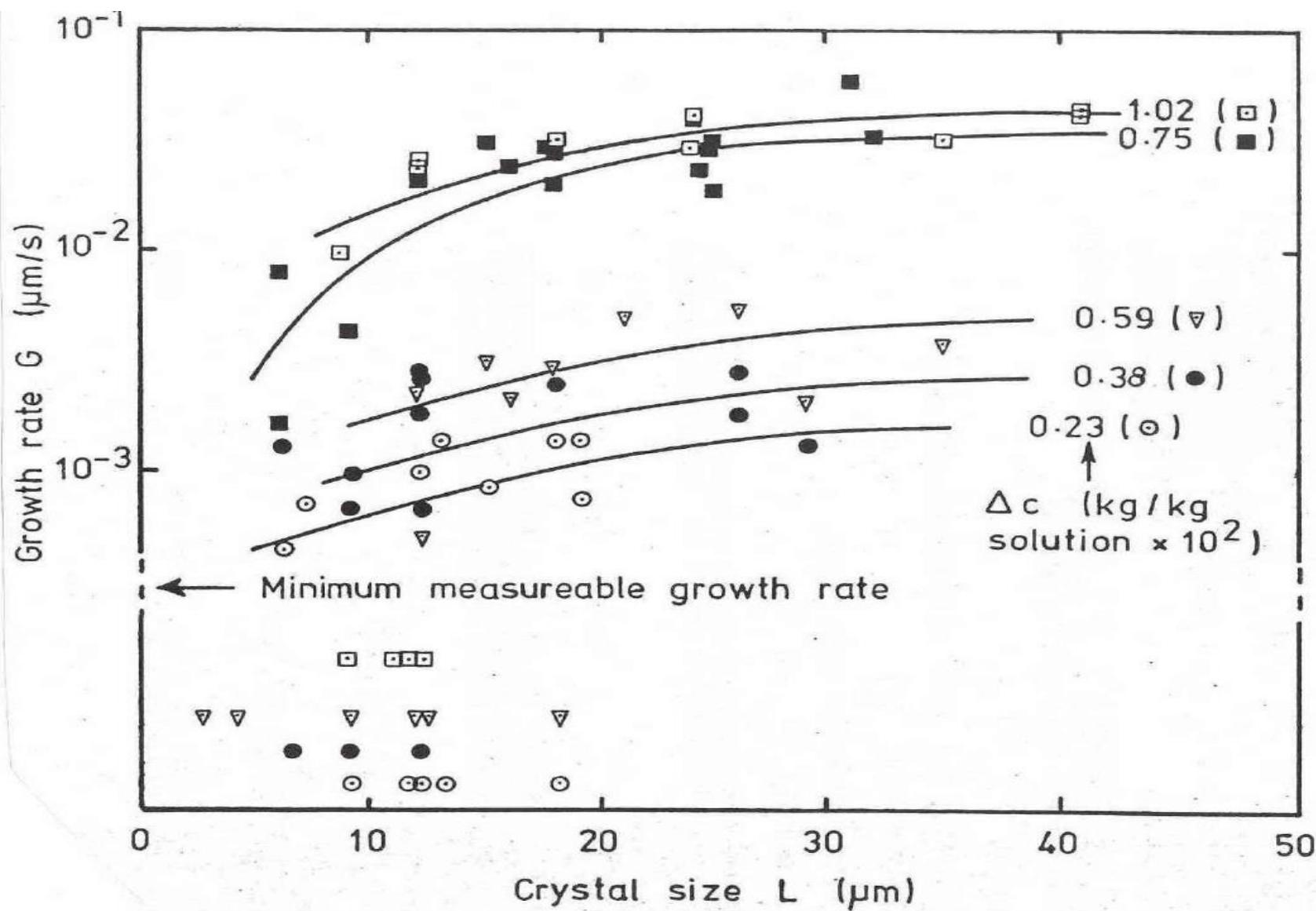
# Growth rates of small and product size crystals



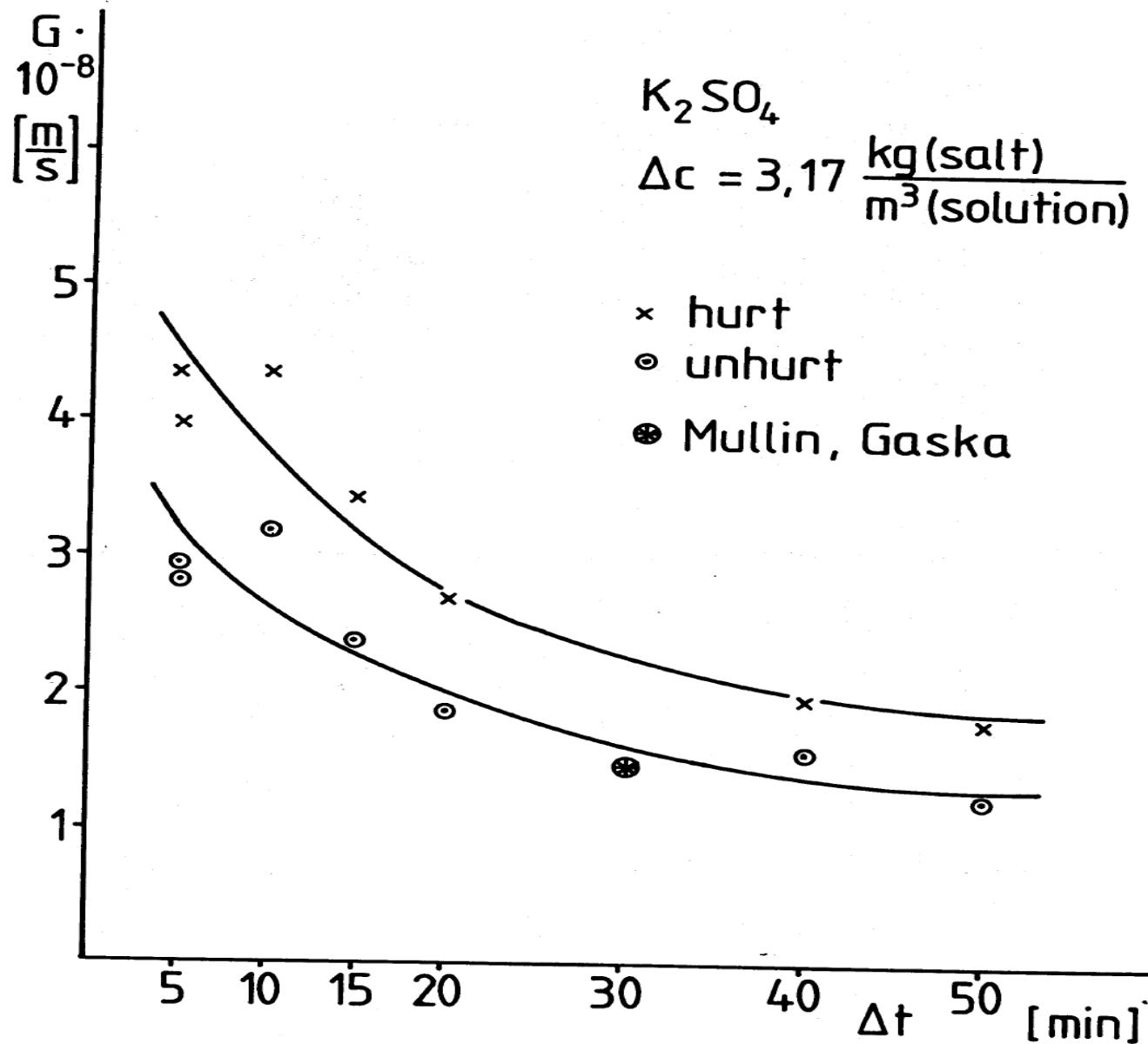
# KAl(SO<sub>4</sub>)<sub>2</sub> · 12H<sub>2</sub>O growth rates



# Growth rates $\text{KAl}(\text{SO}_4)_2 \cdot 12\text{H}_2\text{O}$ (Garside 1978)

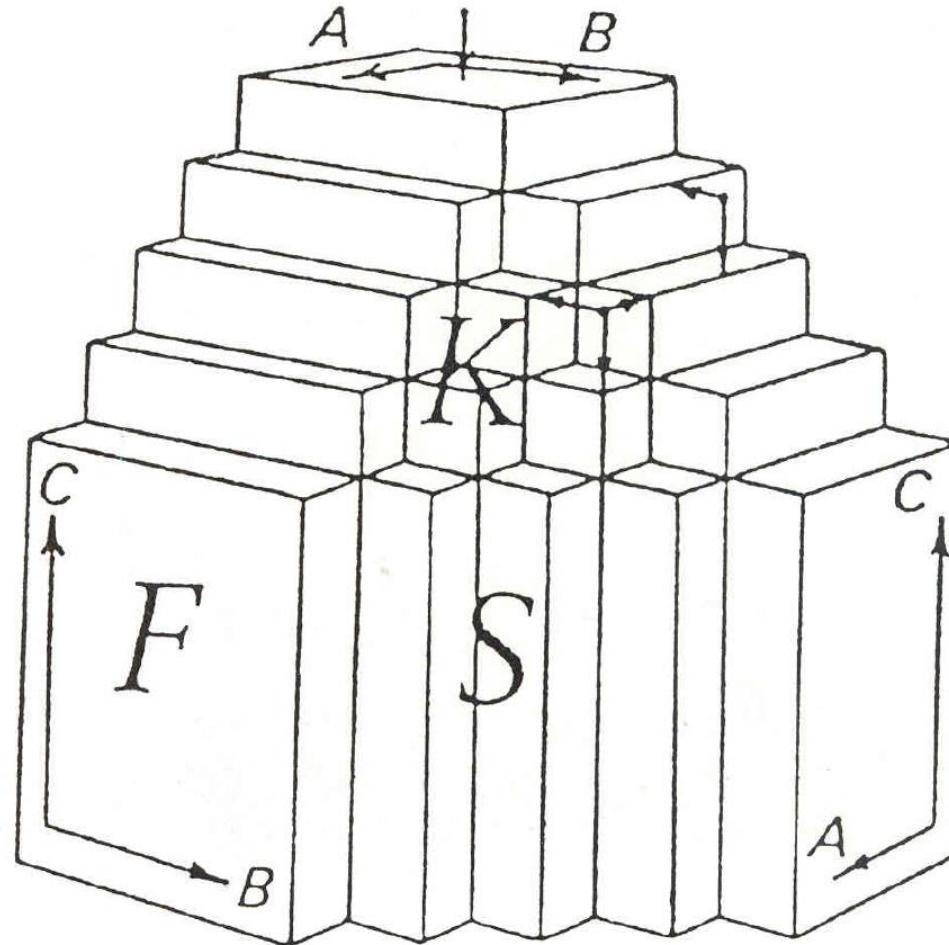


Different growth rates of crystals with different surface qualities in respect with time

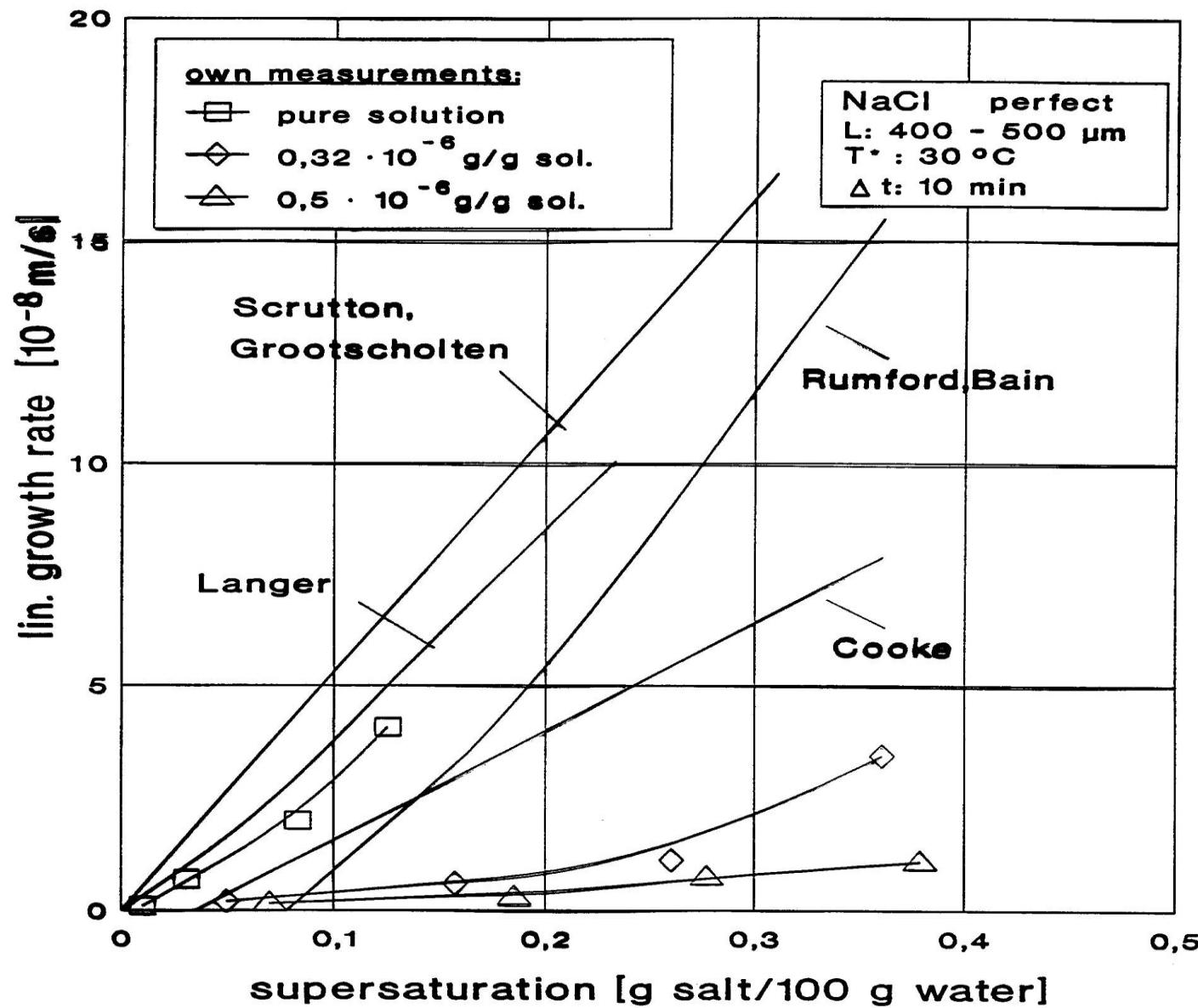


Hypothetical crystal with three PBC's: A // [100], B // [010]  
and C // [001]. Flat faces are: (100), (010) and (001).  
Stepped faces are: (110), (101) and (011). Kinked face is (111).

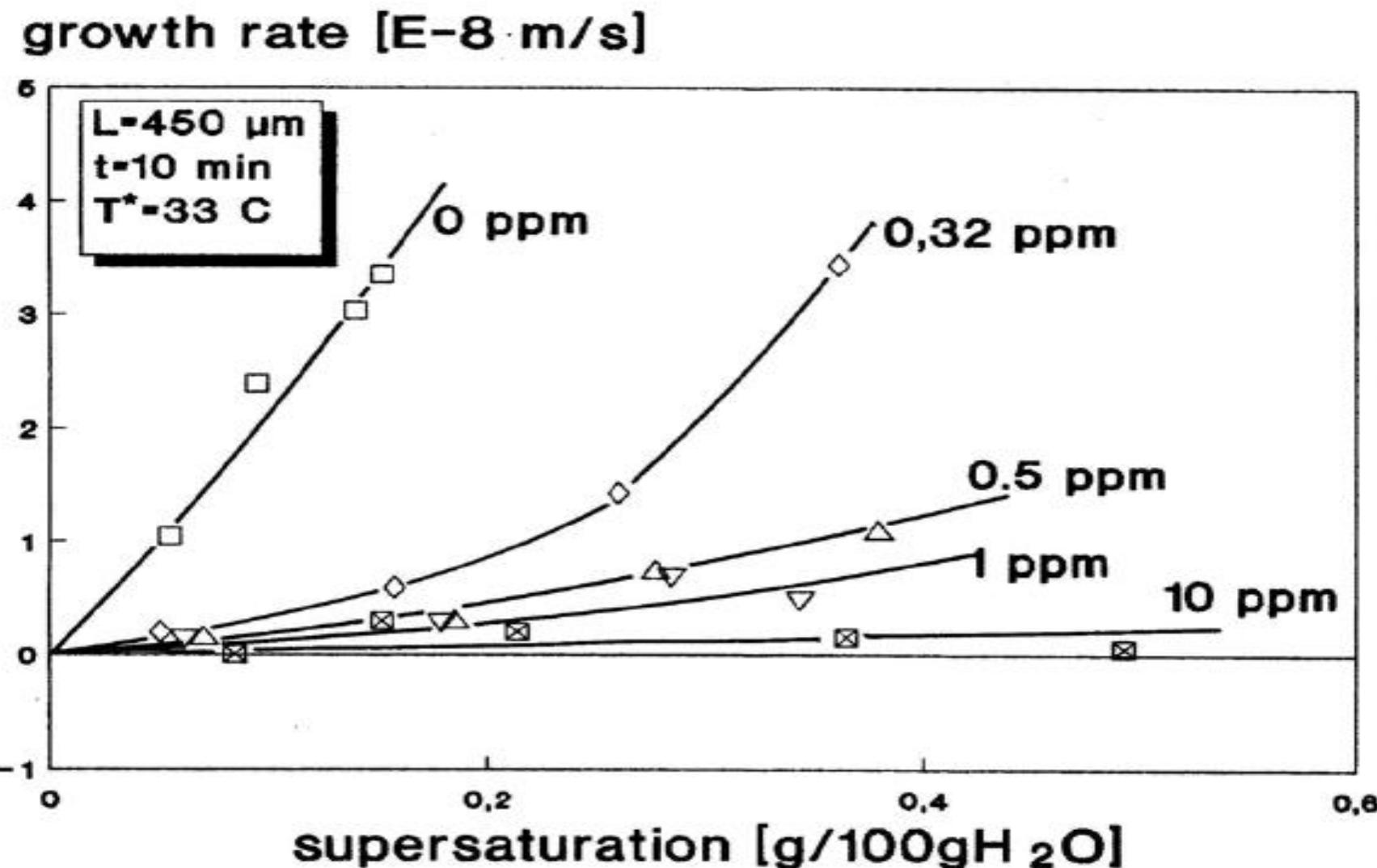
*P. Hartman, Structure and morphology*



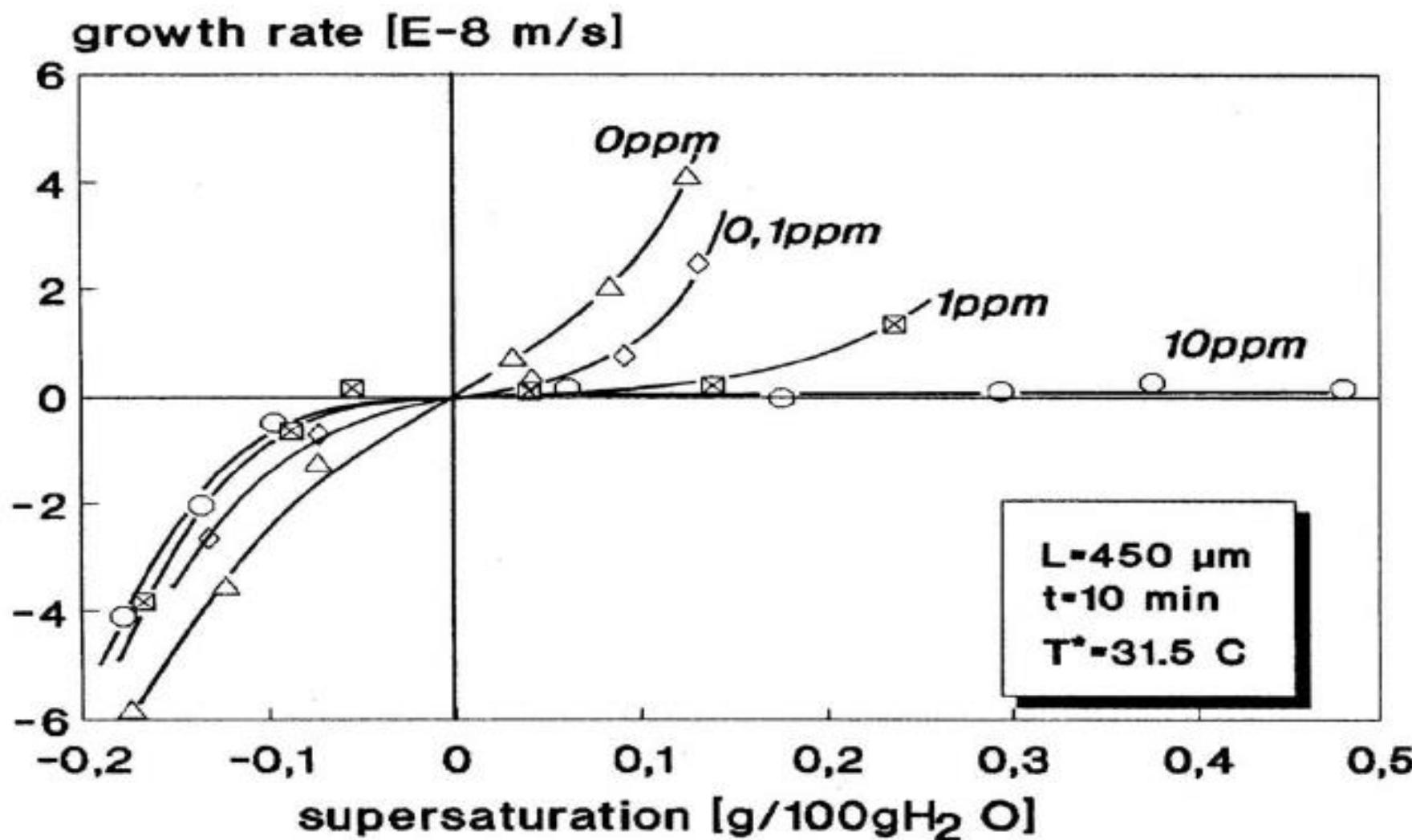
# Growth rates of NaCl crystals according to literature

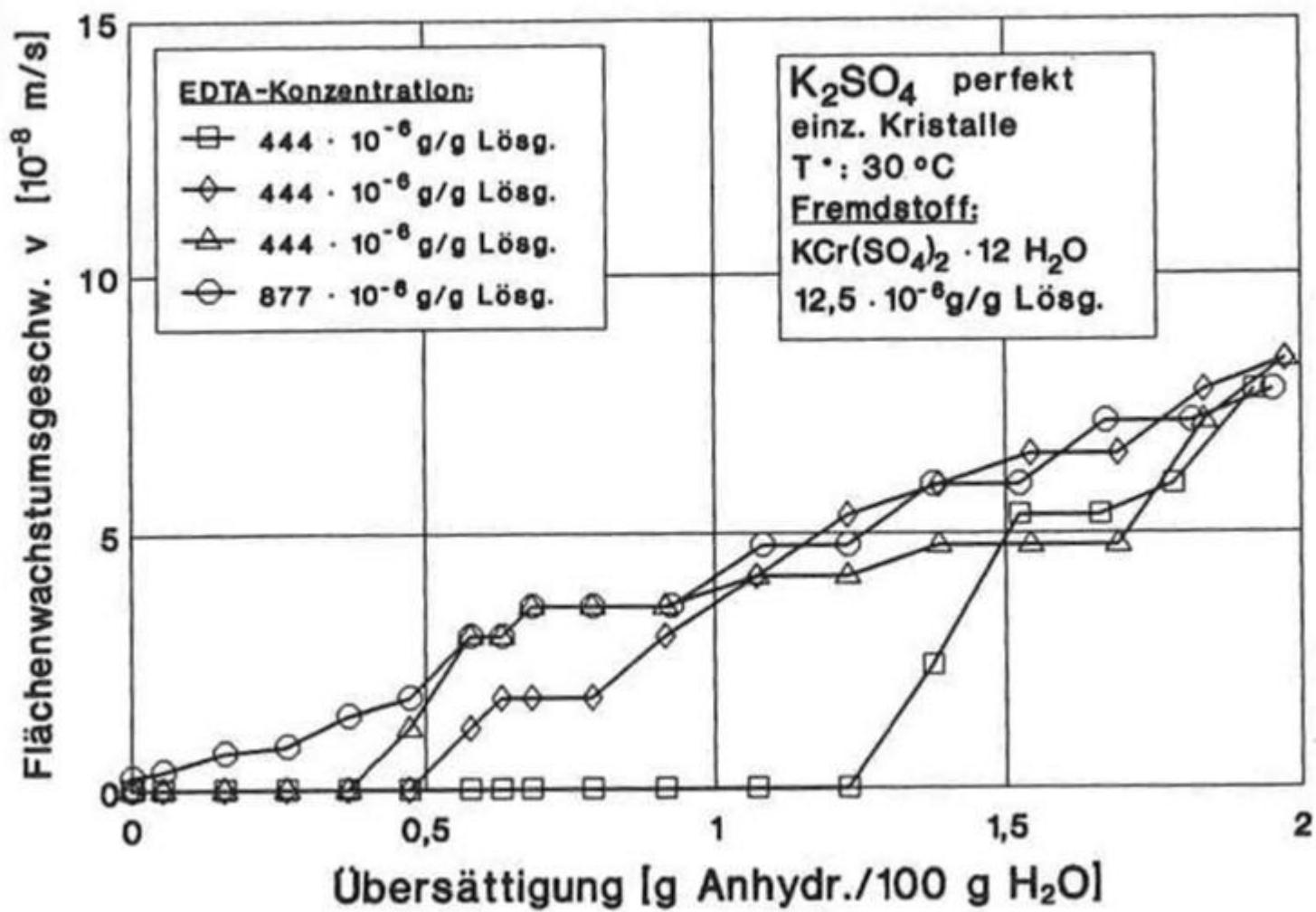


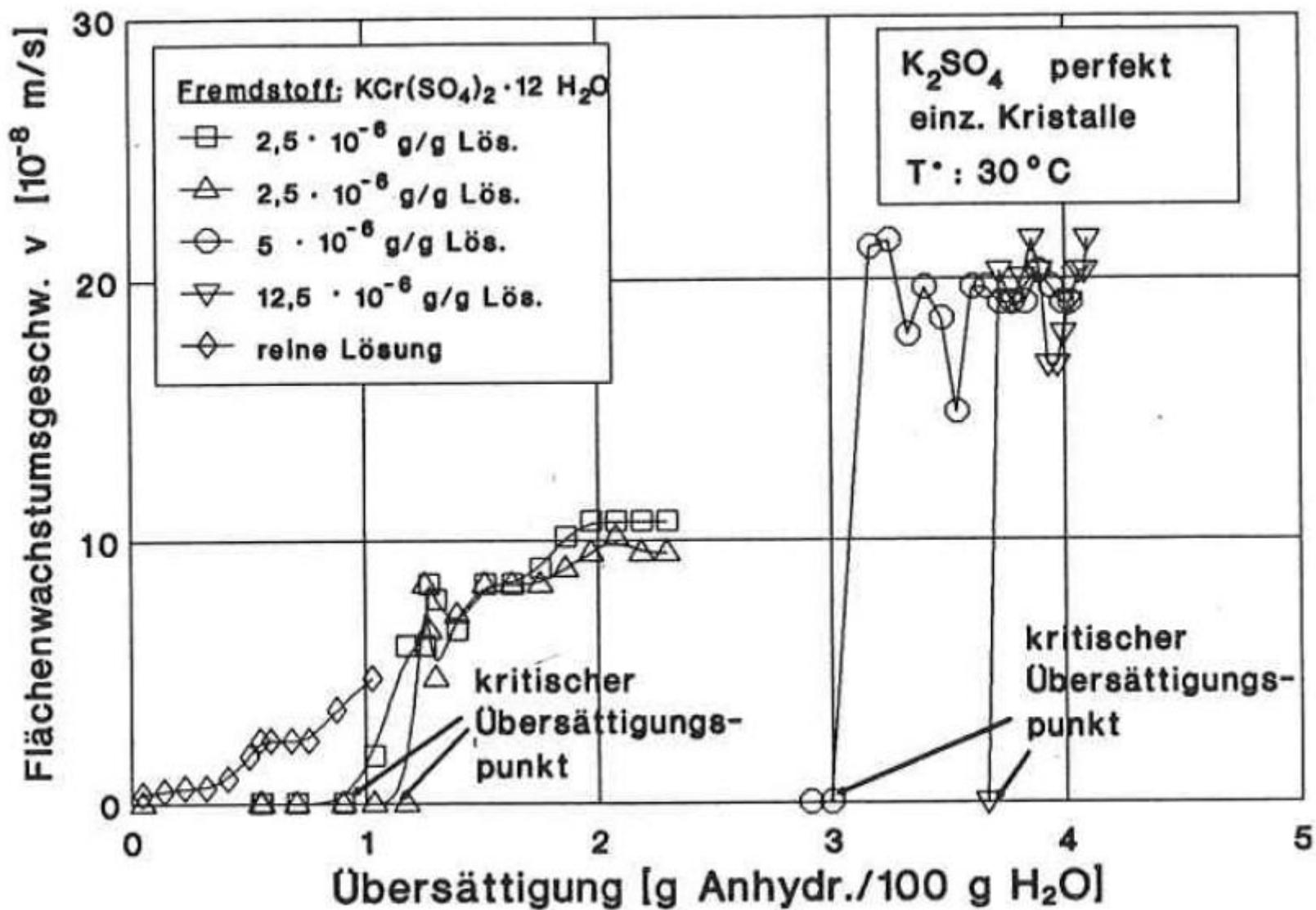
# Growth rates of NaCl crystals in the presence of $\text{PbCl}_2$



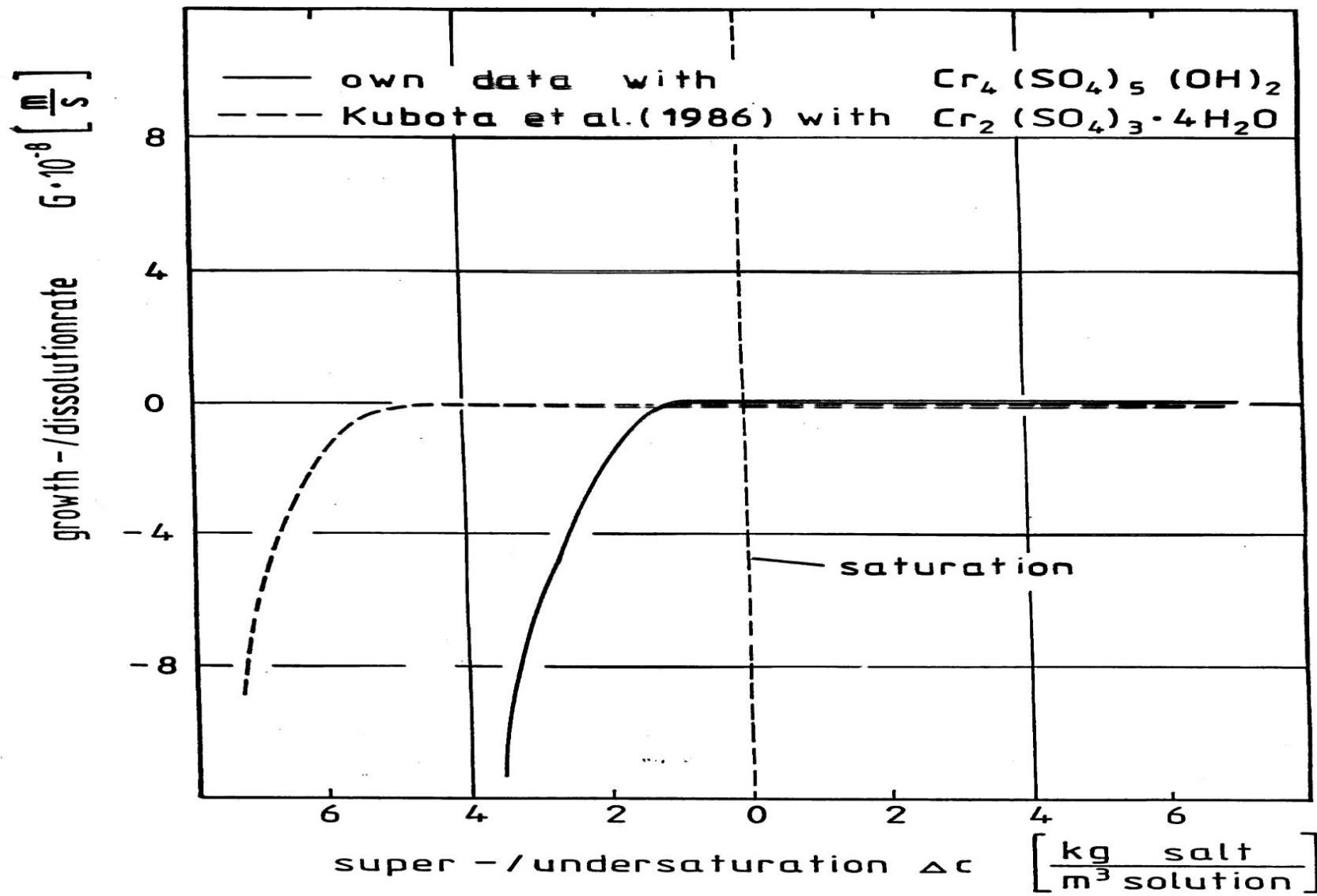
# Growth rates of NaCl crystals in the presence of $K_3Fe(CN)_6$



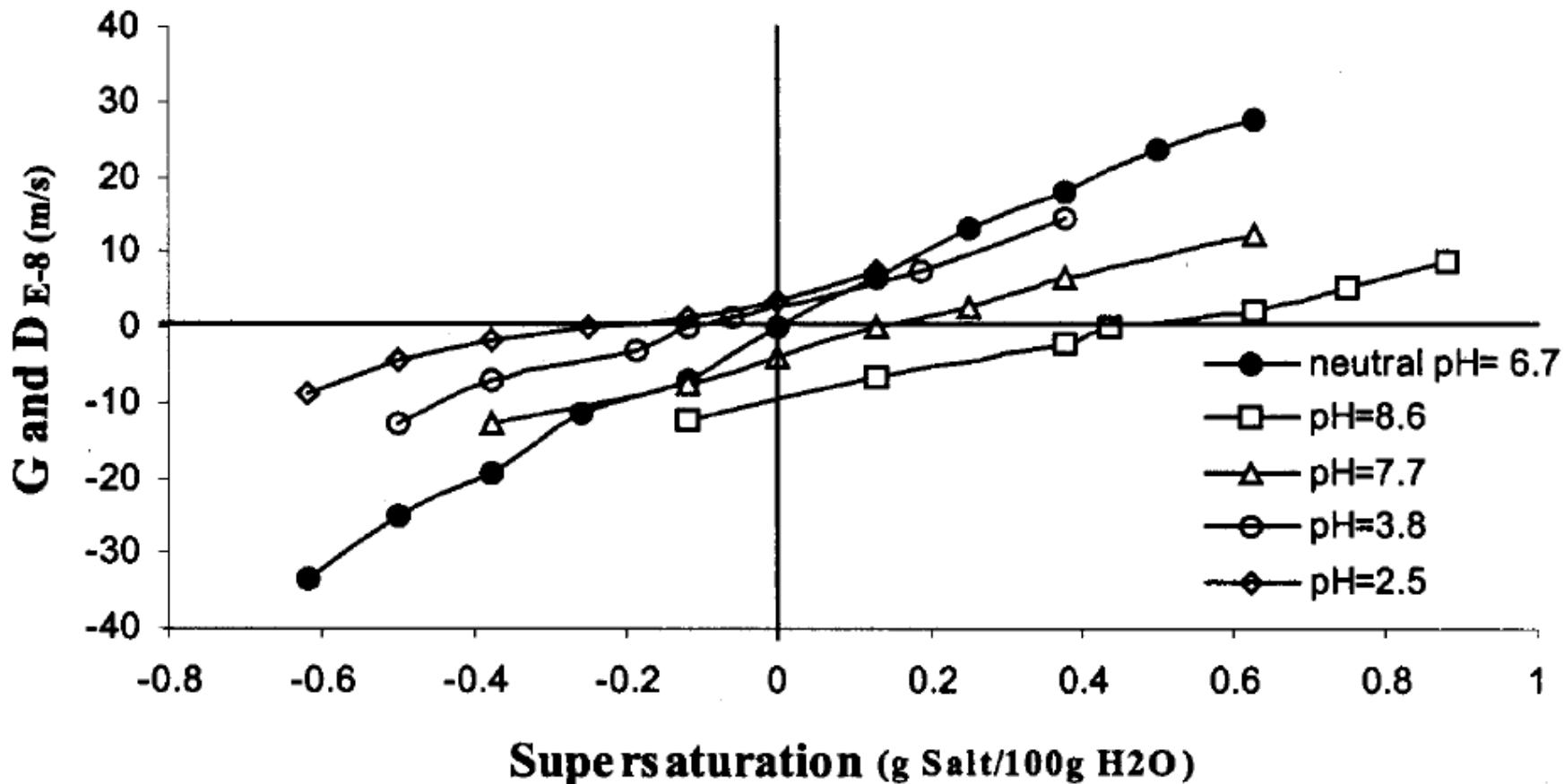




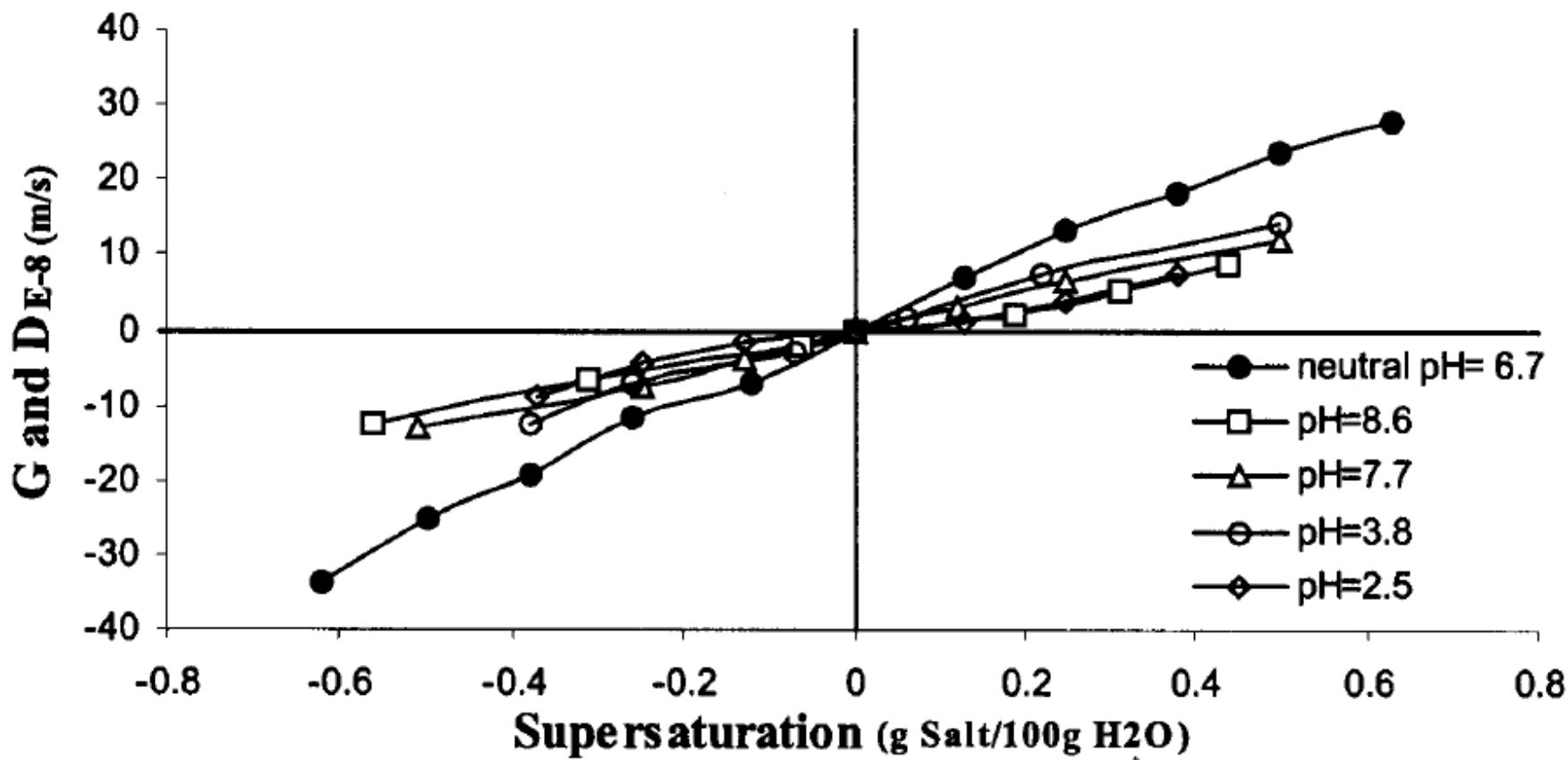
# Suppressed dissolution rates of $K_2SO_4$ by additives



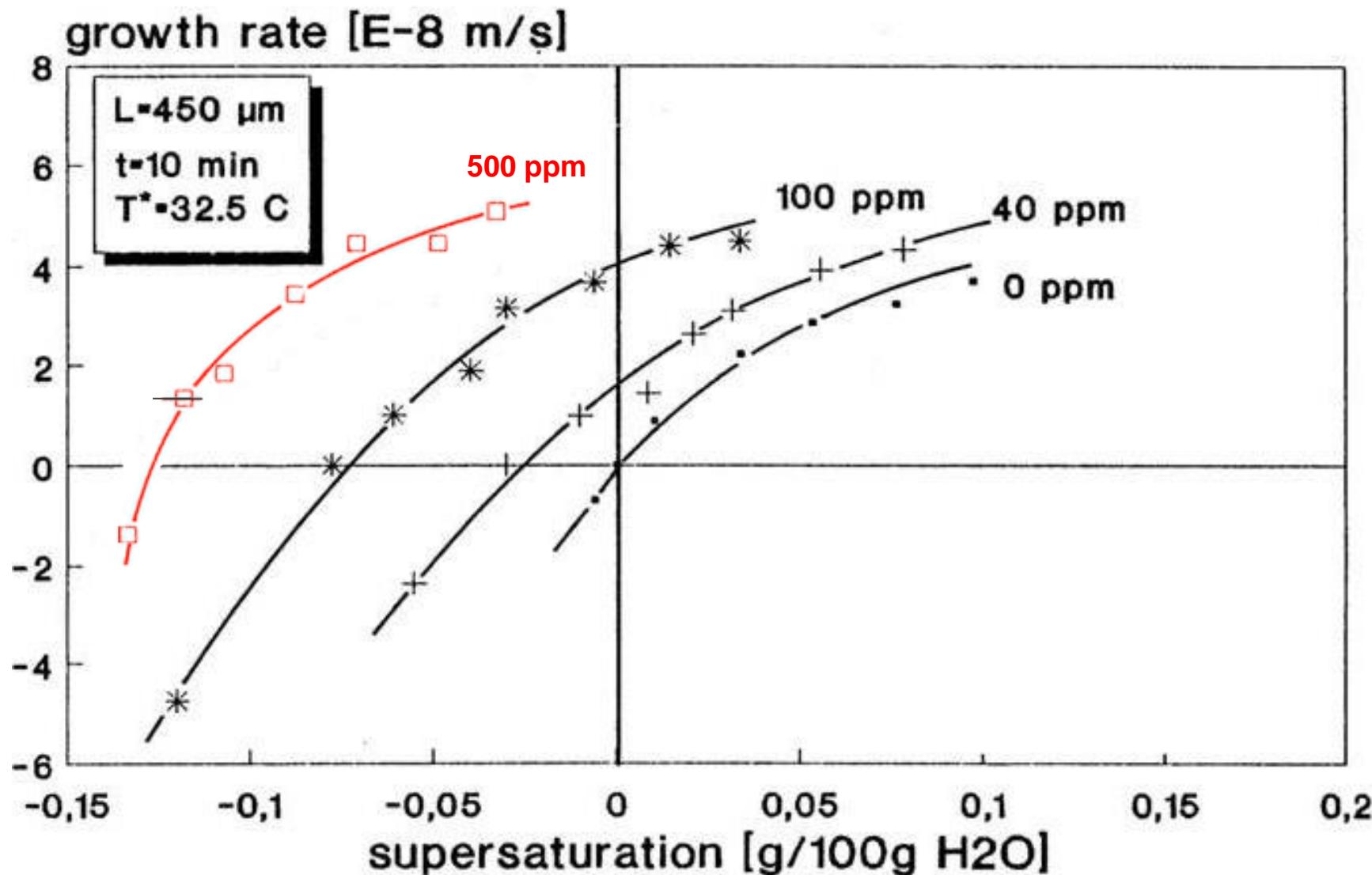
The effect of pH on the growth and dissolution rates of  
 $\text{MgSO}_4 \cdot 7\text{H}_2\text{O}$  with saturation point correction  
(kinetic effect)

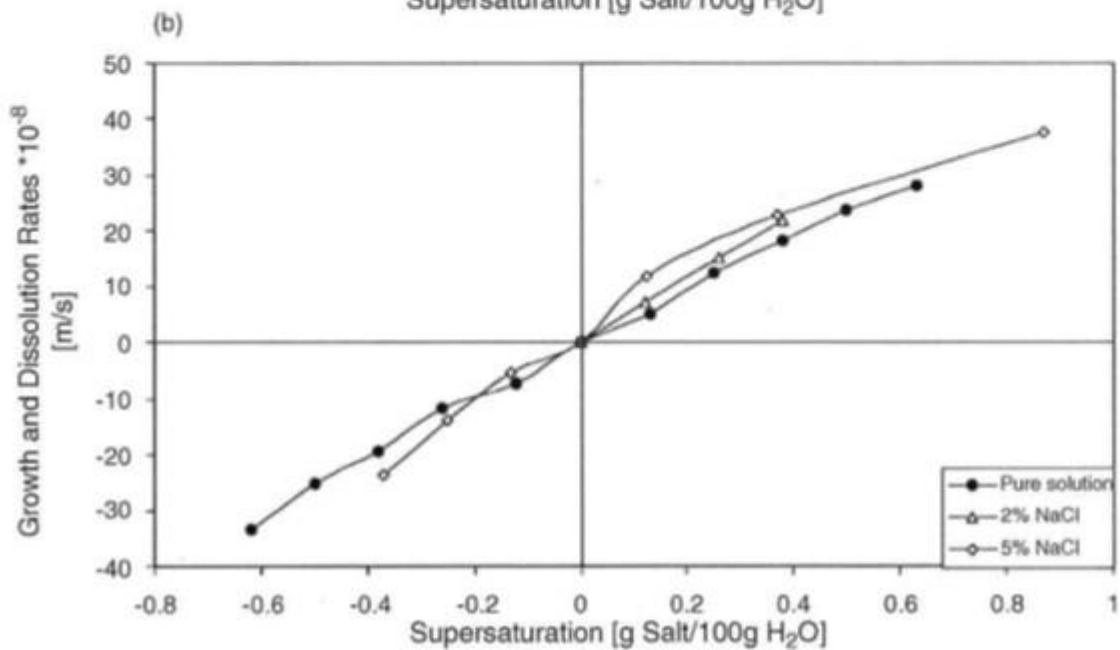
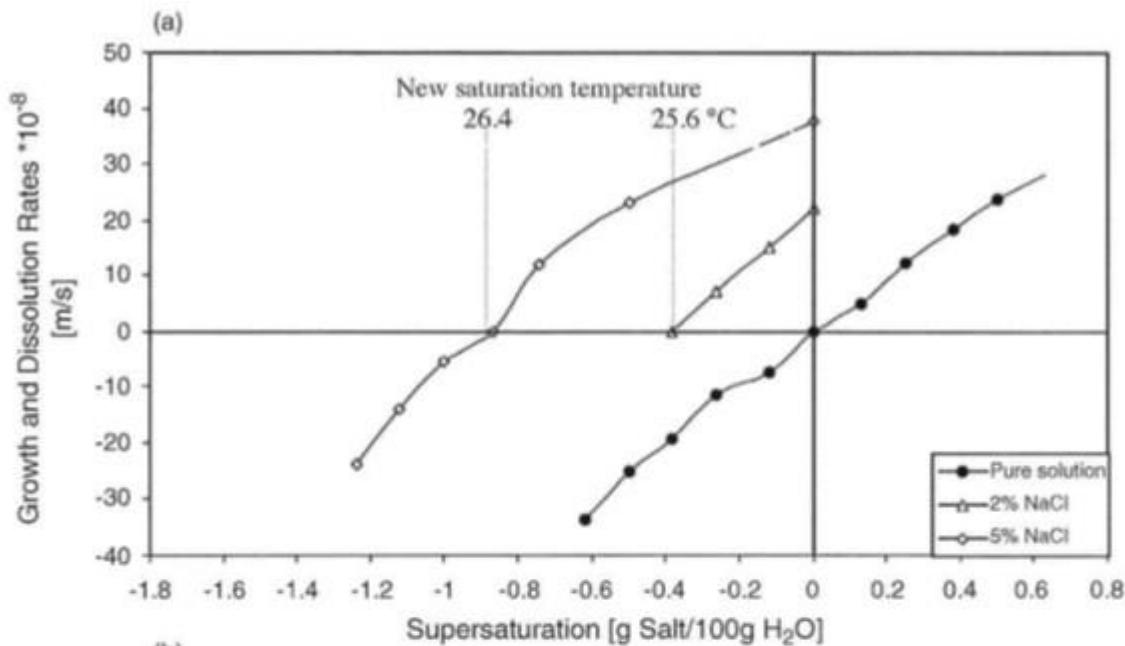


The effect of pH on the growth and dissolution rates  
of  $\text{MgSO}_4 \cdot 7\text{H}_2\text{O}$  with saturation point correction  
(kinetic effect)

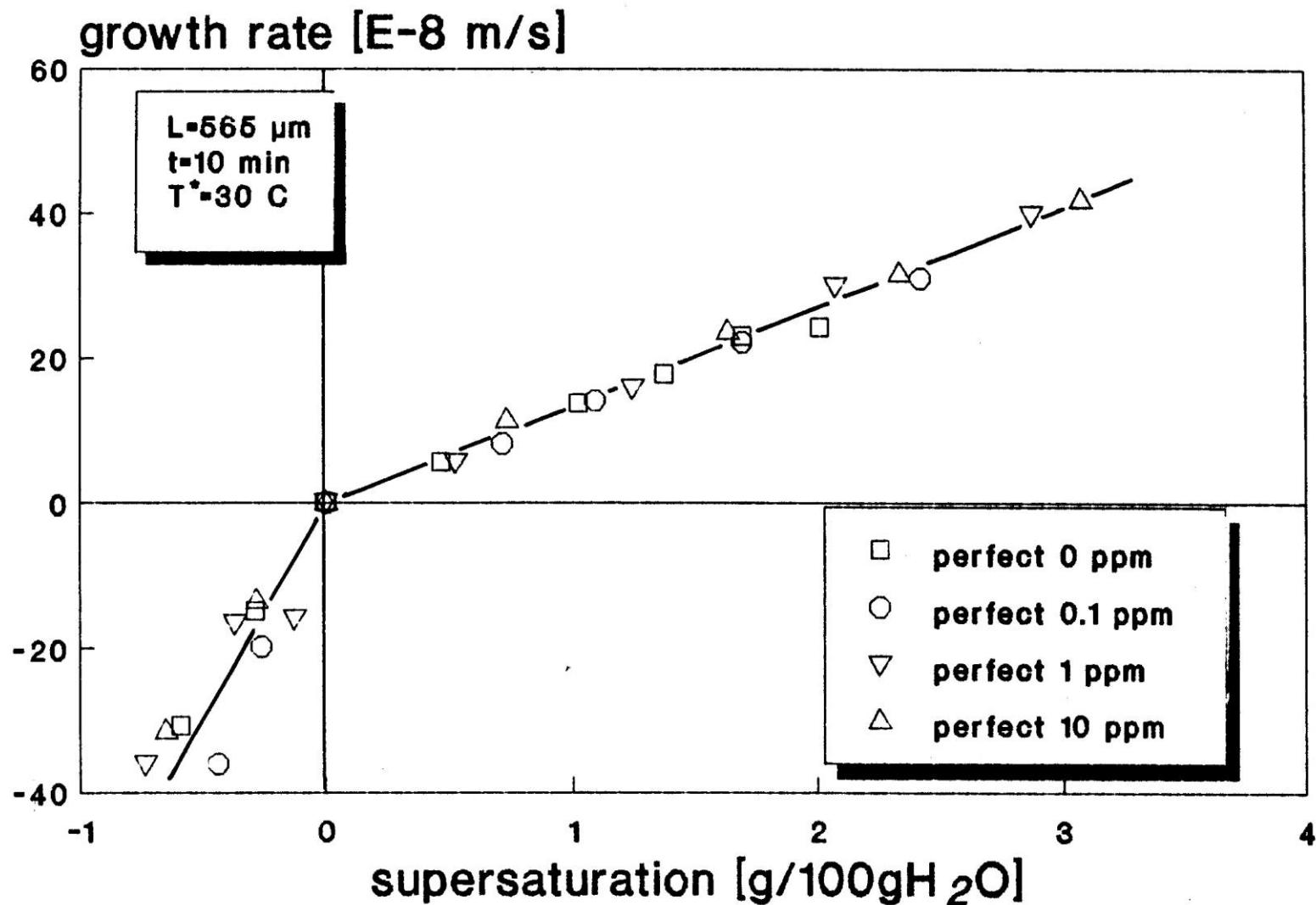


# “Apparantly accelerated growth” of NaCl by the additive $\text{MgCl}_2 \cdot 6 \text{ H}_2\text{O}$





# Growth and dissolution rates of $\text{KAl}(\text{SO}_4)_2 \cdot 12\text{H}_2\text{O}$ in presence of $\text{PbCl}_2$



# Effect of Supercooling on Nucleation and Growth Rate

---

Nucleation rate

$$J = k_n \Delta c_{\max}^n$$

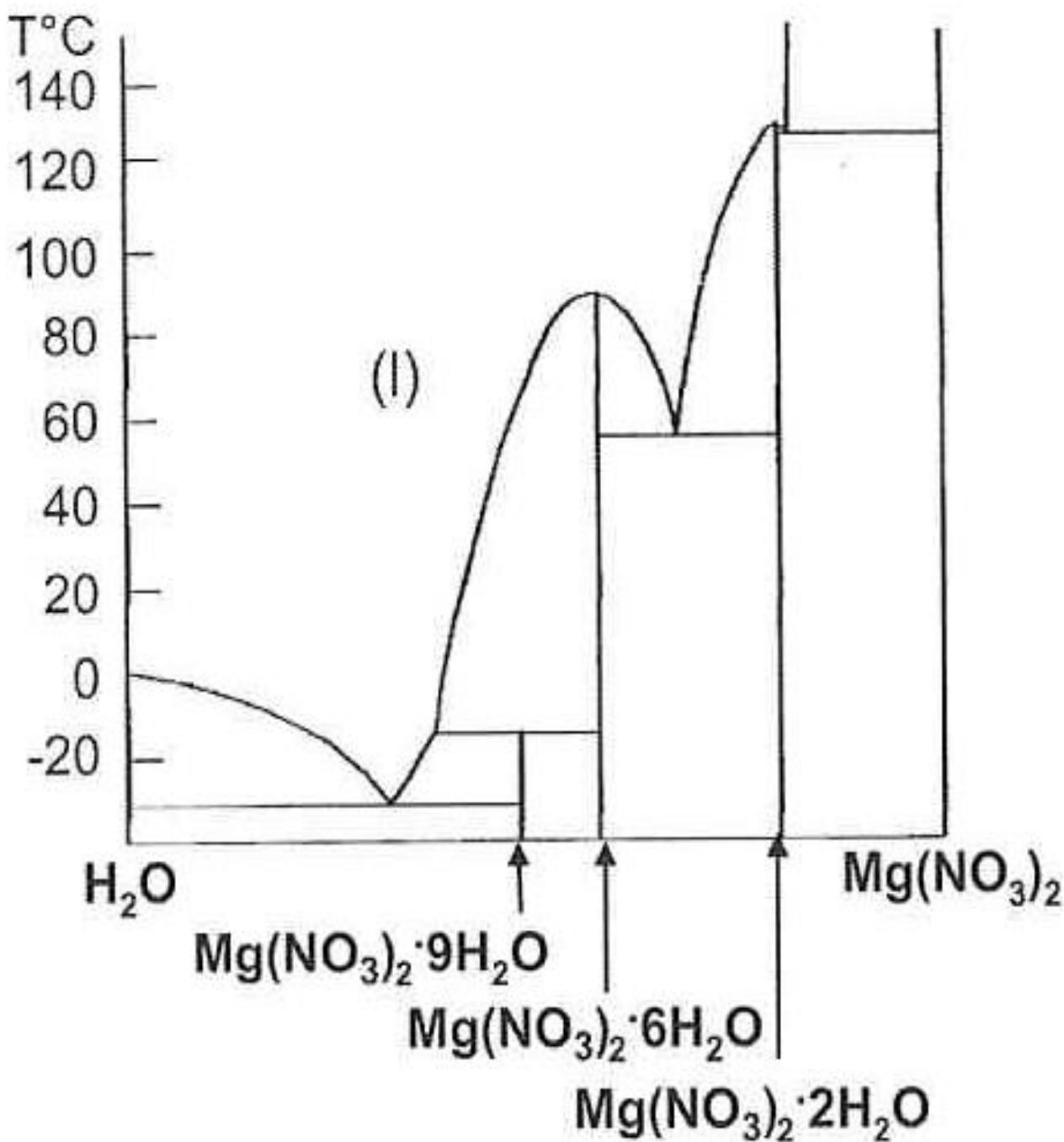
Growth rate

$$G = k_g \Delta c^g$$

with  $\Delta c_{\max} = \left( \frac{dc^*}{dt} \right) \Delta T_{\max}$  and  $\Delta c = c - c^*$

Thank you for your  
attention!

- Polymorph
- Solvat (Hydrat)



Thermodynamically stable phases of organic and inorganic substances depend on:

---

- Temperature
  - Pressure
  - surrounding media:
    - air (relative humidity)
    - solvent (solubility)
  - additional: mechanical stress (e.g. grinding)
- **A change of these parameters often leads to metastable modifications**

# Definition of polymorphism and solvation

- If a substance is capable of crystallizing into different, but **chemically identical** crystalline forms, it is said to exhibit: **polymorphism**.
- If the anhydrous/non-solvate part is identical, but the crystalline forms **differ in the amount of water/solvent** in the lattice, the crystalline form is said to exhibit: **solvation**.

**„No rules exist that allow the prediction of whether a compound will exhibit polymorphism...“**

Stephen R. Byrn: „Solid-State Chemistry of Drugs“,  
Academic Press, New York, 1982

# Industrial relevance of polymorphs and solvates

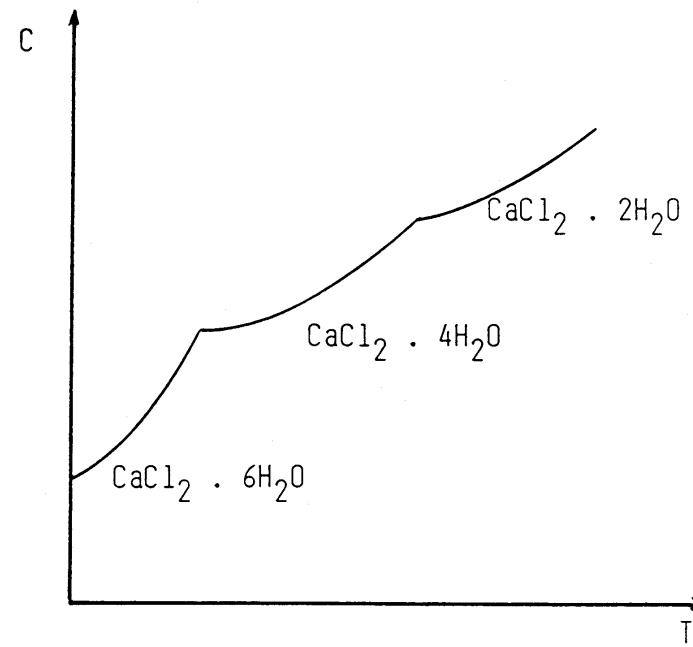
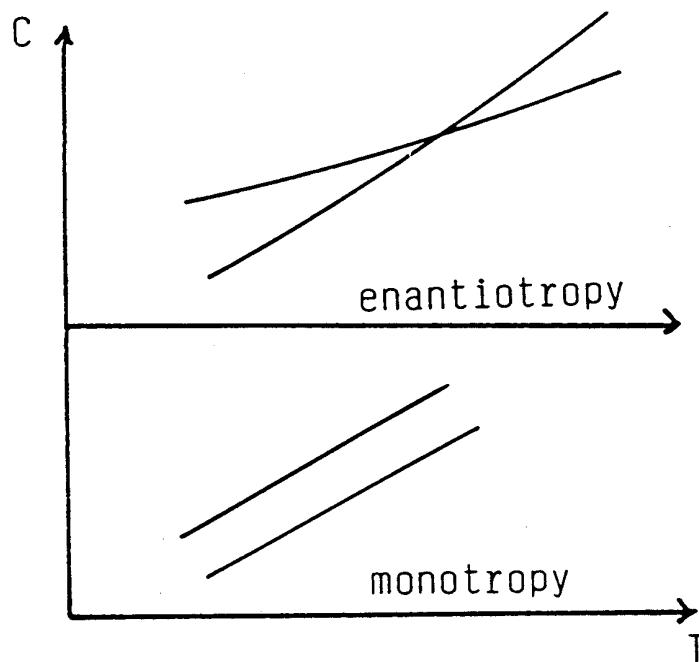
- The change in physical properties such as:
  - bioavailability
  - dissolution behaviour
  - suspension syringeability
  - chemical and physical stability
  - solid-liquid-separation
  - drying
  - packaging
  - tabletting

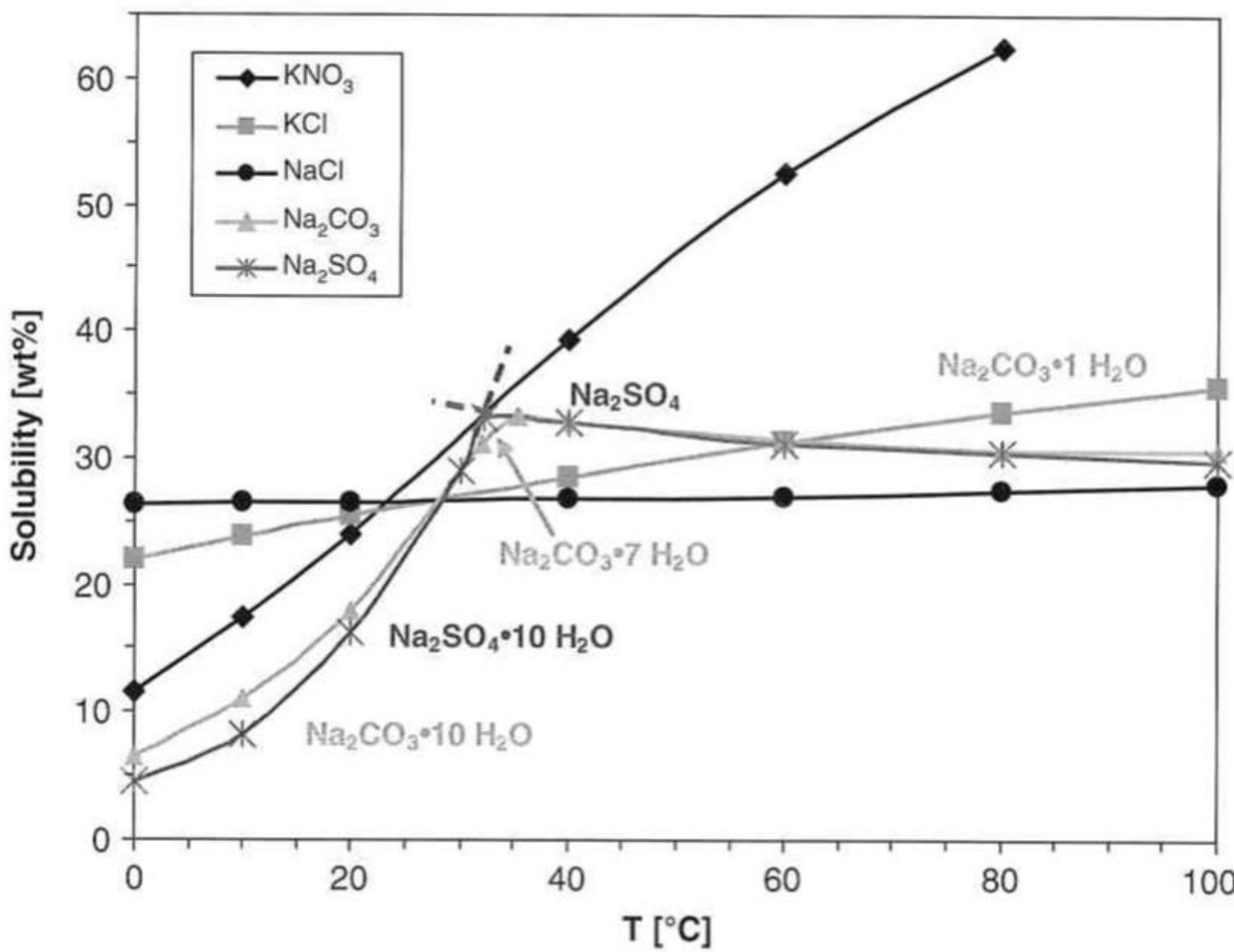
## Important:

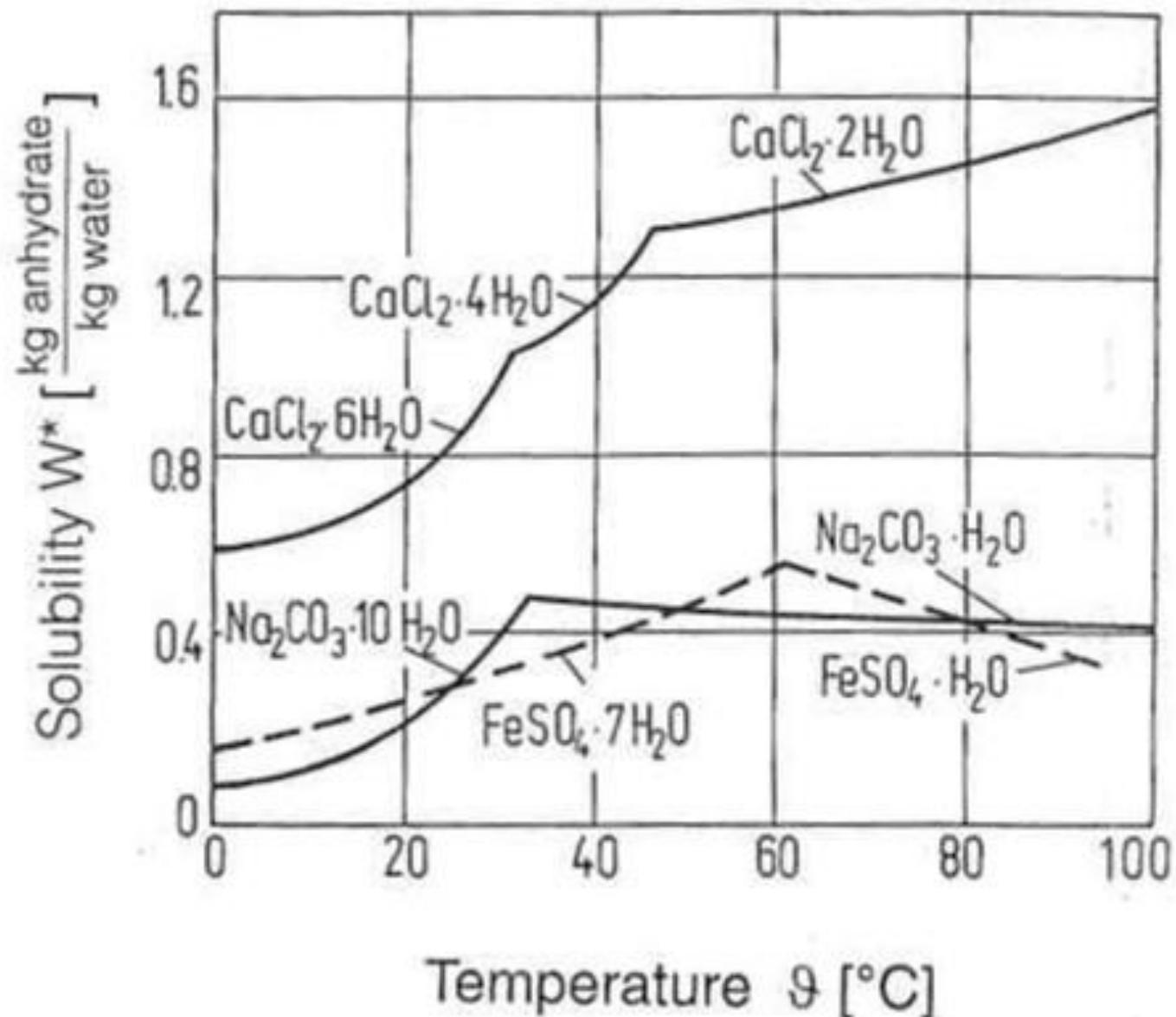
→ Control of the experimental parameters (temperature, pressure, concentration) ***to avoid or generate metastable modifications***

# Phase transformations: principles

(left) schematic solubility diagrams for polymorphic systems exhibiting enantiotropic and monotropic phase transformations, (right) schematic solubility diagram for  $\text{CaCl}_2$ - hydrate structures exhibiting enantiotropic phase transformations





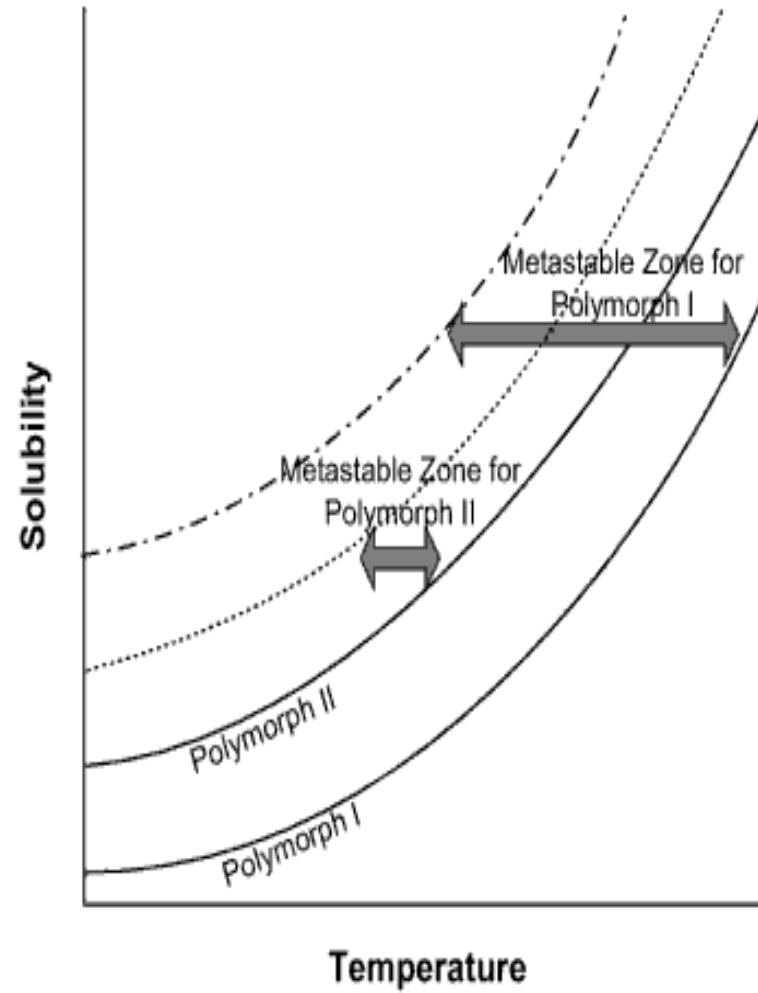
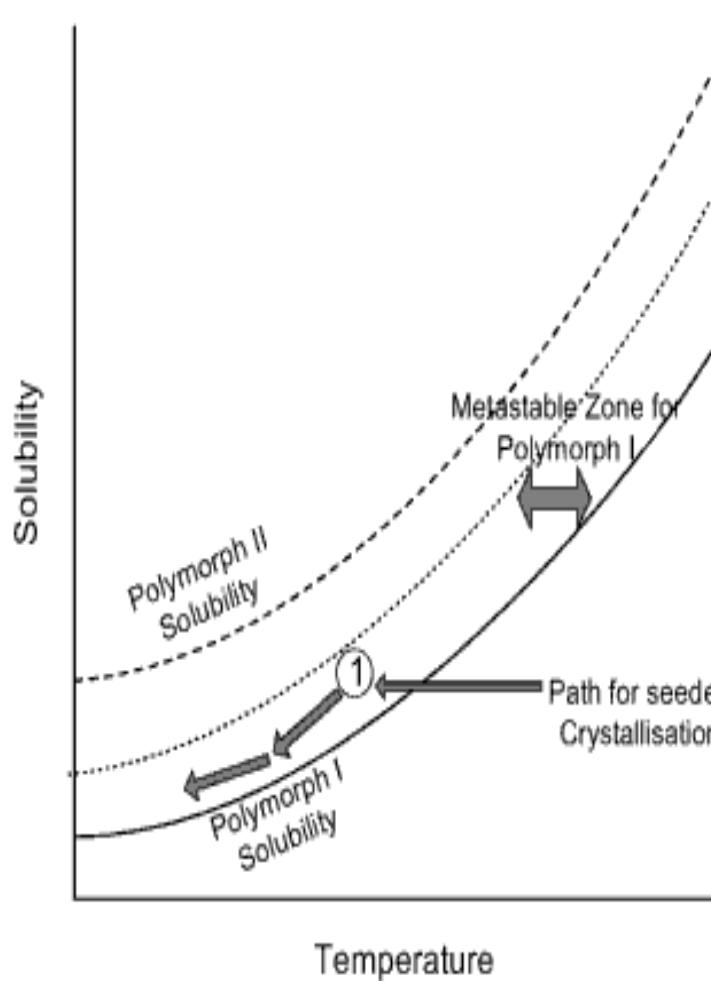


Different units to express a solution concentration of 10 g Na<sub>2</sub>SO<sub>4</sub> in 100 g water

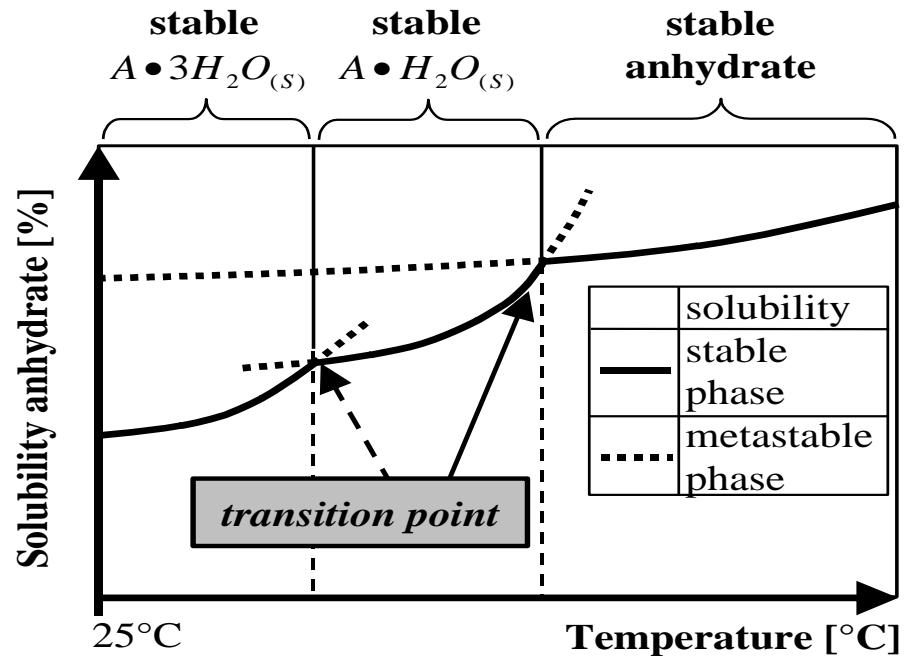
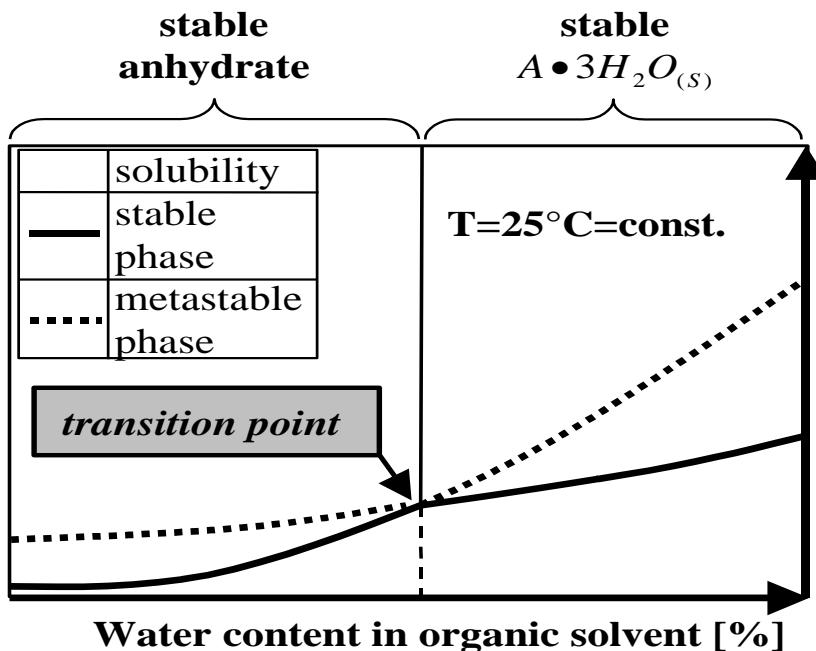
(Substance available as anhydrous Na<sub>2</sub>SO<sub>4</sub> and Glauber's salt (Na<sub>2</sub>SO<sub>4</sub>·10 H<sub>2</sub>O))

- 9.1 g Na<sub>2</sub>SO<sub>4</sub> / 100 g solution = 9.1 wt%
- 12.7 mol Na<sub>2</sub>SO<sub>4</sub> / 1000 mol H<sub>2</sub>O
- 0.7 mol Na<sub>2</sub>SO<sub>4</sub> / 1000 g H<sub>2</sub>O
- 26 g Na<sub>2</sub>SO<sub>4</sub>·10 H<sub>2</sub>O / 100 g H<sub>2</sub>O
- 20.6 g Na<sub>2</sub>SO<sub>4</sub>·10 H<sub>2</sub>O / 100 g solution

# Different possibilities of MSZW of monotropic system, overlapped MSZ of form I (right)



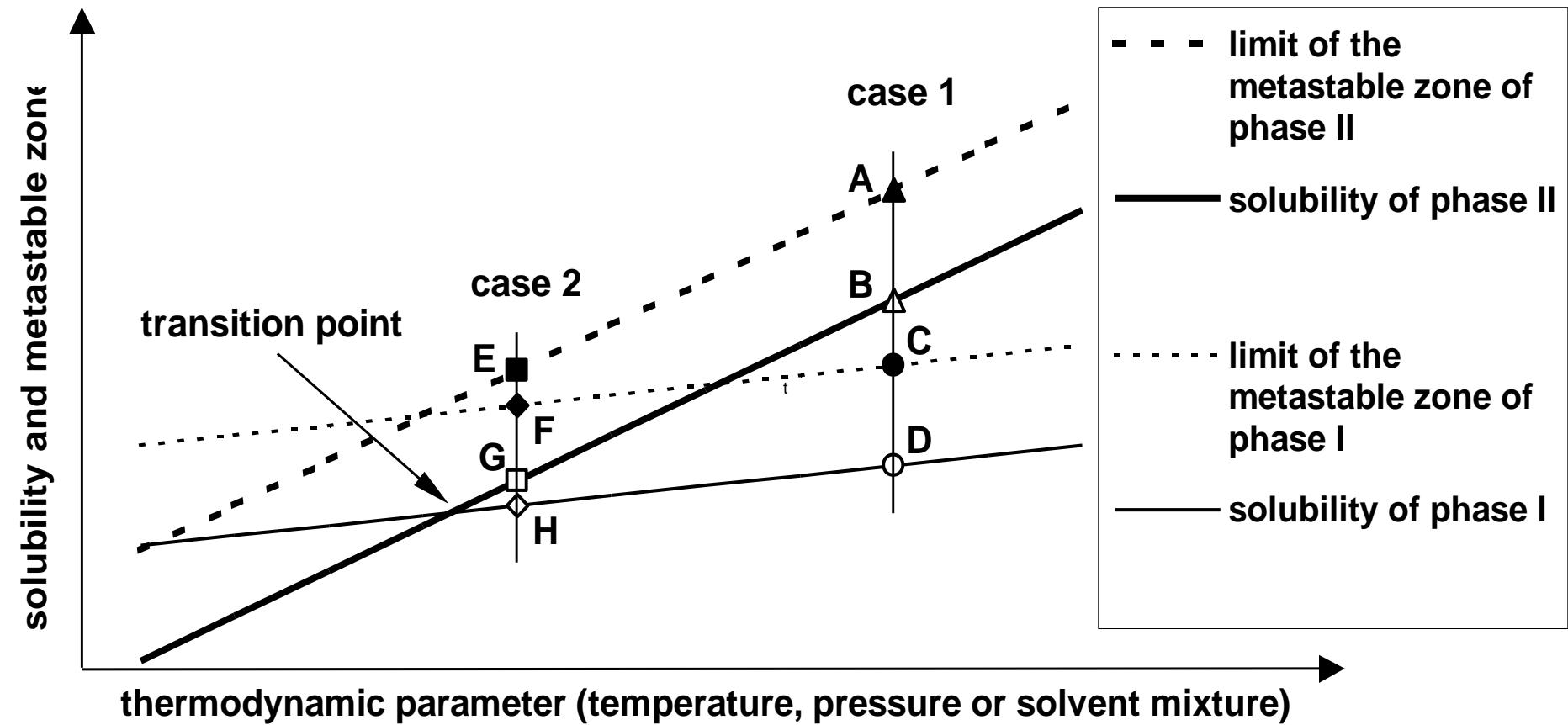
# Comparison of *transition points* in binary and ternary systems



a) ternary system  
 (anhydride A - water - organic solvent),  
 $p, T = \text{const.}$

b) binary system  
 (anhydride A - water),  
 $p = \text{const.}$

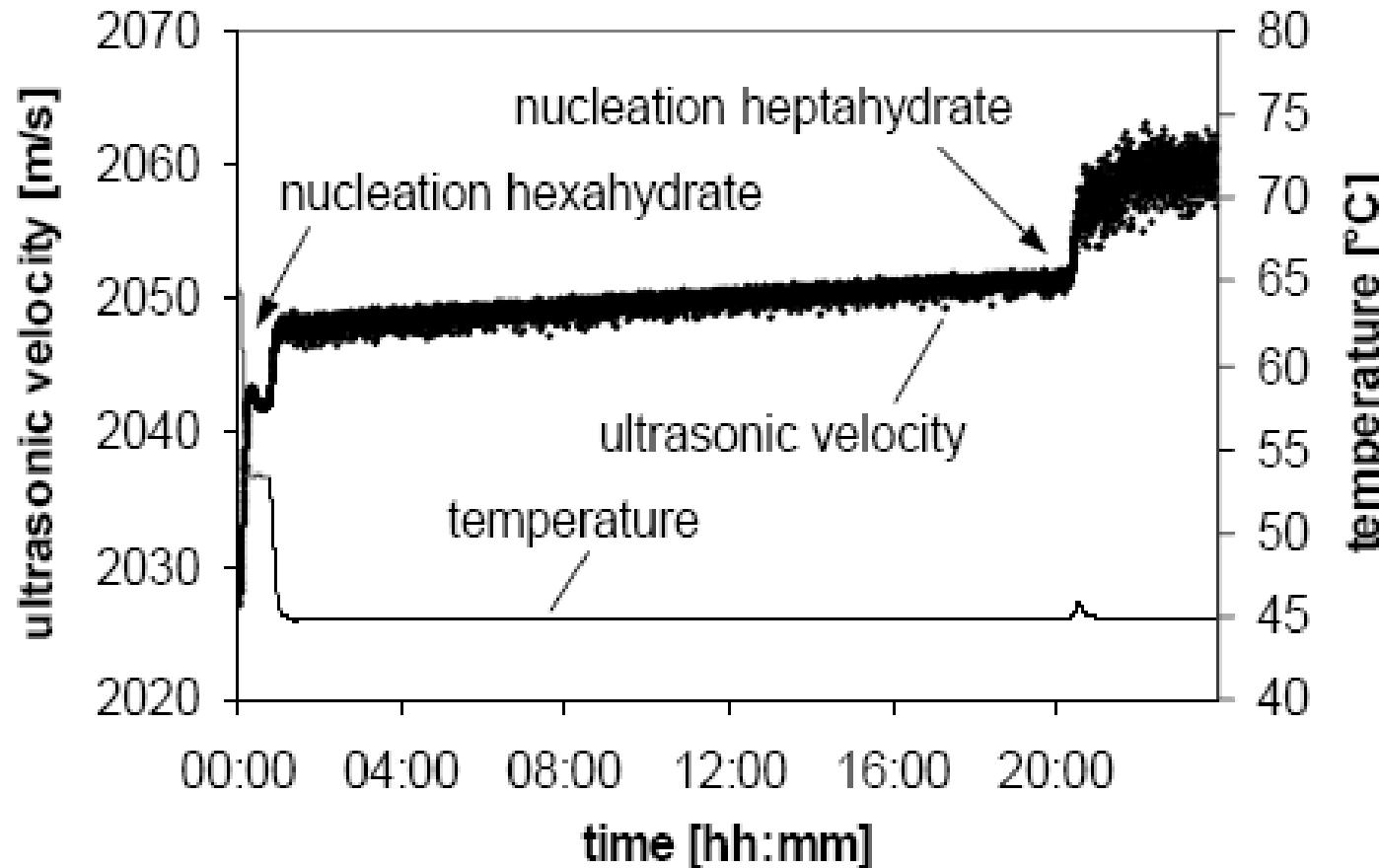
# Metastable Zone



# Example

## Solvates with additives

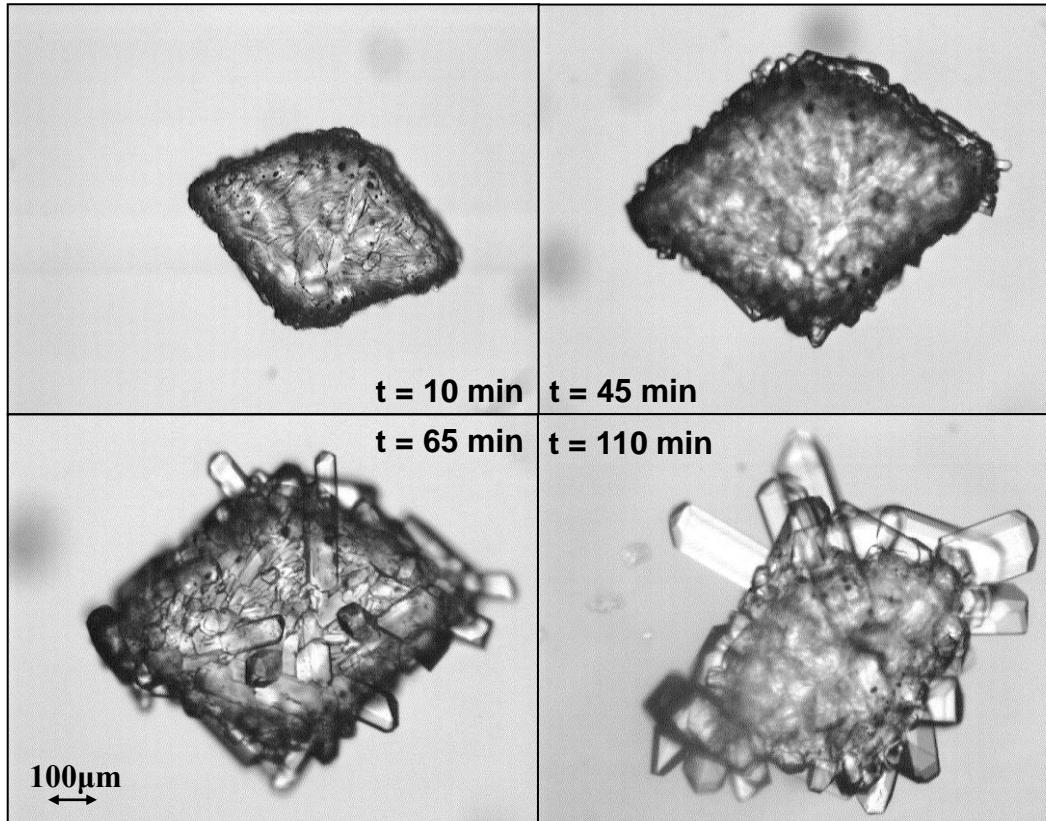
- Phase transformation of magnesium sulfate heptahydrate to the hexahydrate



# Example

making use of the kinetic - time related processes - not only thermodynamics

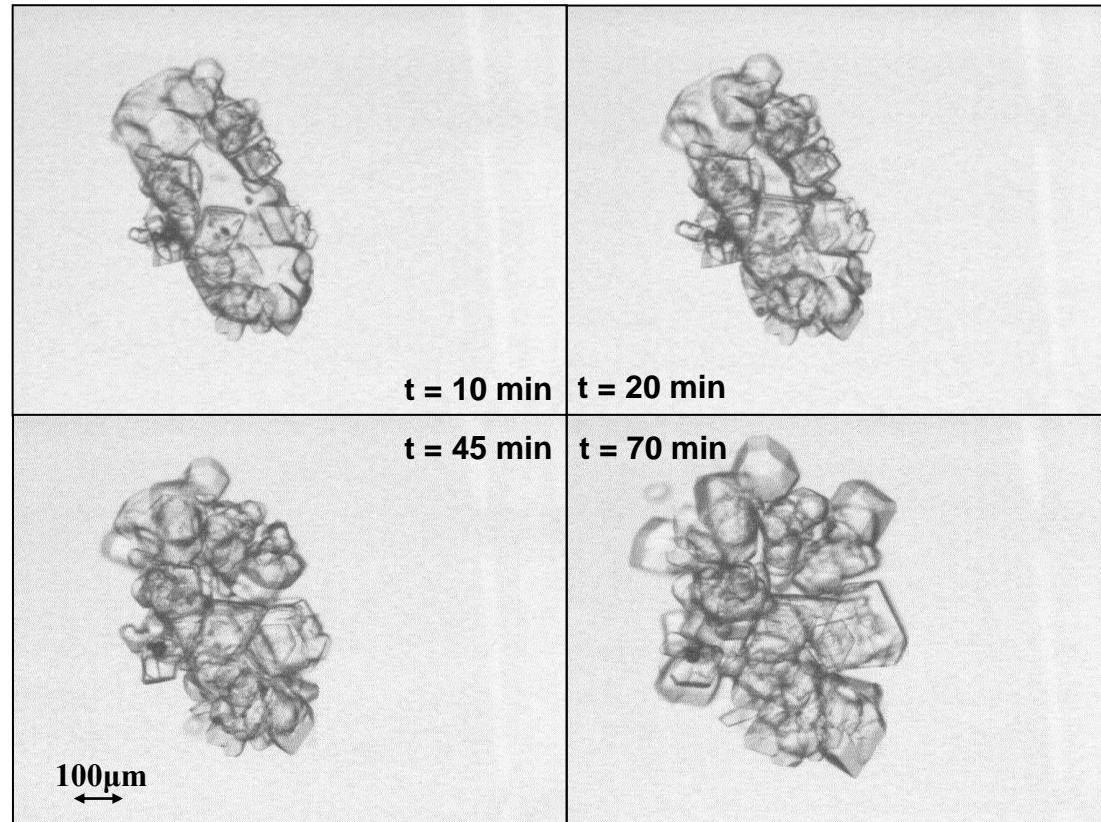
- Phase transformation of magnesium sulfate hexahydrate to the heptahydrate



# Example

making use of the kinetic - time related processes - not only thermodynamics

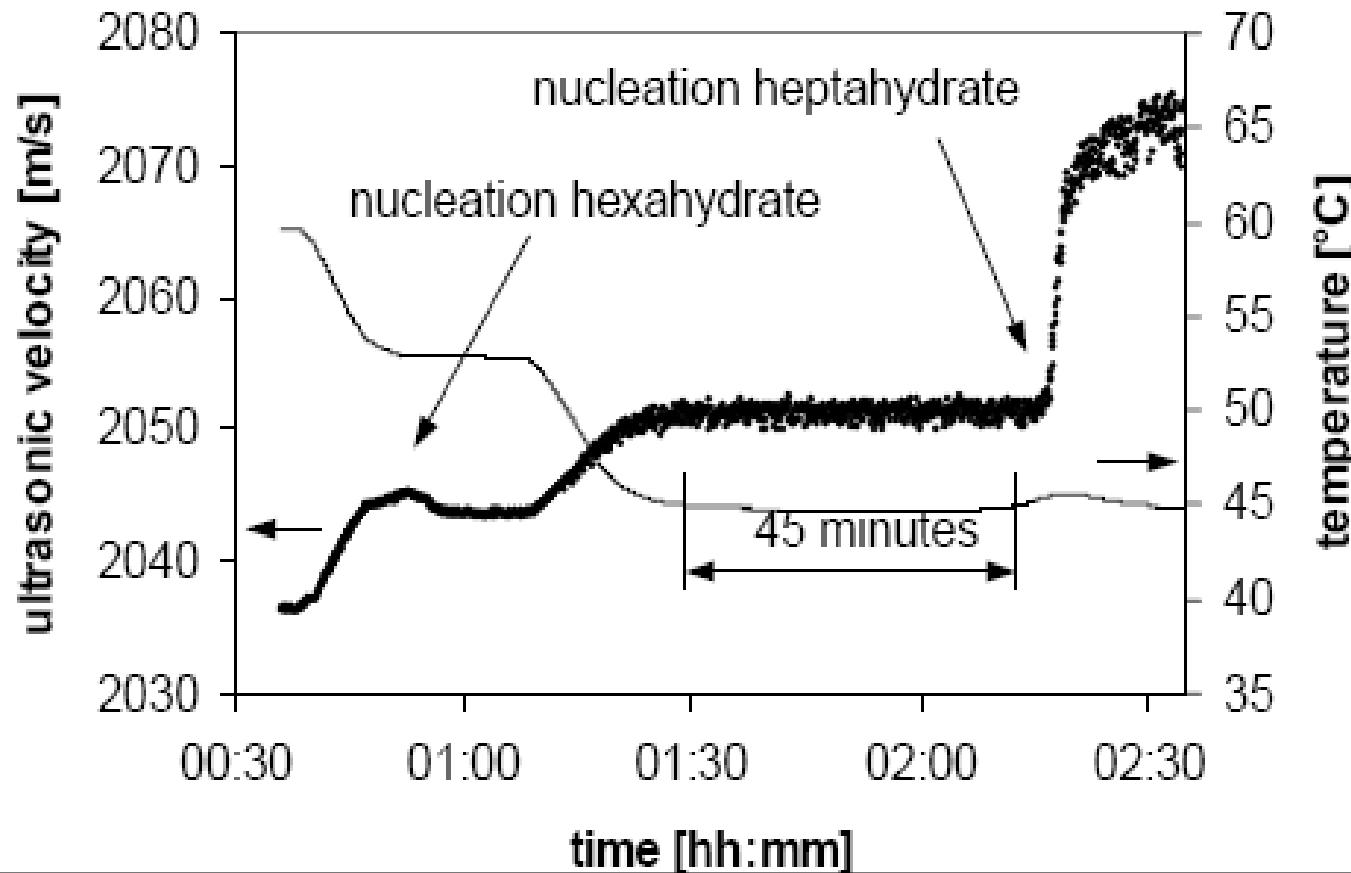
- Phase transformation of magnesium sulfate heptahydrate to the hexahydrate



# Example

## Solvates with additives

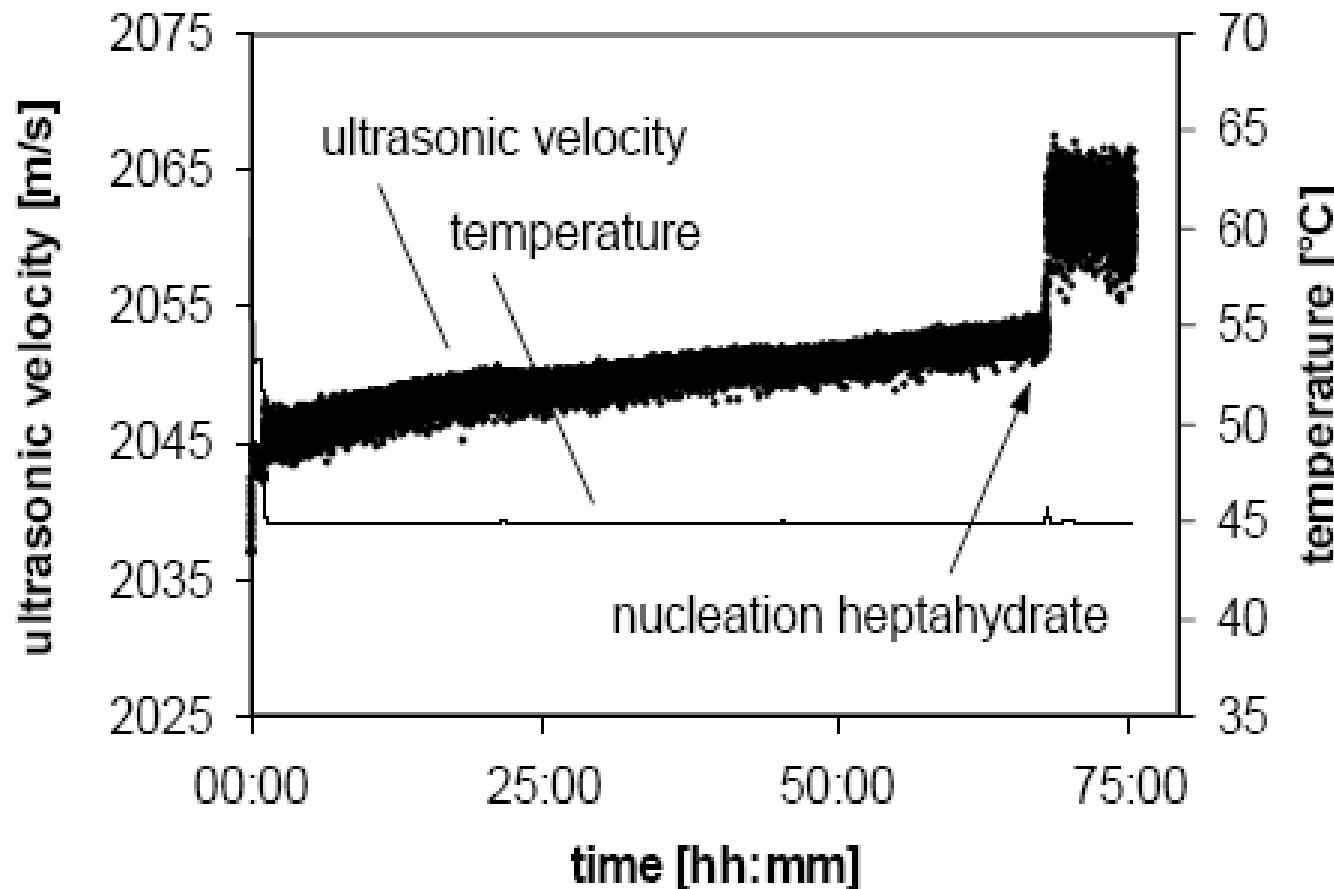
- Phase transformation of magnesium sulfate hydrate with 0.5 wt% KCl



# Example

## Solvates with additives

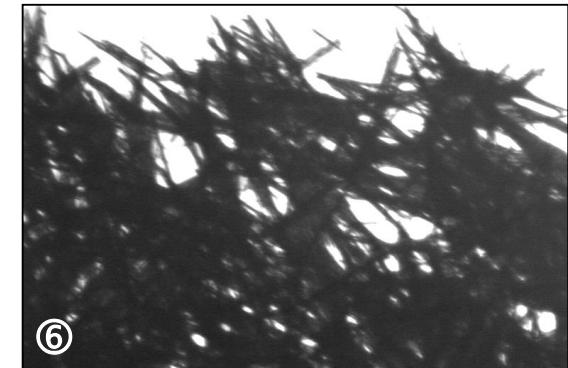
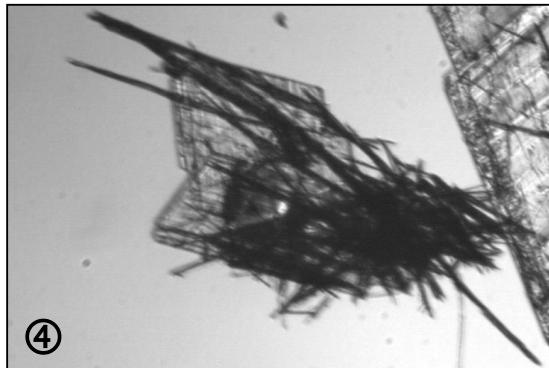
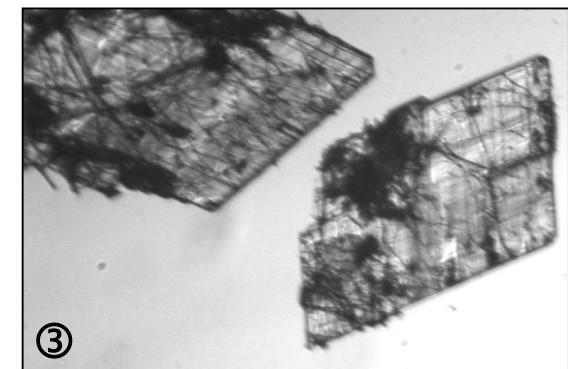
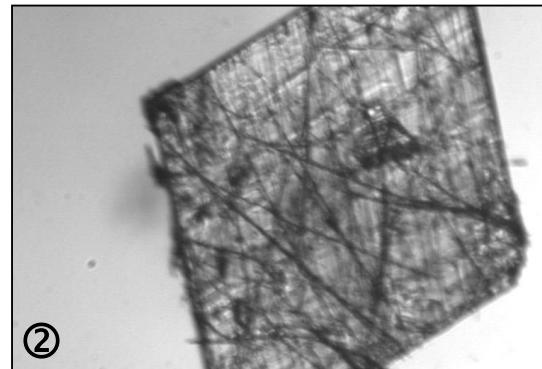
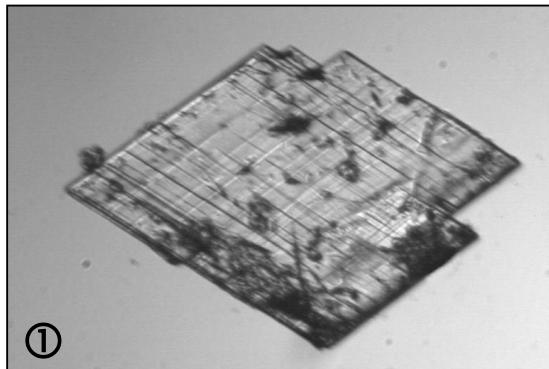
- Phase transformation of magnesium sulfate hydrate with 0.5 wt% borax



# Example

making use of the kinetic - time related processes - not only thermodynamics

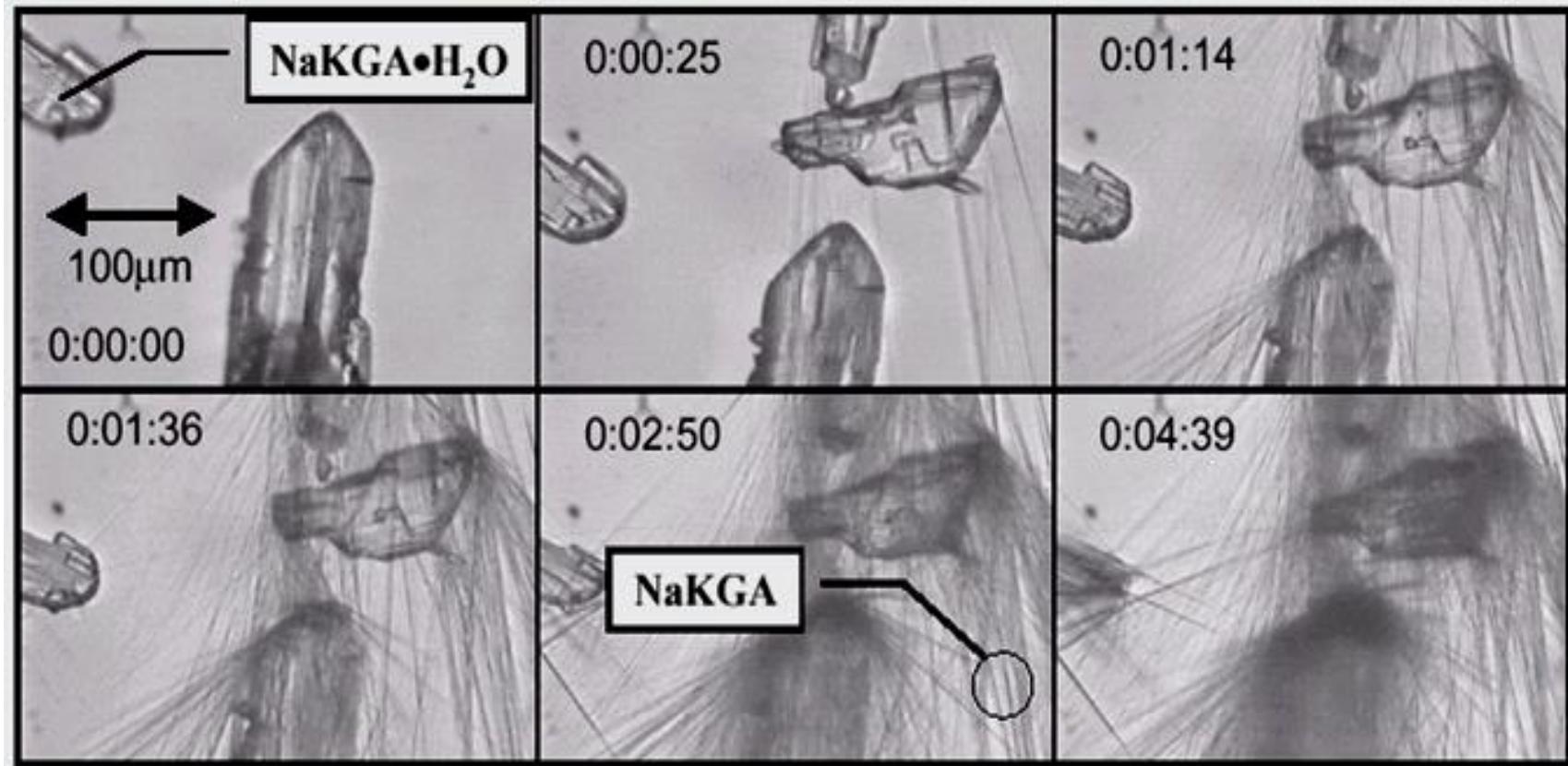
- Phase transformation of anhydrous L-phenylalanine to the monohydrate [1]



[1] Strege, C.: *On (Pseudo-) Polymorphic Phase Transformations*, Dissertation, Martin-Luther-Universität Halle-Wittenberg, PhD-thesis, Martin-Luther-Universität Halle-Wittenberg, online-publication:  
<http://sundoc.bibliothek.uni-halle.de/diss-online/04/04H318/index.htm>, 2004.

# Phase Transition

- Sodium-2-keto-L-gulonate-monohydrate (skgm)
- growth rate of the needles:  $10^{-5} - 10^{-4} \text{ ms}^{-1}$



Needle growth during the transformation of skgm in methanol

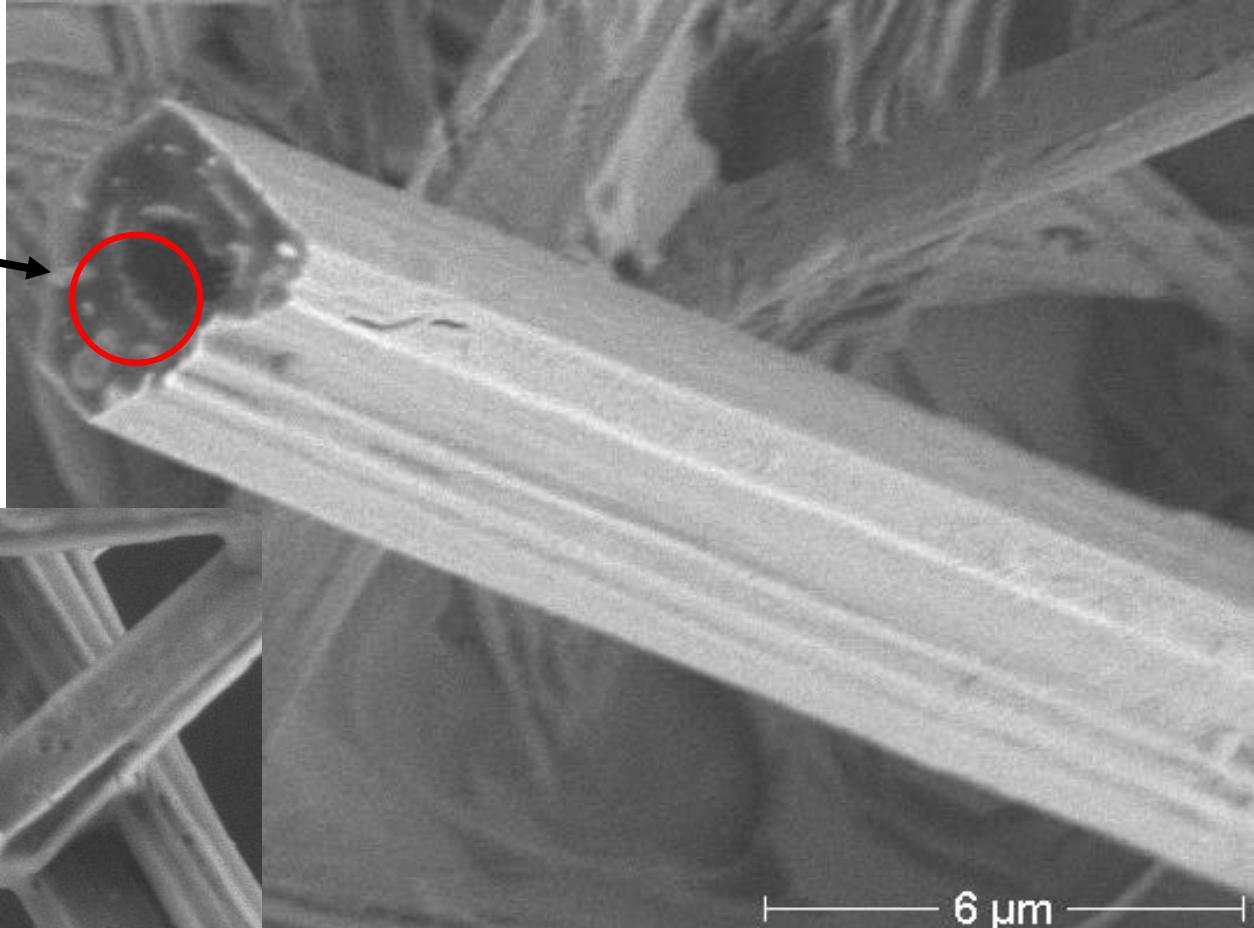
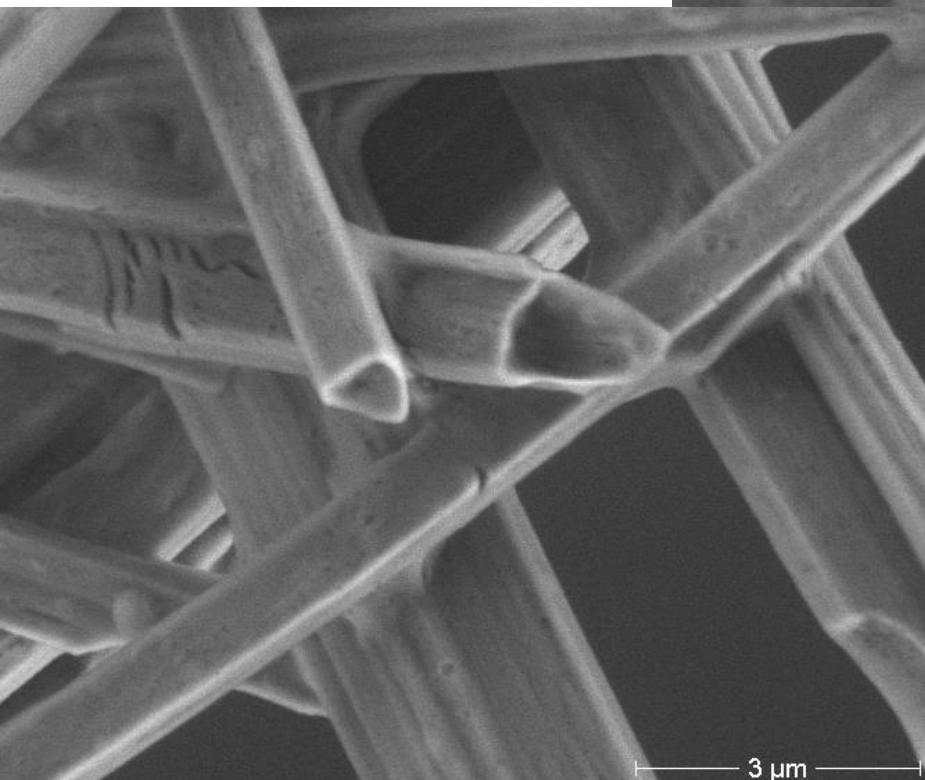
Bechtloff, B.: *Gezielte Beeinflussung der Kinetik von Fest-Flüssig-Reaktionskristallisationen*,  
Dissertation, Martin-Luther-Universität Halle-Wittenberg, 2002,  
Onlineveröffentlichung: <http://sundoc.bibliothek.uni-halle.de/diss-online/02/02H105/index.htm>.

# Solvent mediated phase transitions

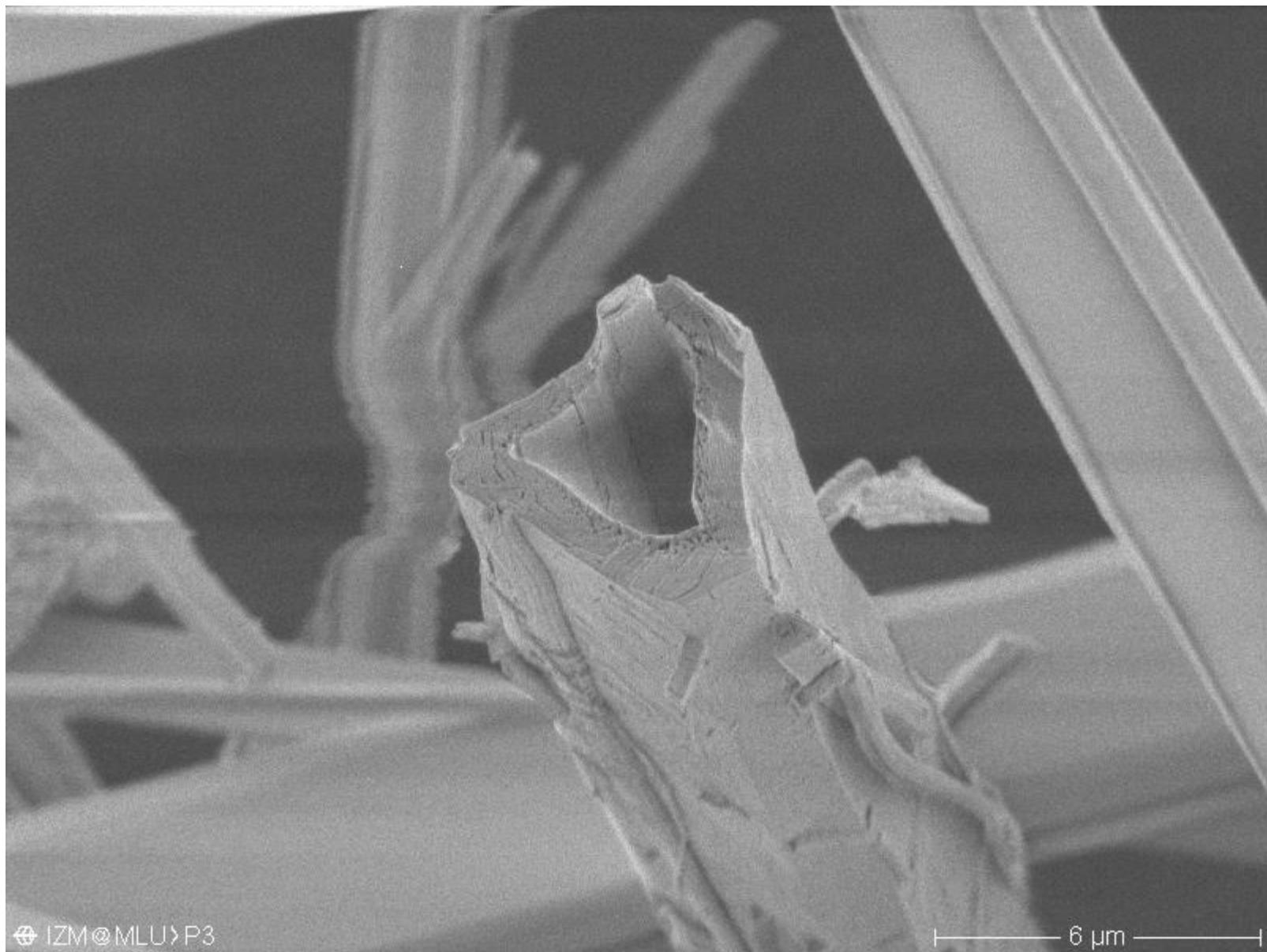


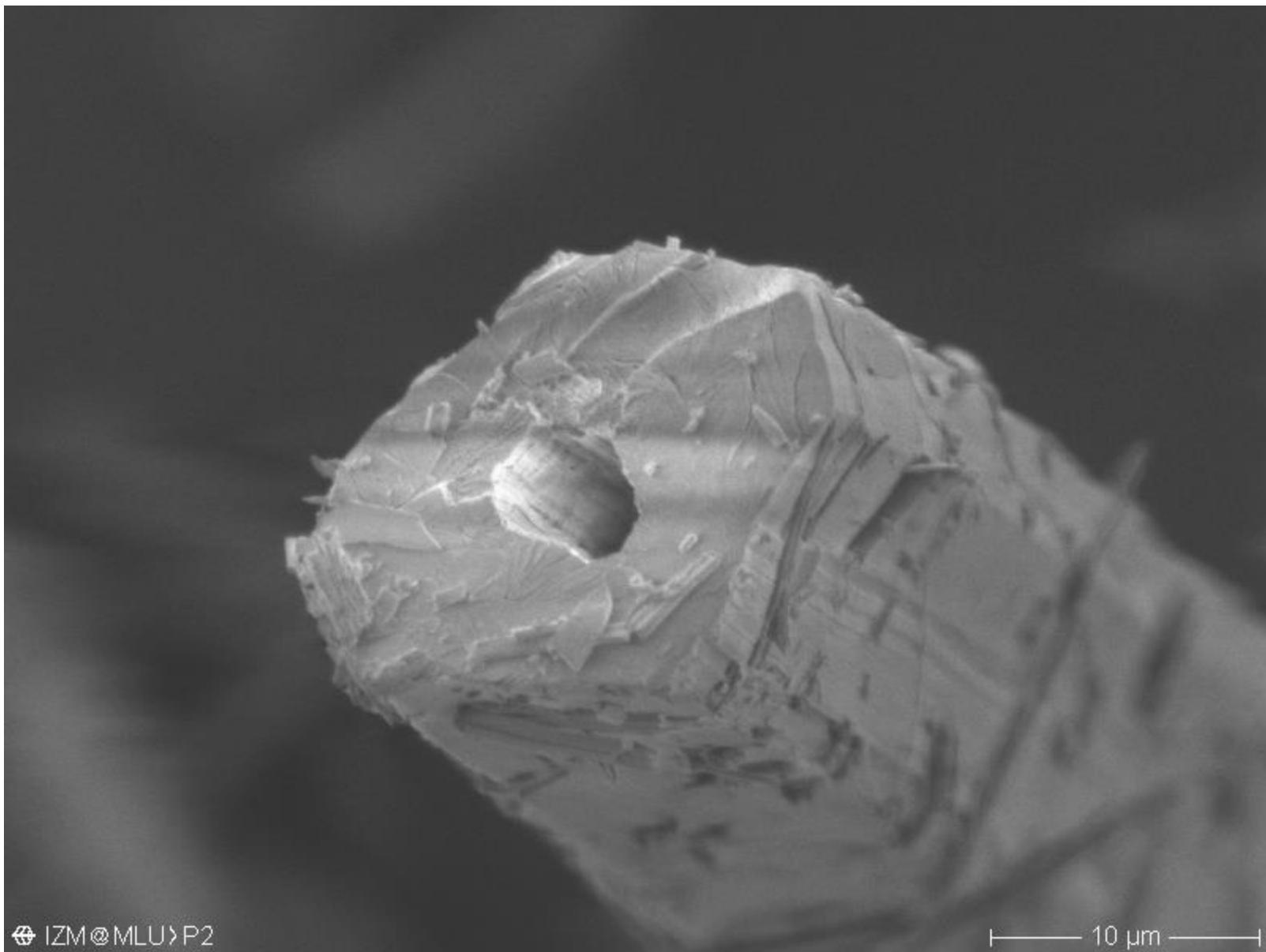
100g methanol ( $\approx$ 150ml, left); 10g NaKGA monohydrate (centre),  
after suspending the hydrate in methanol (right)

**internal diameter  
approximately 1.3  $\mu\text{m}$**



SEM images of hollow skga needles.



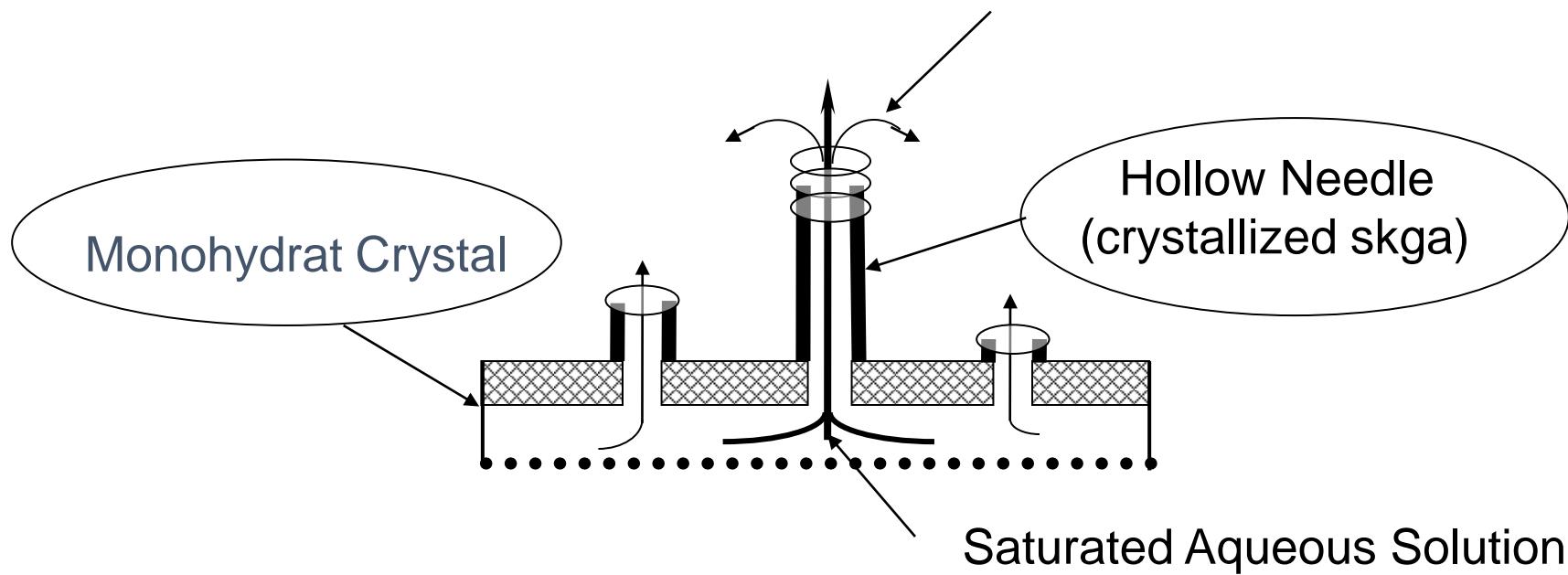




# Dehydration in Methanol

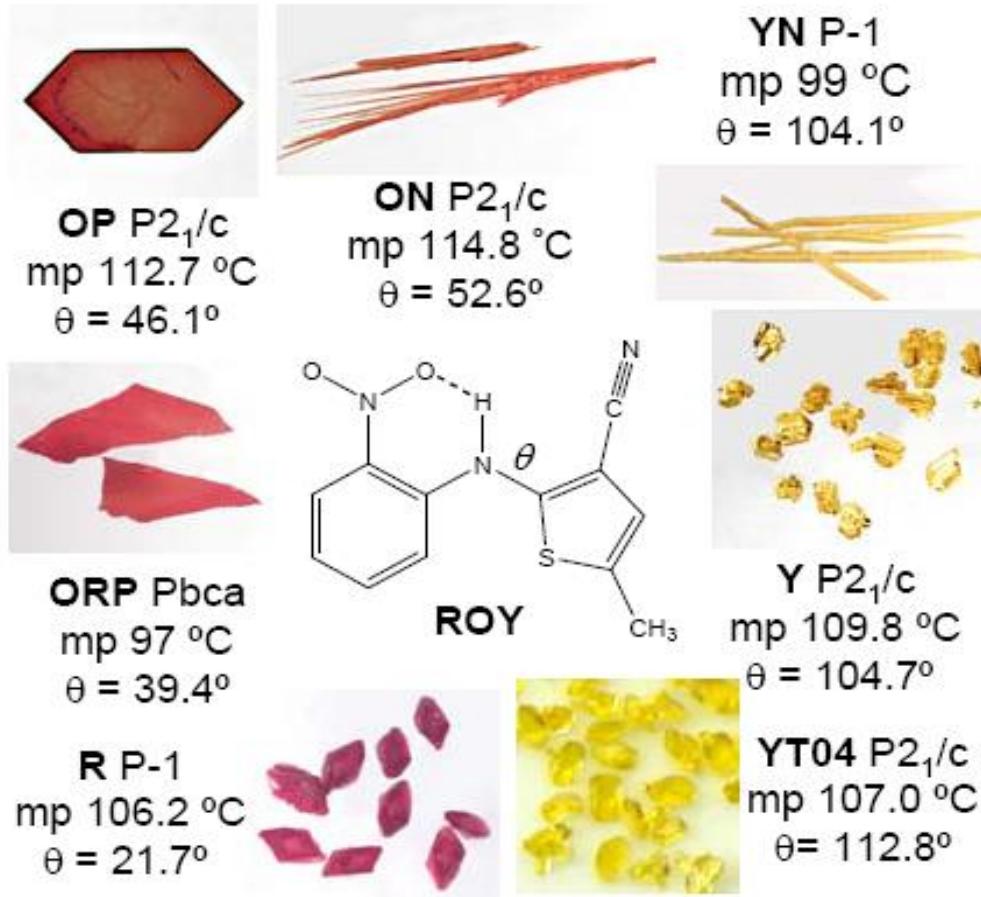
Methanol Environment

Water → Methanol



# Color difference between polymorphs of ROY

Olanzapine



Guo, J.: *Crystallization of Polymorphs: A Case Study on Astaxanthin and Apocarotenoic Ester*, Dissertation, Martin-Luther-Universität Halle-Wittenberg, 2009.

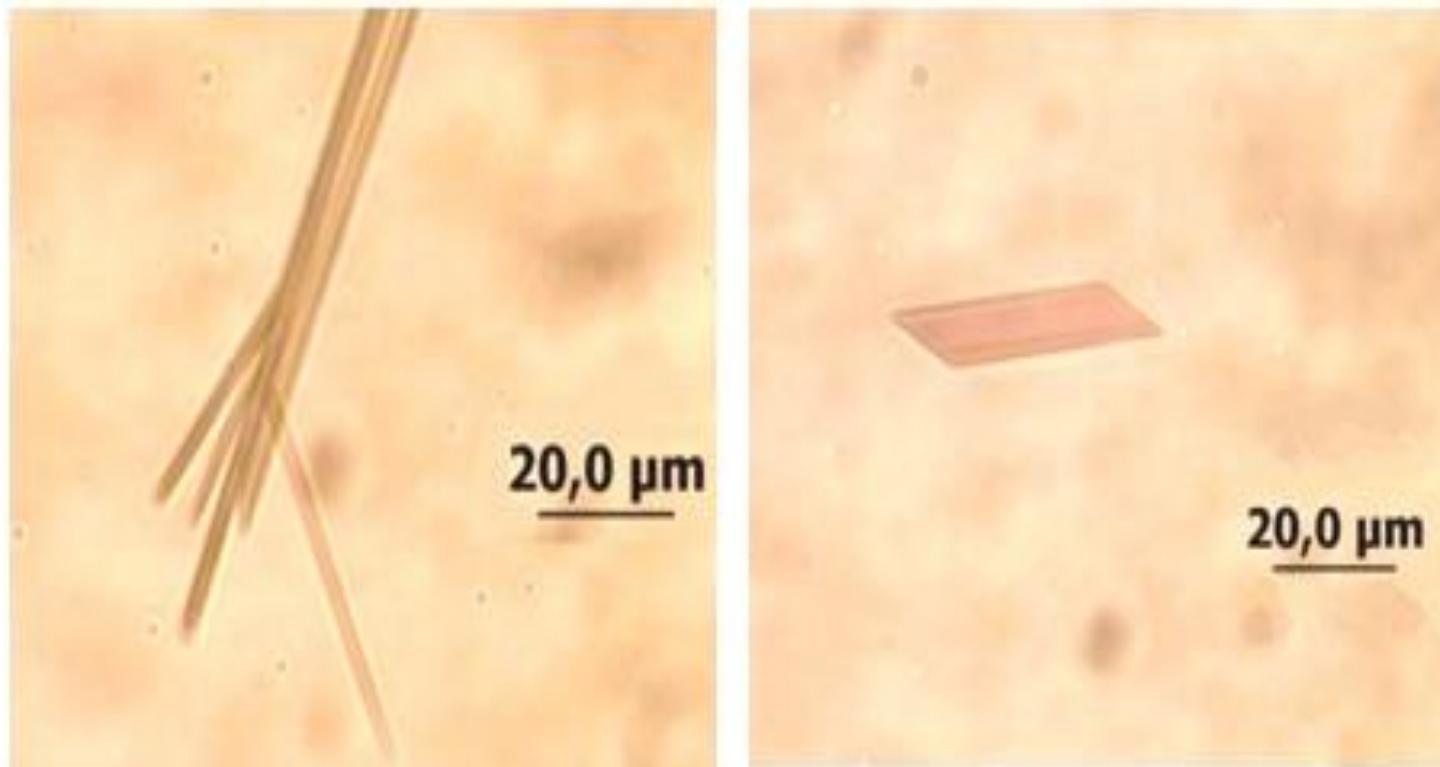
Yu, L., Chen, S., Xi, H.: *Cross Nucleation between ROY Polymorphs*, J. Am. Chem. Soc., 127 (2005), 17439 – 17444.<sup>27</sup>

# Techniques available for the examination of polymorphs

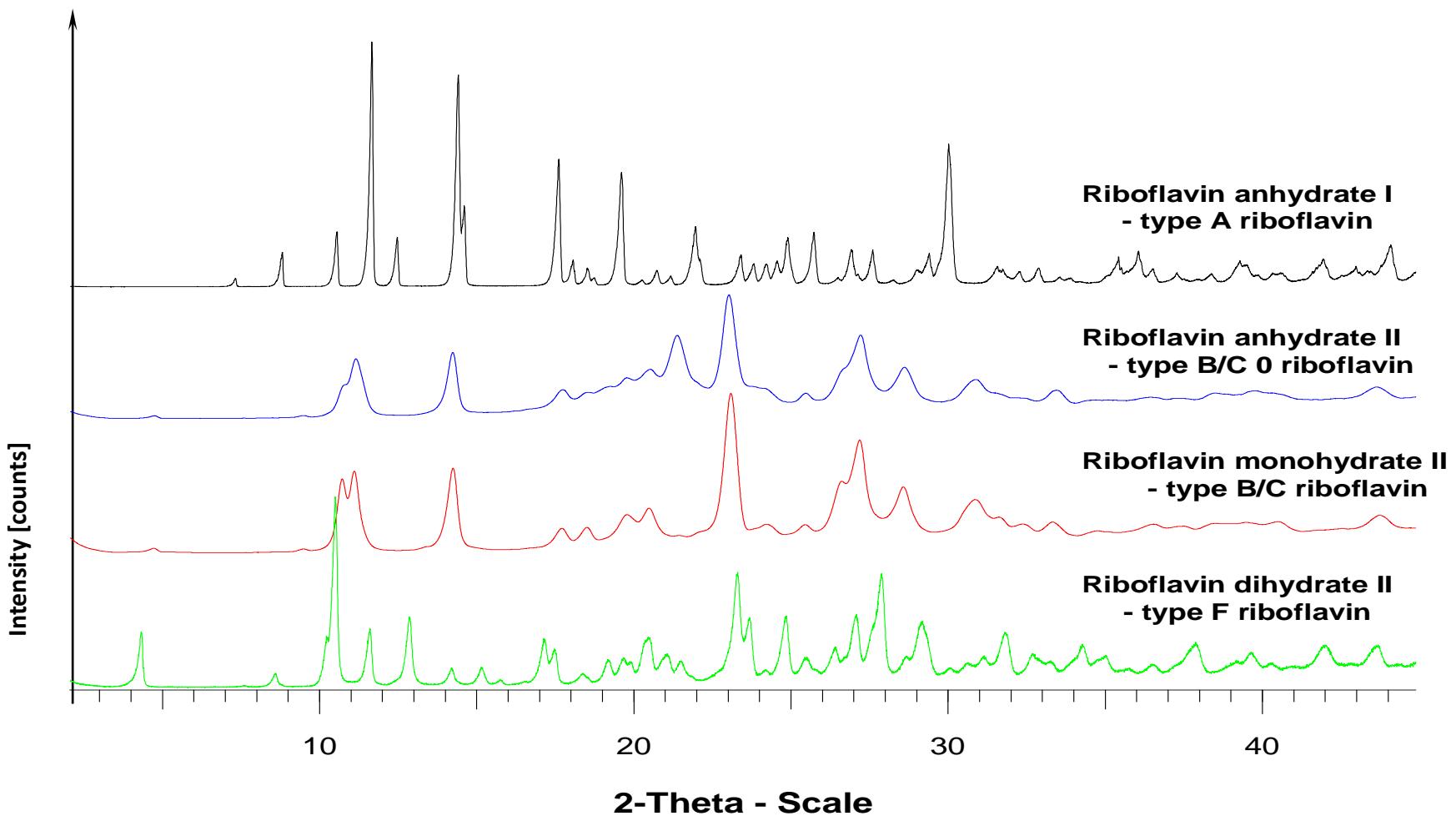
Method	Data measured	Feature obtained	Literature
Optical microscopy	Refractive index Inherent and polarization colour Interfacial angles	Particle shape and size, Surface characteristics Inclusions Symmetry elements	HAR 1960, 1964, McC 1978 McL 1990, STR 1997, BER 1998
Solubility analysis	Amount dissolved per volume and time (in different solvents)	Dissolution kinetics Saturation solubility Phase transition point	BUR 1982, BRI 1999, GU 2001
Moisture sorption/ desorption isotherms	Change of mass versus variable RH%	Hygroscopy Study of solvation and desolvation Prediction of handling properties	???
DSC	Heat flow versus temperature	Study of glass transition, melting and recrystallization point	GIR 1995, 1999, 2001, BUR 1990
TG	Change of mass versus temperature	Study of solvates Release and stability testing	CHE 2000, BRI 1995
FT-IR, ATR, DRIFT	IR-spectrum	Chemical information Phase characterization	KUH 1976, BRI 1997, GIR 1990, 1999,
Raman	Raman-spectrum	Chemical information Phase characterization	TUD 1993, TER 1994, GU 1995
Solid state NMR	Magnetic resonance	Chemical information Phase characterization	BUG 1993, HAR 1993, BRI 1997, BYR 1999
X-ray diffraction	Diffractogram	Chemical information Phase characterization structure determination Crystallinity measurement	AZA 1958, BIS 1989, ZEV 1995, JEN 1996, STE 2001

# Microscope images of the crystals of form I (left) and form II (right)

---



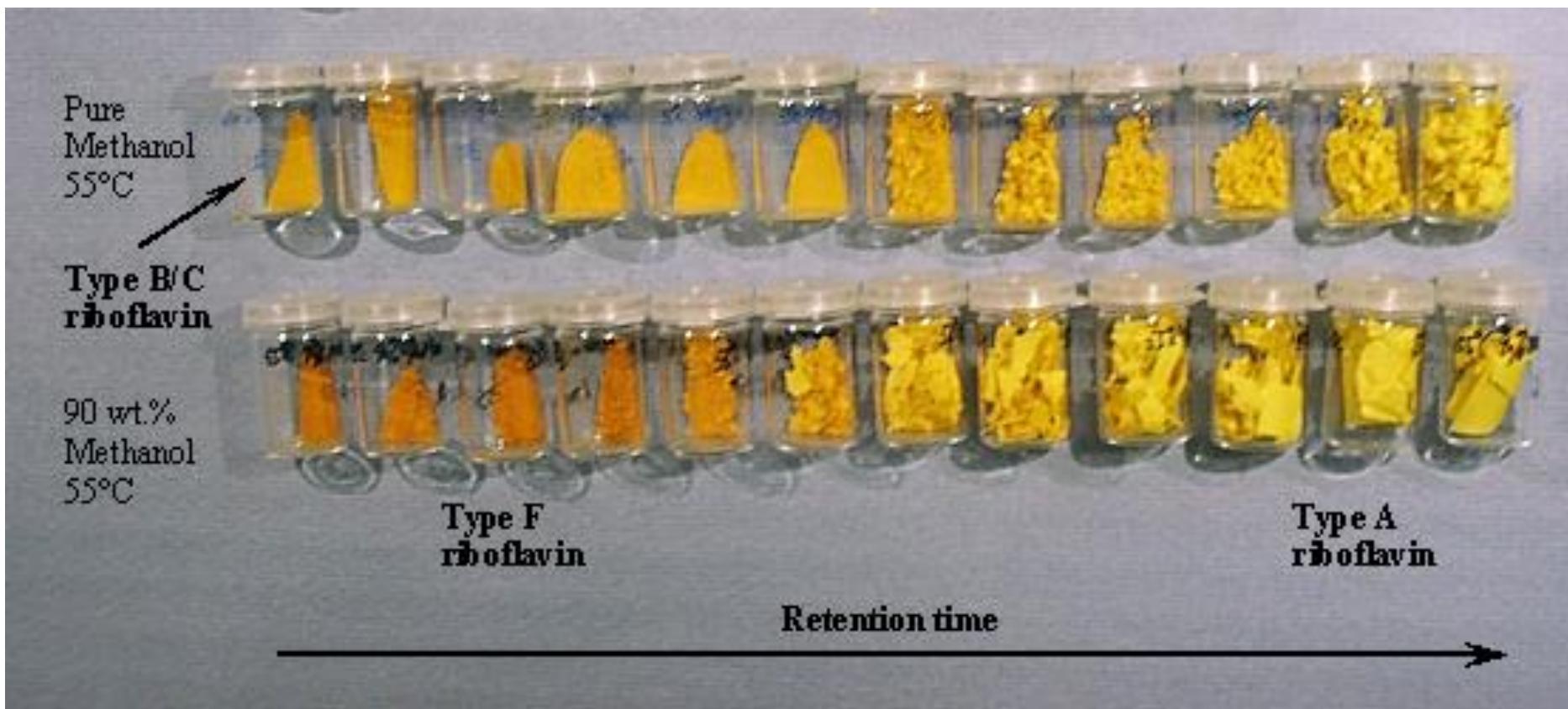
# Powder XRD patterns of known riboflavin structures (part I)



# Example

## polymorph

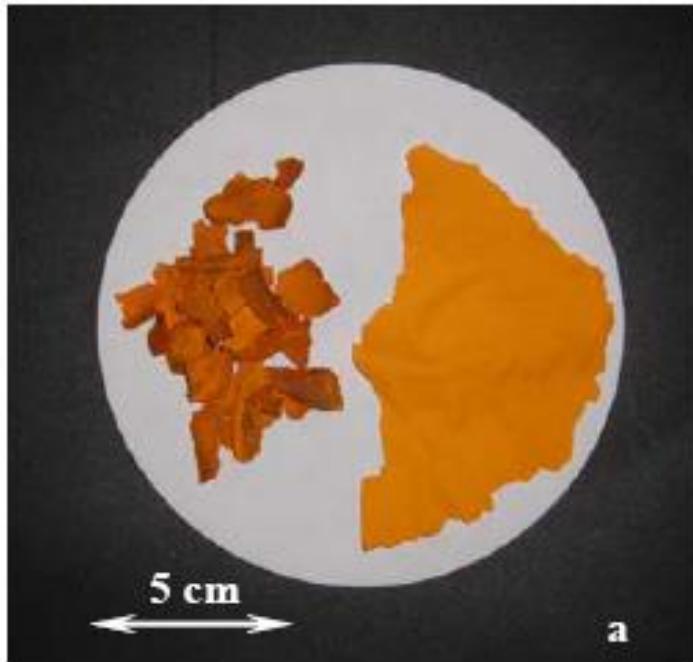
- Influence of crystal structure, temperature, retention time and solvent composition on the colour of riboflavin crystals<sup>[1]</sup>



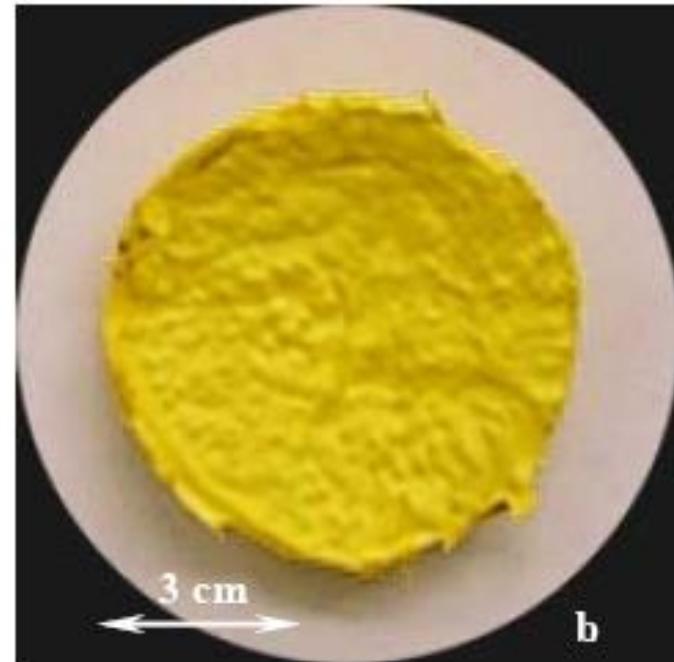
# Example

## polymorph

- Influence of solvent content on the crystal structure of riboflavin



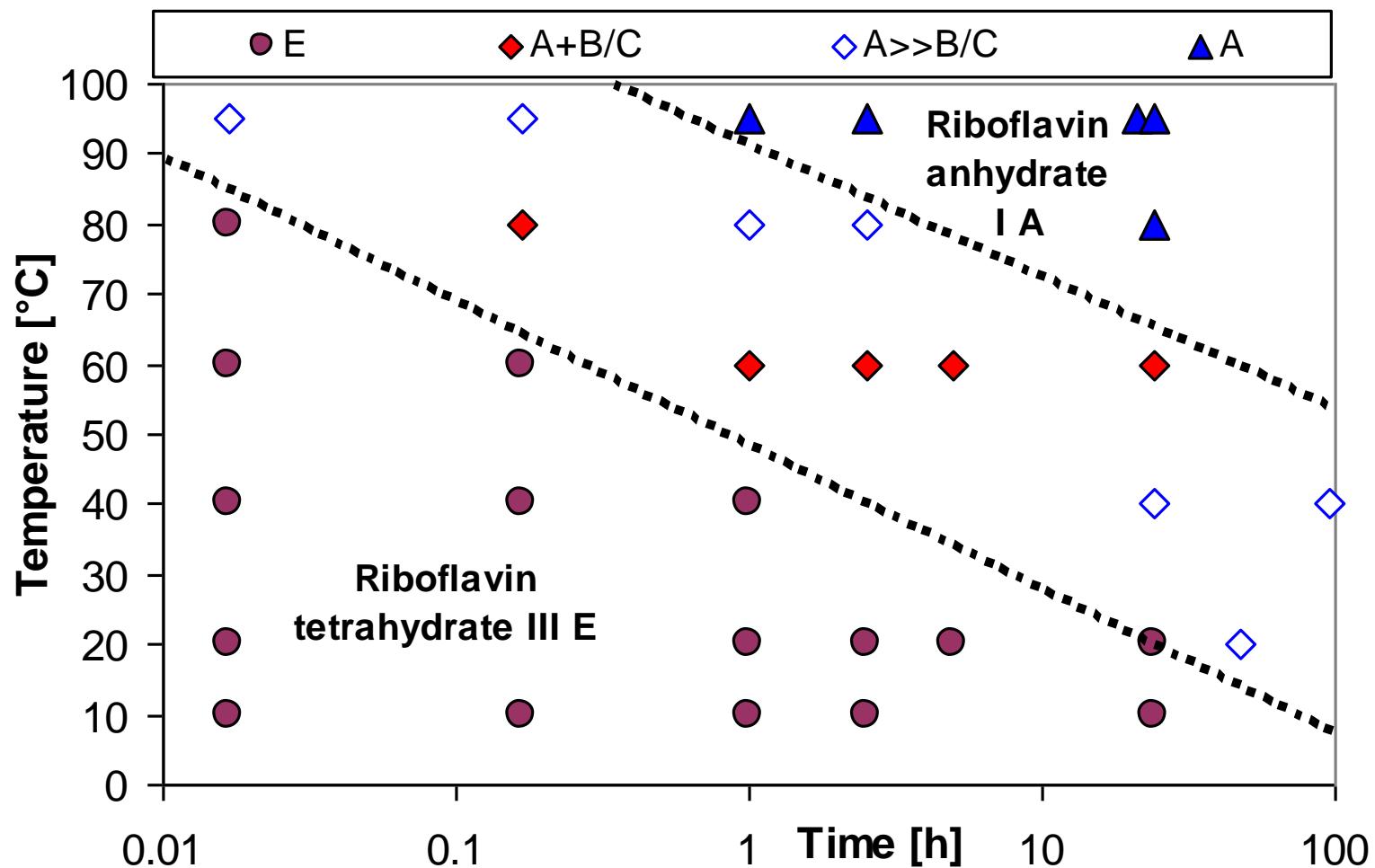
type B/C riboflavin derived  
from type E riboflavin



type A riboflavin derived  
from type E riboflavin

# Example

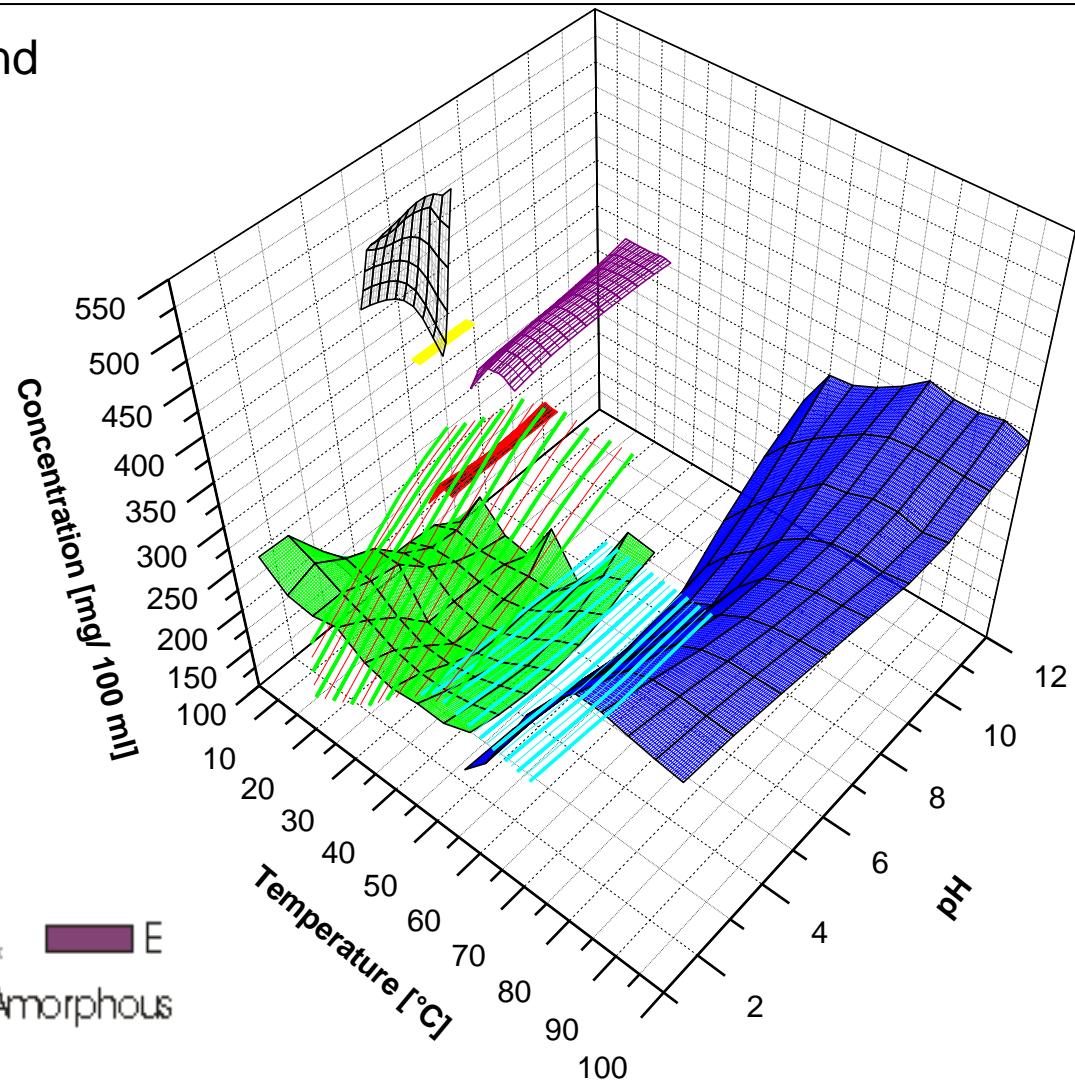
- Phase transition behaviour of type E riboflavin in water



# Example

## polymorph

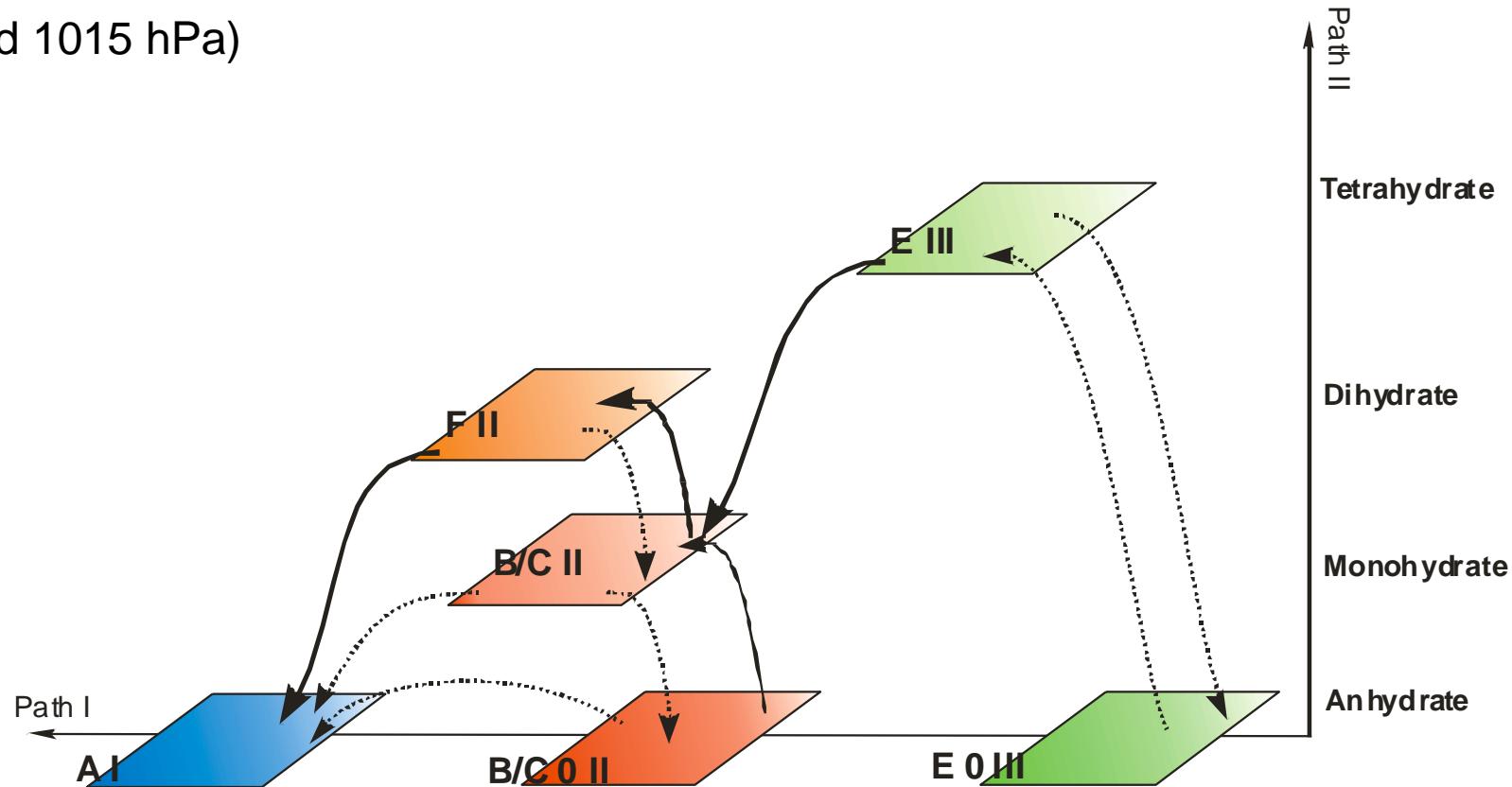
- Influence of temperature, pH and concentration on the crystal structure formation of riboflavin



# Example

## polymorph

- Phase transition pathways of riboflavin (Riboflavin anhydrate I (A)=thermodynamic stable crystal form of riboflavin, at room temperature, normal pressure (18 to 25 °C and 1015 hPa))



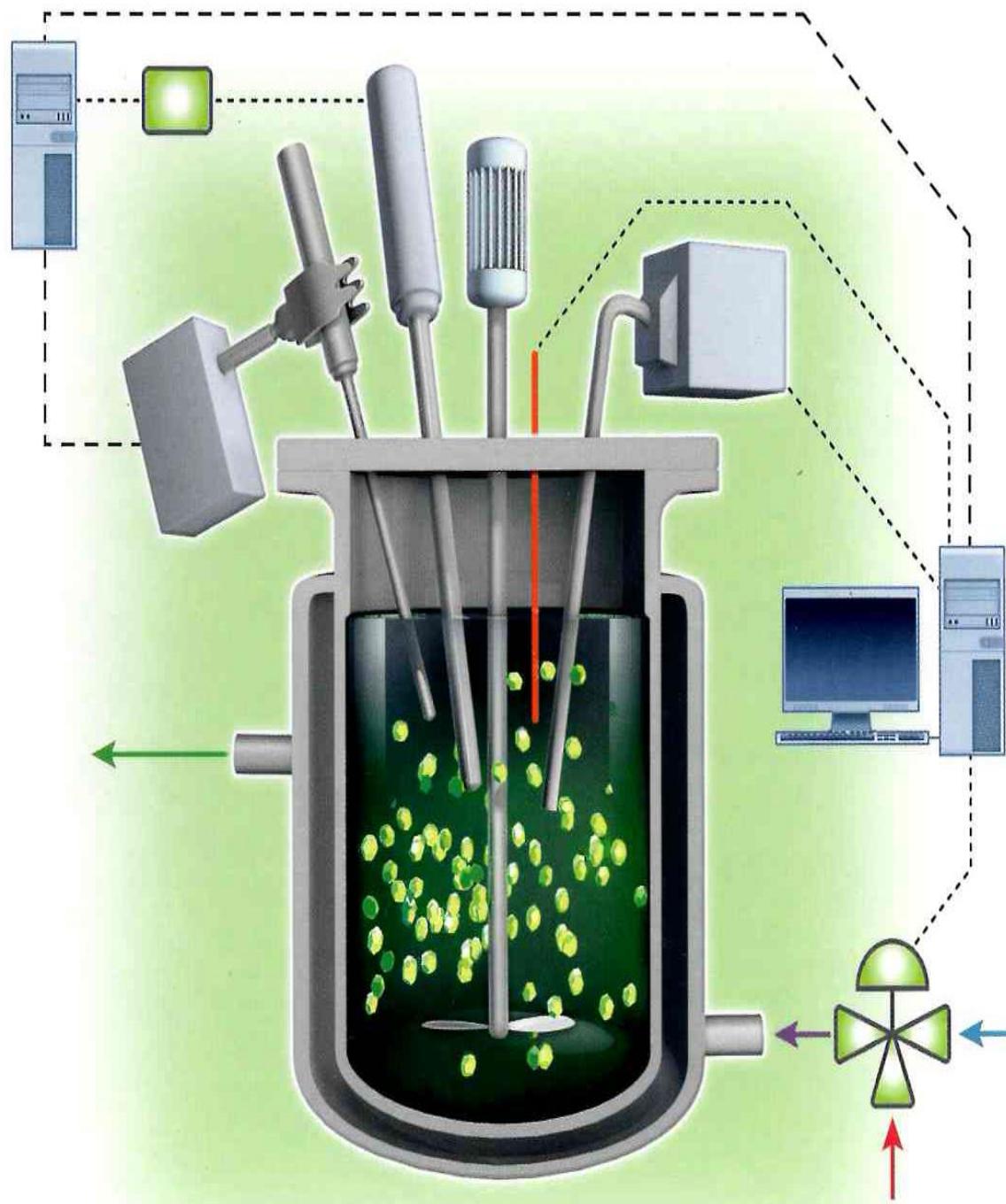
Thank you for your  
attention!



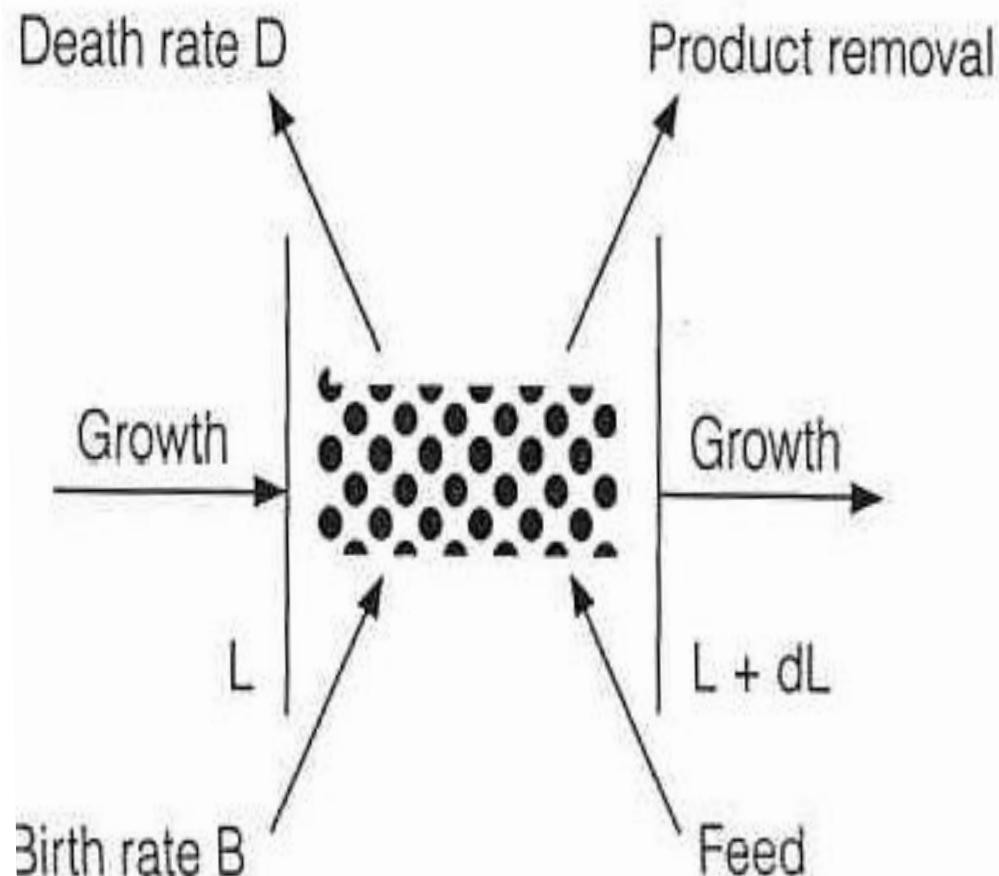
# Process control in batch crystallization

---

Prof. Dr.-Ing. habil. Joachim Ulrich



$$\frac{\partial n}{\partial t} + \frac{\partial(Gn)}{\partial L} + n \frac{\partial V}{V \partial t} + D(L) - B(L) + \sum_k \frac{\dot{V}_i n_i}{V} = 0$$



$$\frac{\partial(Gn)}{\partial L} + \sum_k \frac{n_i \dot{V}_i}{V} = 0$$

$$\frac{\partial(Gn)}{\partial L} + n \frac{\dot{V}}{V} = 0$$

$$\frac{\partial(Gn)}{\partial L} + \frac{n}{\tau} = 0$$

$$G\,\frac{\mathrm{d}n}{\mathrm{d}L}+\frac{n}{\tau}=0$$

$$n = n_0 \exp\left(-\frac{L}{G\tau}\right)$$

$$\ln\left(\frac{n}{n_0}\right) = -\frac{L}{G\tau}$$

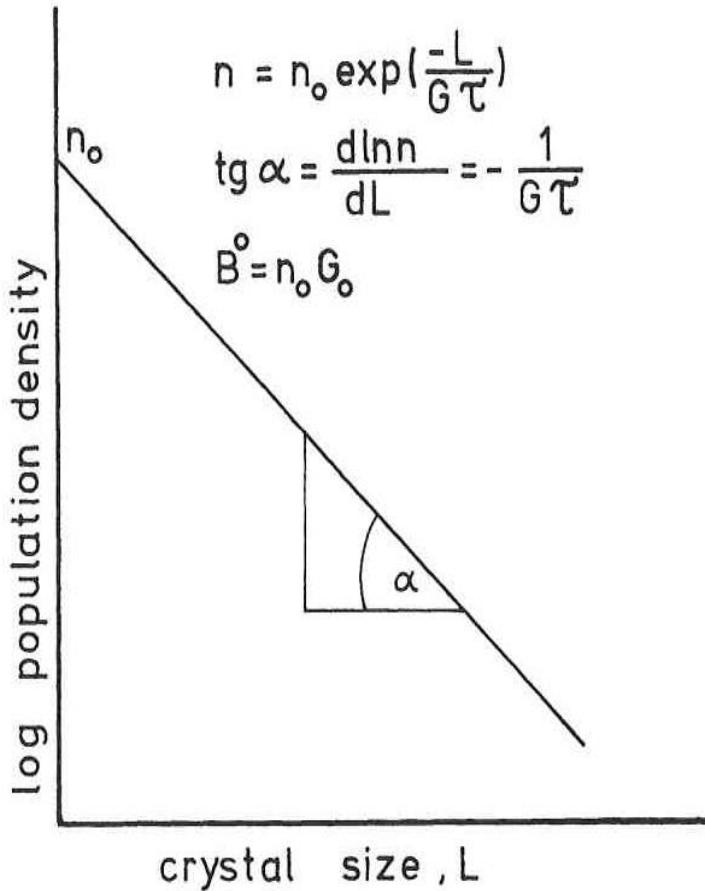
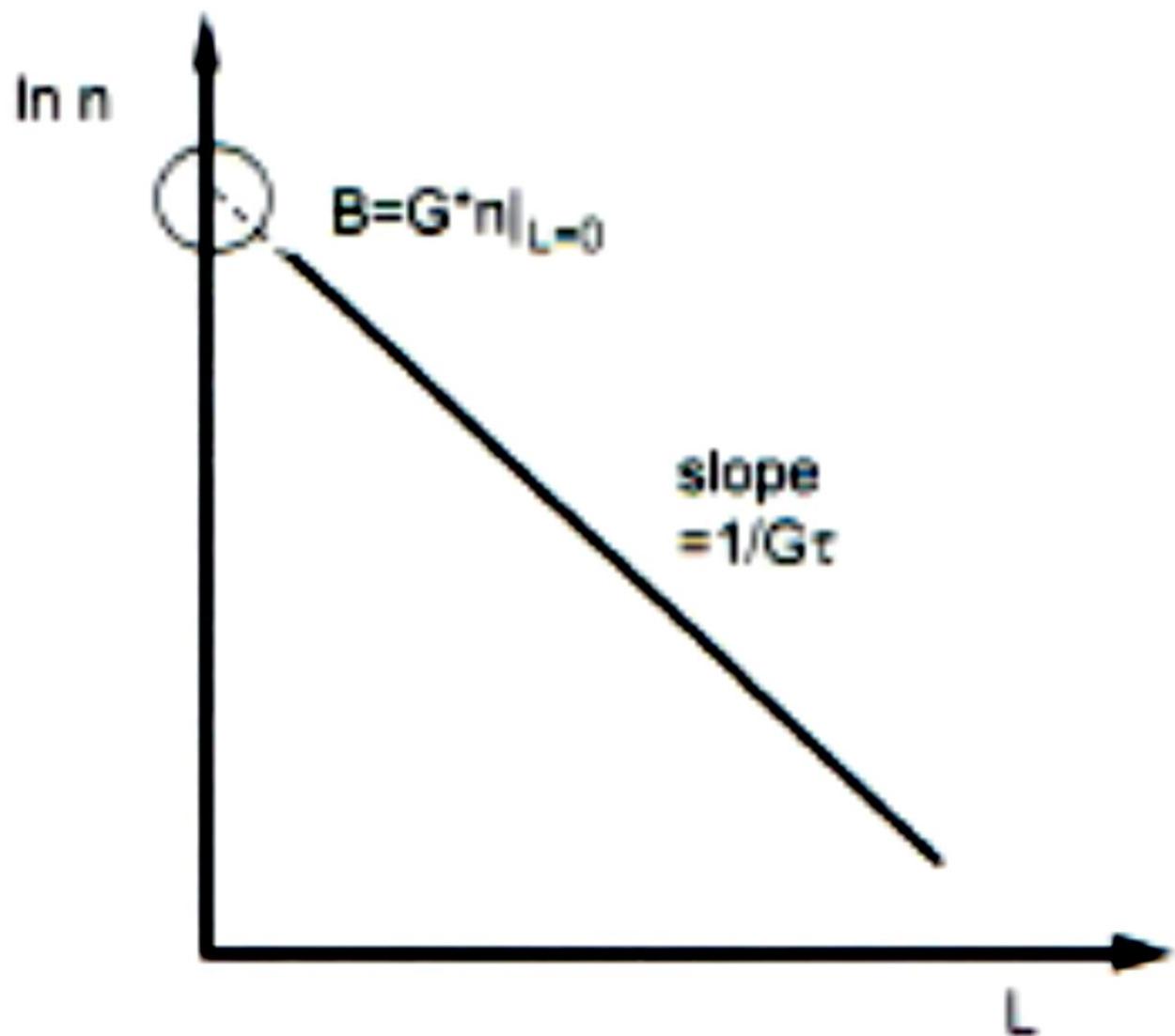
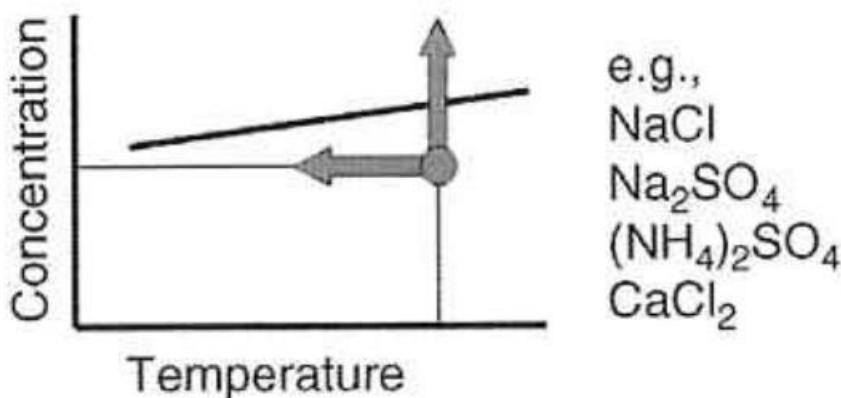


Figure 7.2 Theoretical population density plot for a steady state MSMR crystallizer operating at the following conditions:  
 - no secondary nucleation other than at zero size  
 - no attrition other than at zero size  
 - no crystal breakage  
 - no agglomeration  
 - no growth dispersion  
 - crystal growth rate is independent of size.

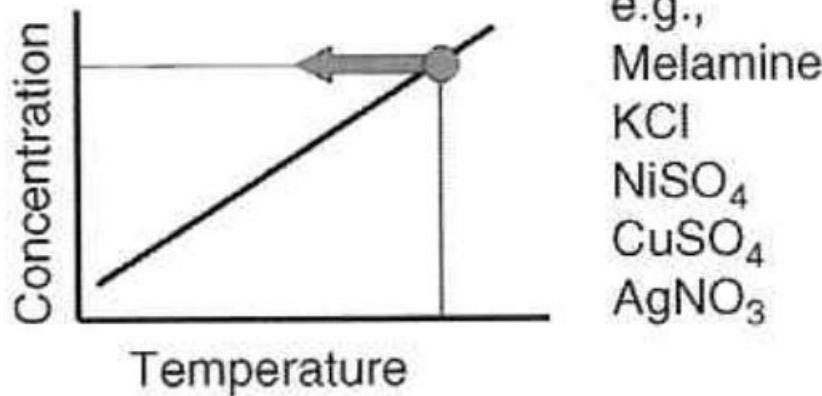


## Evaporation

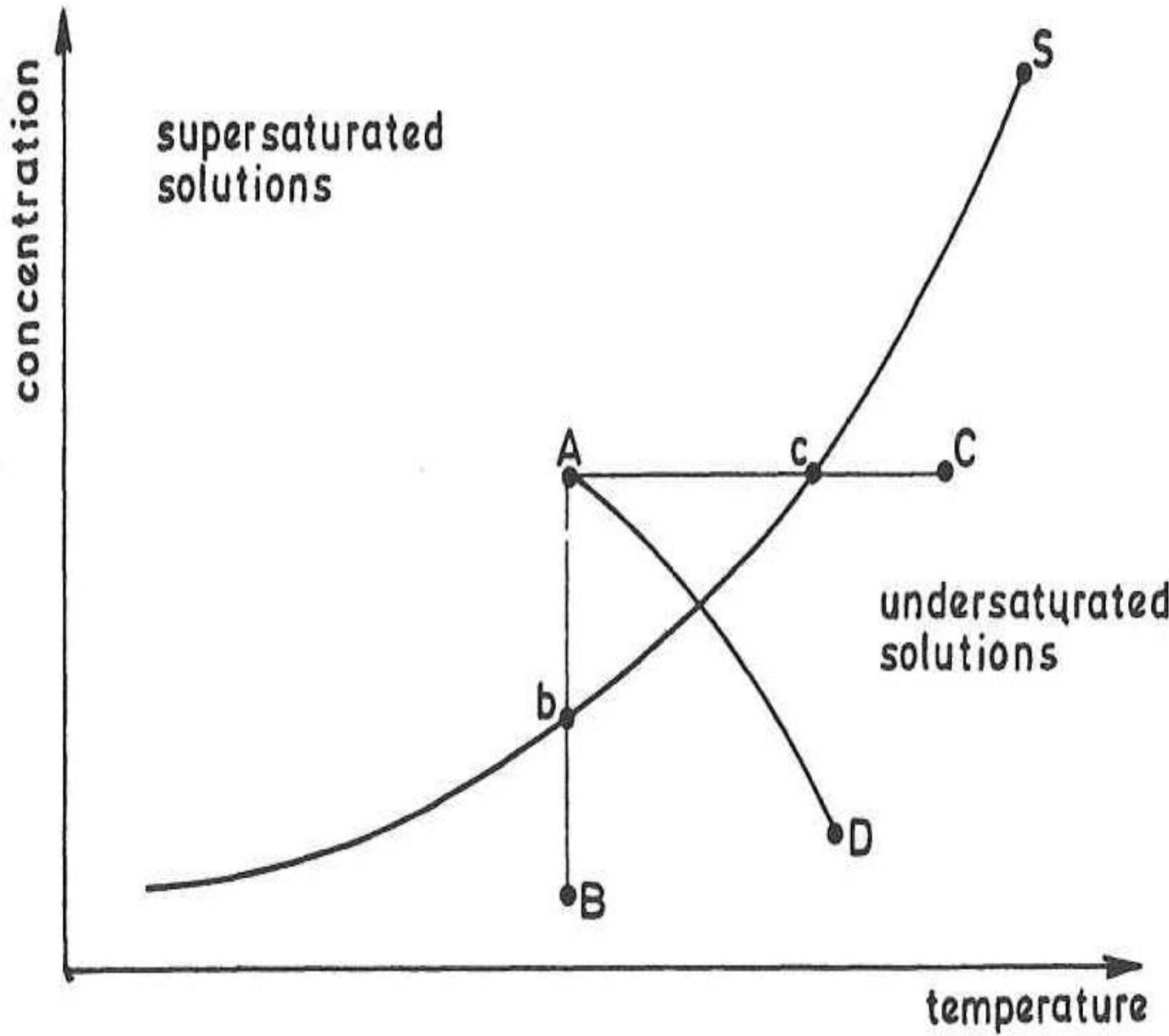


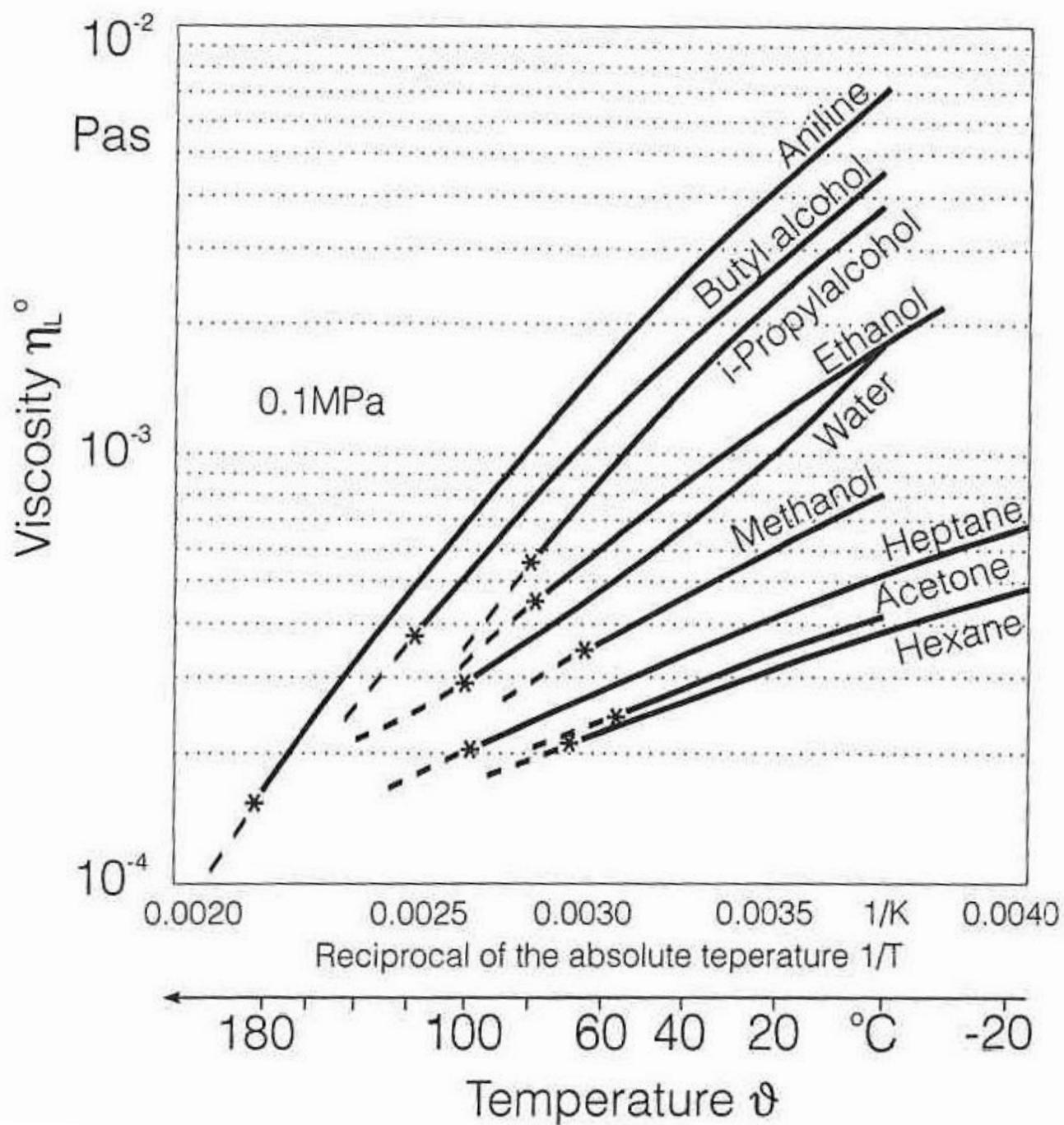
e.g.,  
 $\text{NaCl}$   
 $\text{Na}_2\text{SO}_4$   
 $(\text{NH}_4)_2\text{SO}_4$   
 $\text{CaCl}_2$

## Cooling

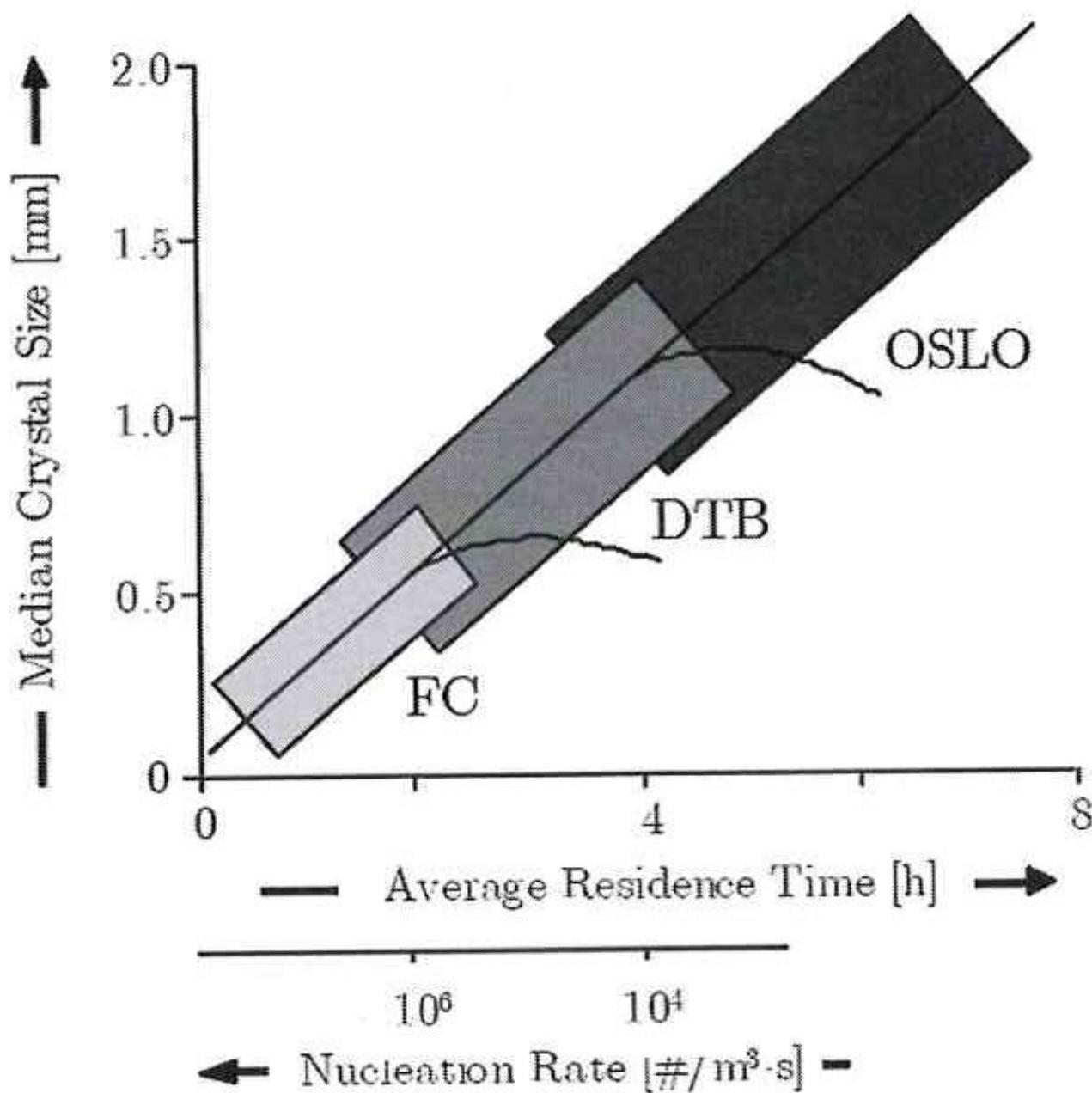


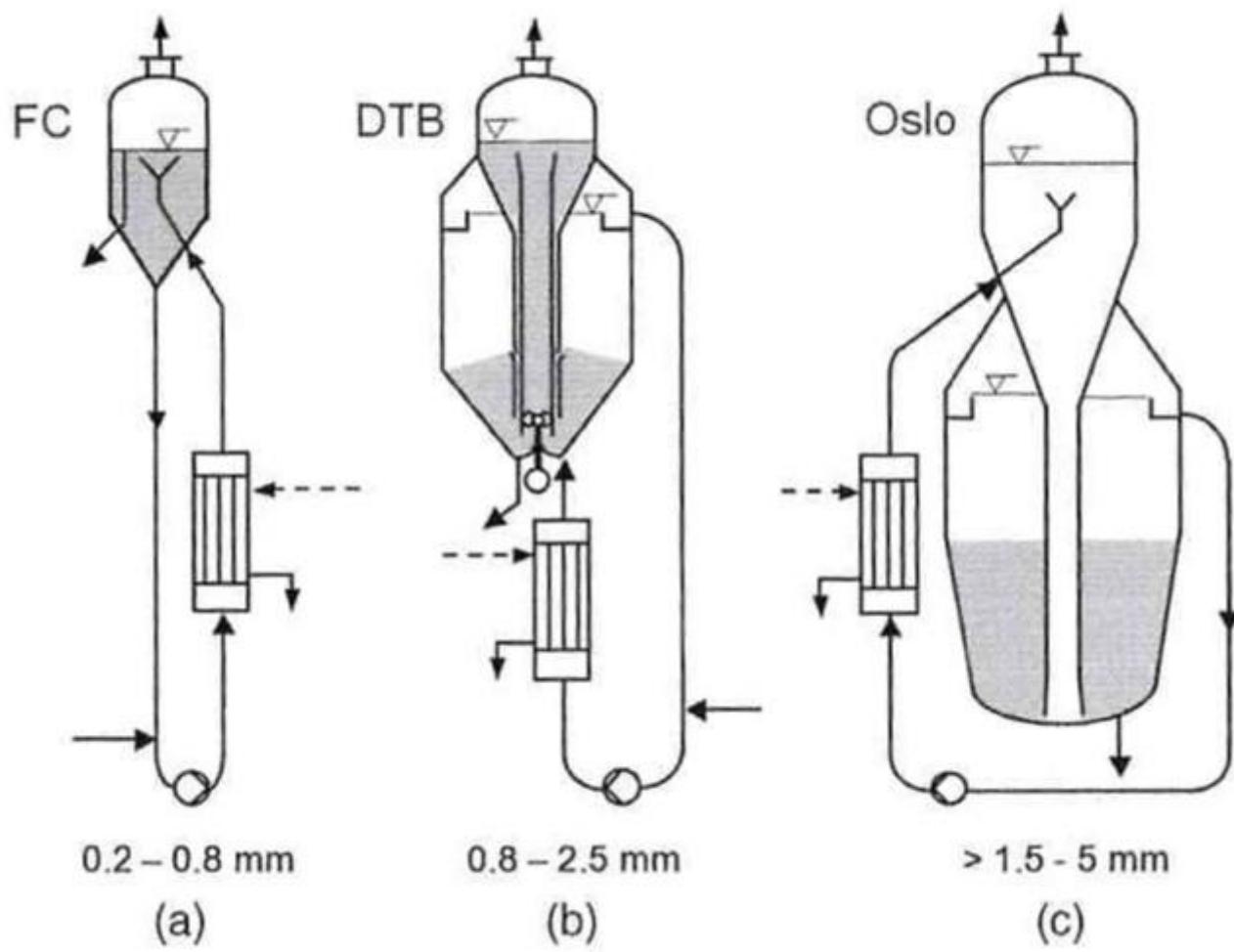
e.g.,  
Melamine  
 $\text{KCl}$   
 $\text{NiSO}_4$   
 $\text{CuSO}_4$   
 $\text{AgNO}_3$

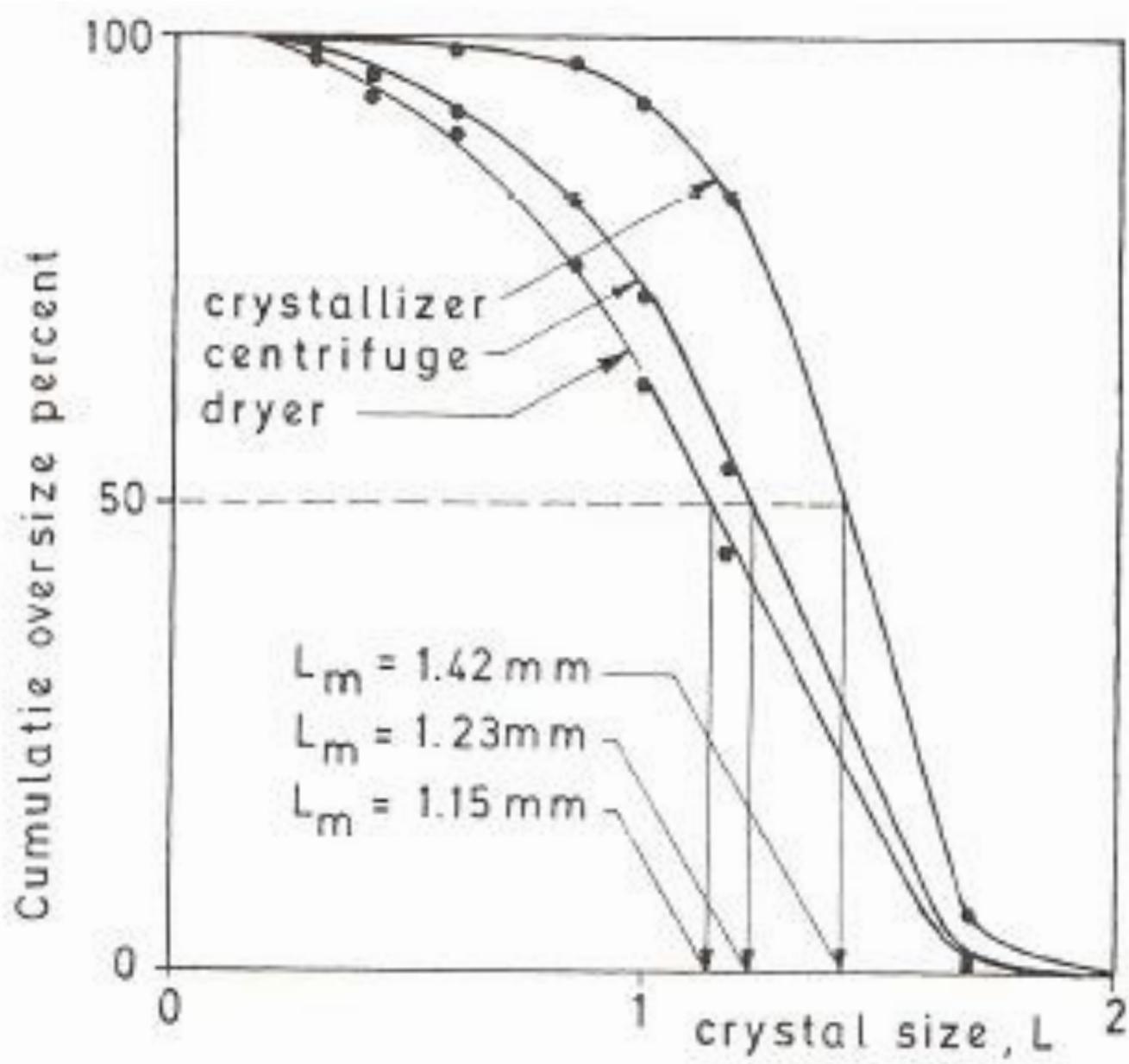




FC crystallizers:	0.2-0.8 mm
DTB crystallizers:	0.8-2.5 mm
Oslo crystallizers:	1.5-5 mm

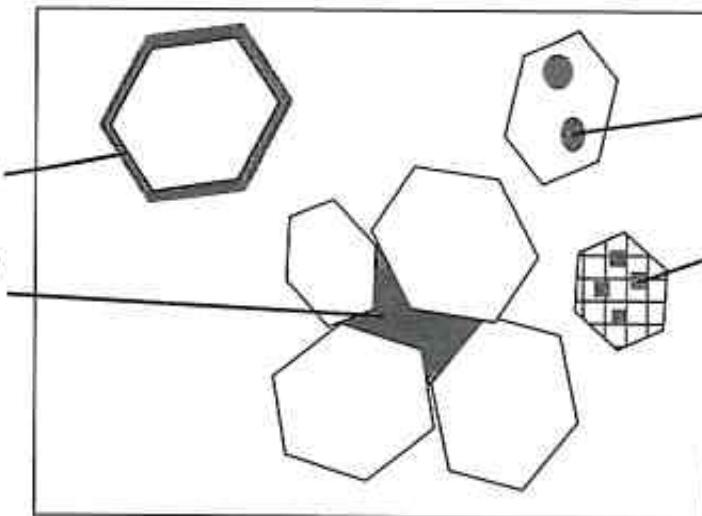






Surface adhesion/adsorption

Bulk phase inclusion of mother liquor



Liquid inclusions in the crystal

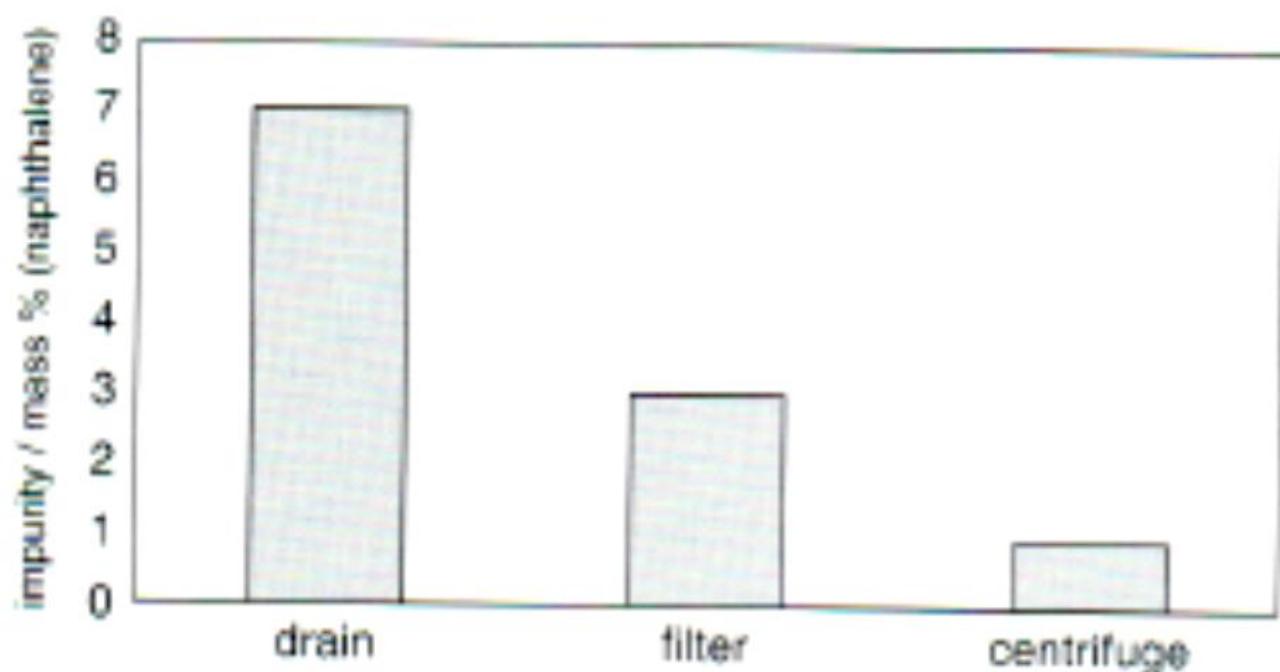
Lattice incorporation  
→ substitutional or interstitial solid solutions/mixed crystals  
→ non-equilibrium lattice incorporation at defect sites

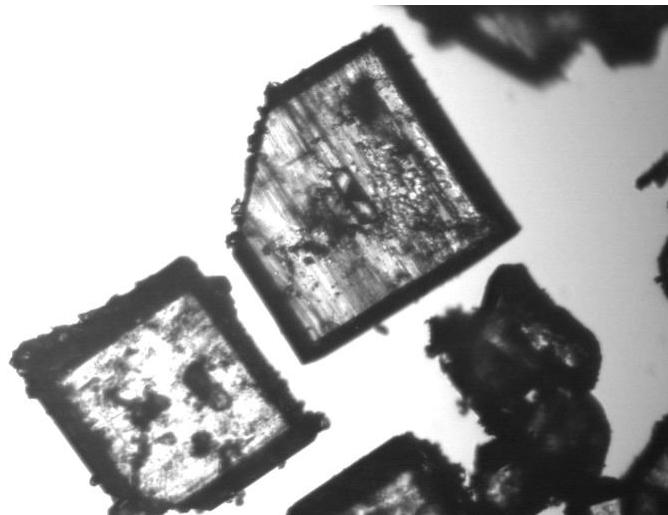
**Figure 7.1** Location of impurities in a crystalline product after solid–liquid separation. The growing crystal itself can incorporate impurities either in the lattice on a molecular level or as three-dimensional faults, liquid

inclusions (right). In addition, the crop can contain impurities via mother liquor, either adsorbed on the crystals or entrapped between crystals (left).

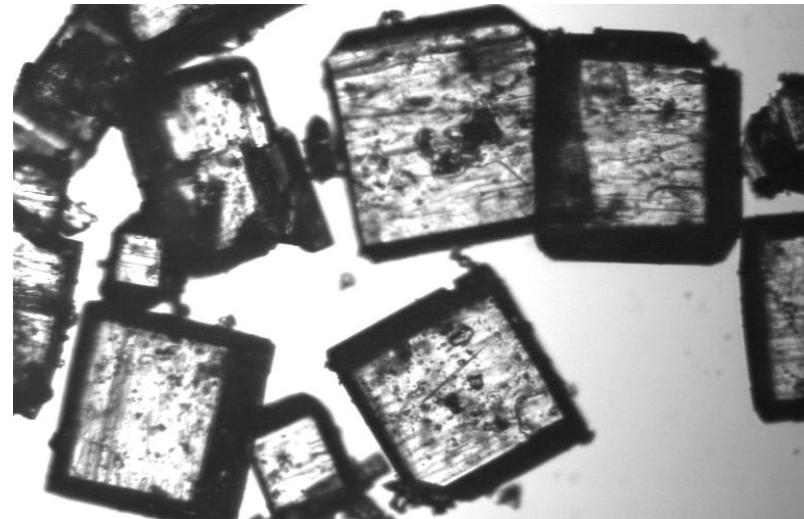
**Residual moisture content related to the solid (wt%)**

Sedimentation	20–40
Filtration	8–18
Centrifugation	4–8

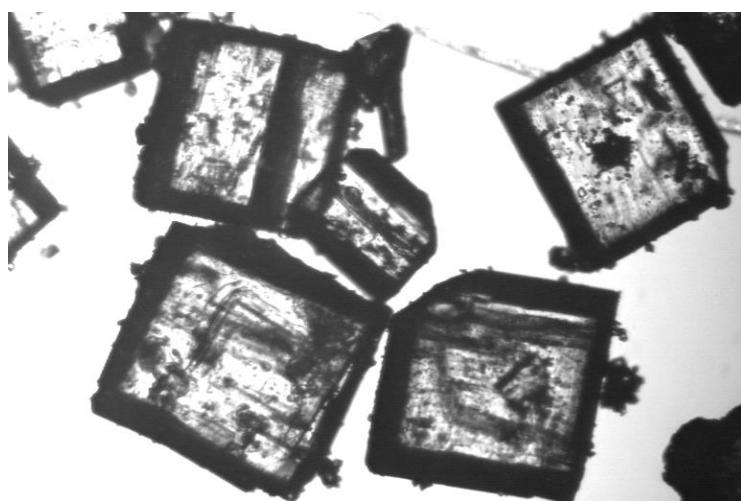




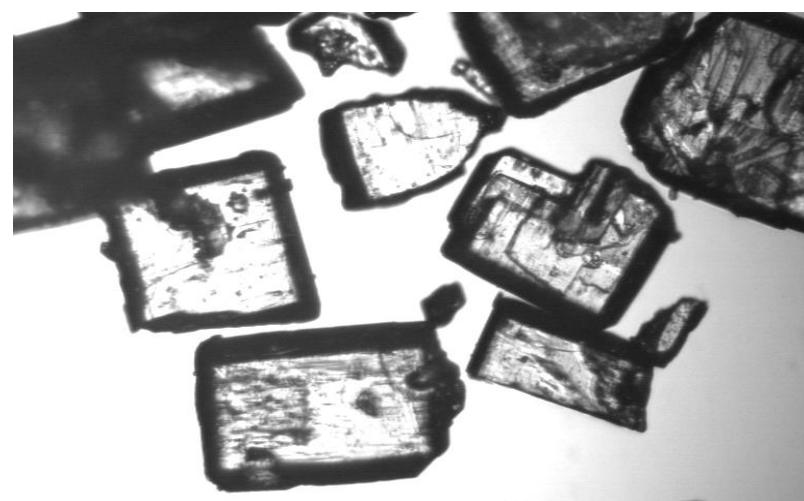
Ethanol



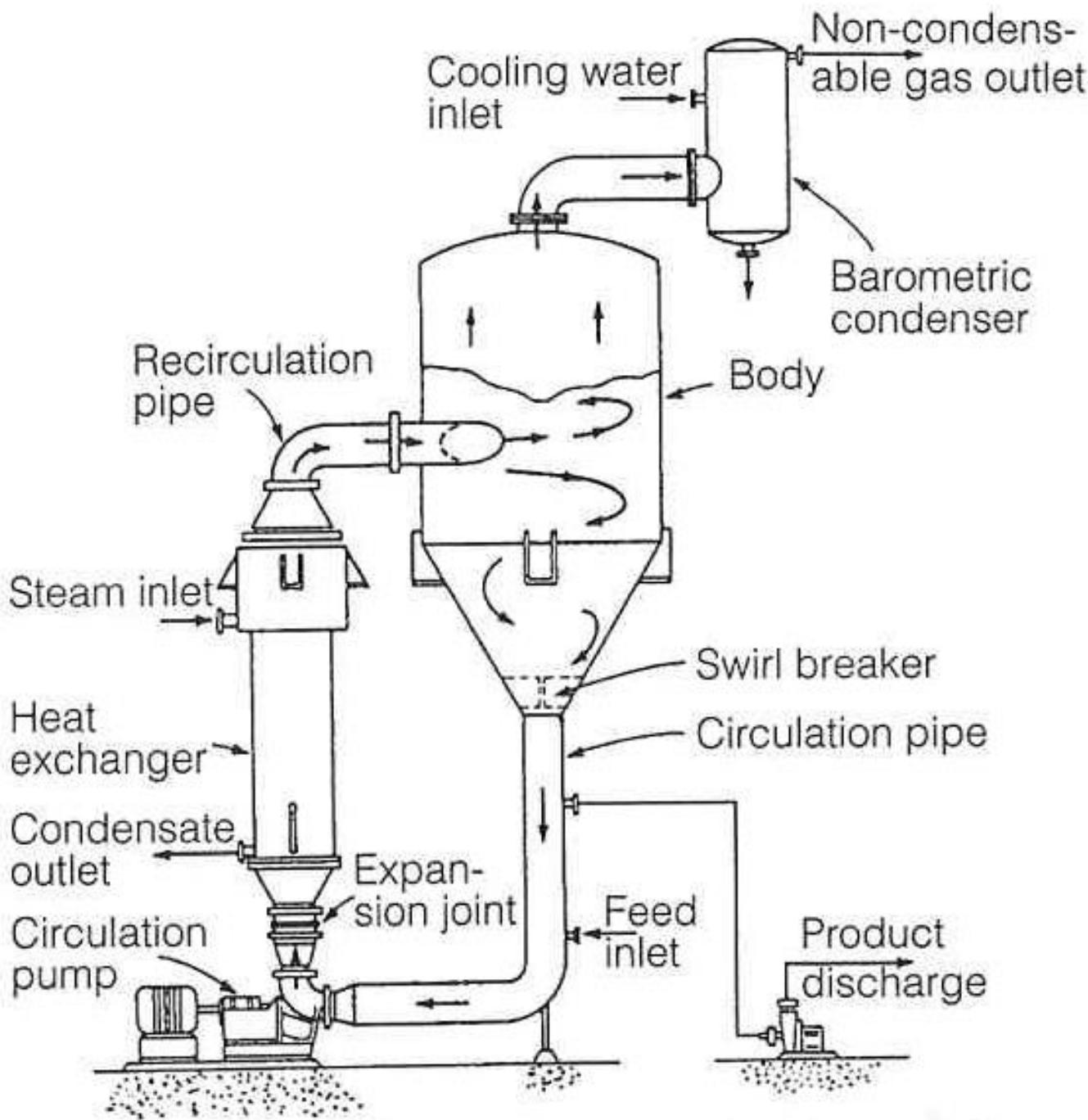
Methanol



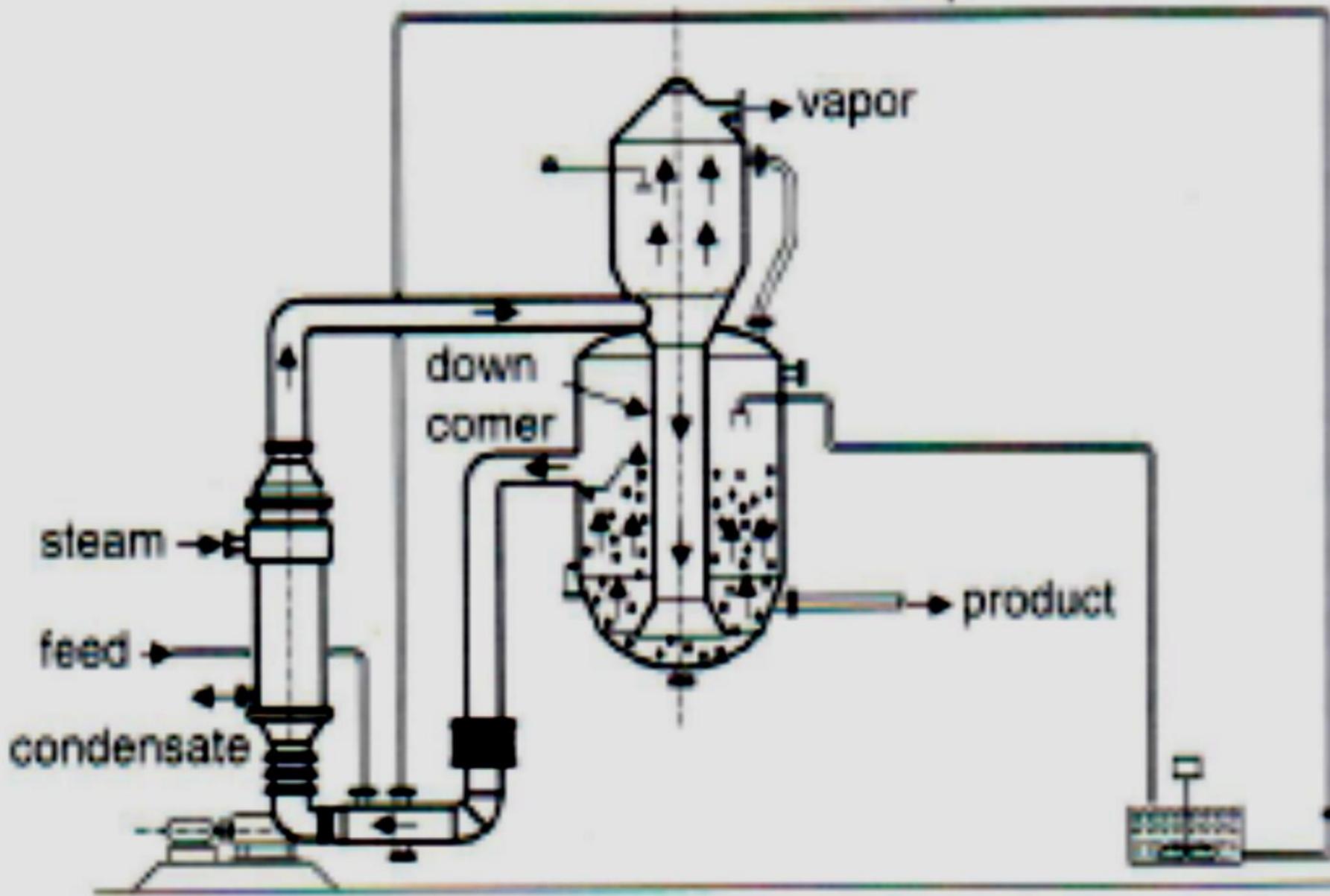
Propanol

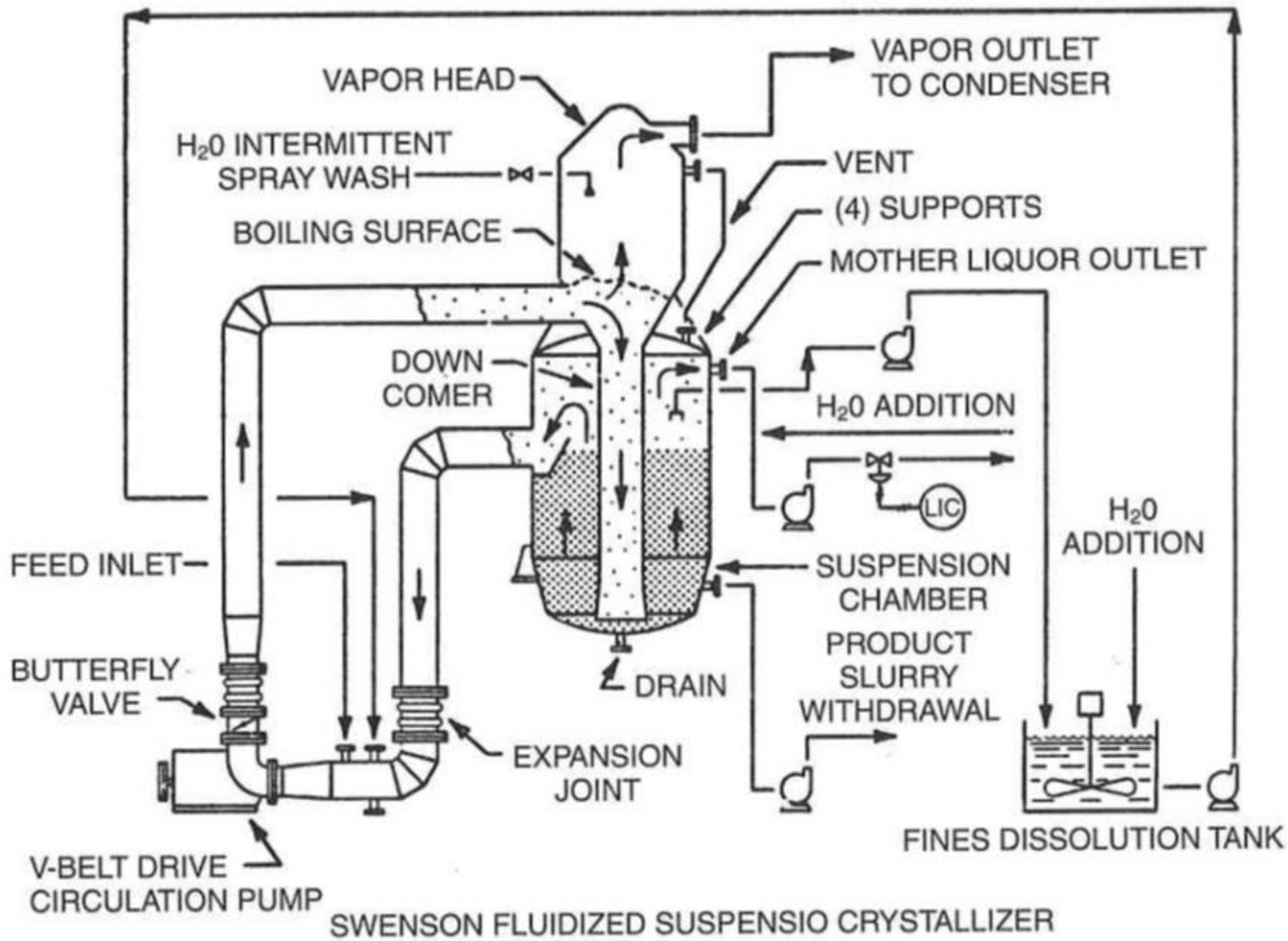


Water



fines loop



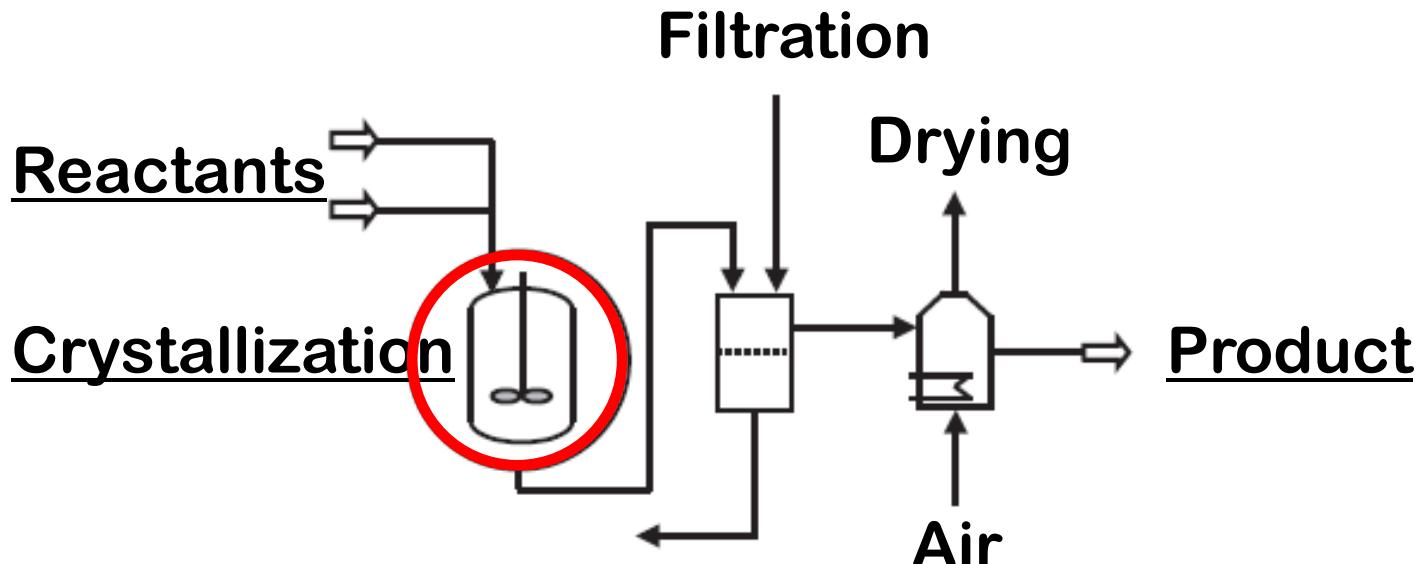


$$\Delta C = 0.4 - 0.6 \Delta C_{\text{met}}$$

$m_T = 10 - 30$  mt% crystals in suspension

$k_G = f(T, \dots)$  Target: T high

# Crystallization Process



Aims: Product *quality & quantity*

- purity
- morphology + CSD
- flowability, shelf life,...
- maximum yield
- efficiency (materials, energy...)

Thermodynamically stable phases of organic and inorganic substances depend on:

---

- Temperature
  - Pressure
  - surrounding media:
    - air (relative humidity)
    - solvent (solubility)
  - additional: mechanical stress (e.g. grinding)
- **A change of these parameters often leads to metastable modifications**

## **Yield**

- mass growth rates decrease
    - decreasing yield
  - loss of charges
- 
- mass growth rates can increase?
  - expanded metastable zone width
    - higher supersaturations?
  - prevent scaling?

## **Product Quality**

- crystal habit changes
    - filtration, transport and storage problems
    - useless product
  - undesired crystal size distribution
- 
- directed crystal modifying
    - special applications
  - “tailor-made”-additives

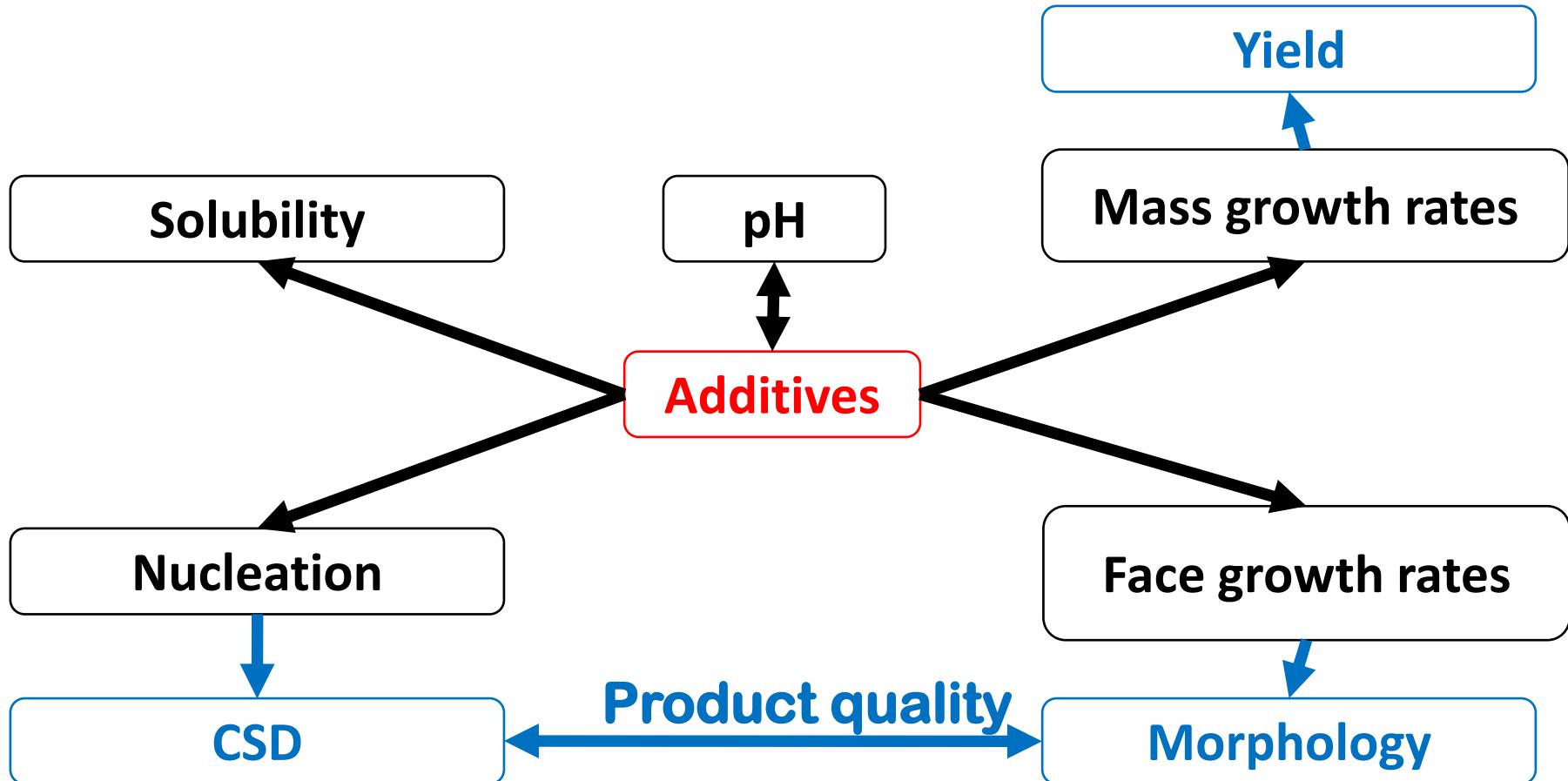
# Aim of crystallization processes

---

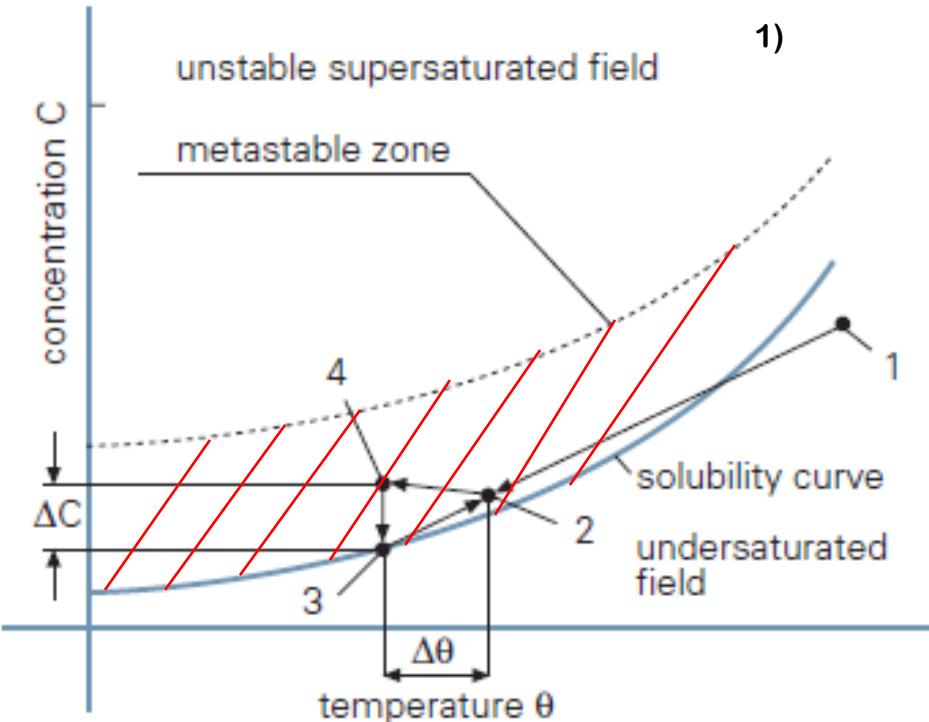
The crystallization process includes the determination of:

- Purification
- Particle size (distribution)
- Modification (polymorph / solvates)
- Shape design
- Lower costs (reduction of number of steps)

# Effects of additives – An Overview



# Crystallization Process – A closer look



*Metastable zone width (MZW):*

- zone for industrial crystallizations
- no primary homogeneous nucleation
- secondary nucleation → control of CSD

*Supersaturation σ „driving force“*

- $\sigma$  should not exceed MZW
- maximized for maximum growth rate

**Where can additives affect the crystallization process?**

# Tools in crystallization

---

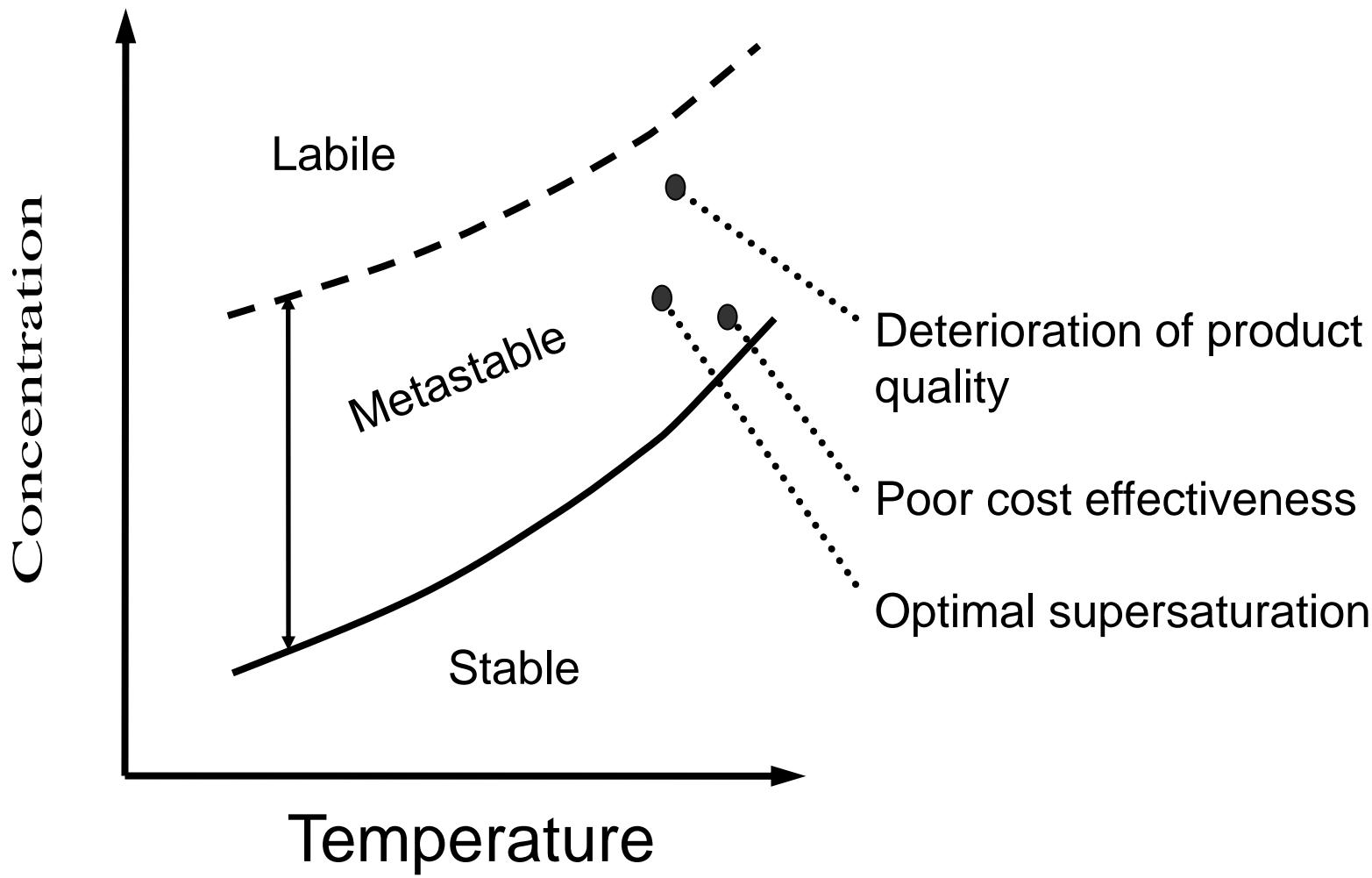
## ❖ Thermodynamics:

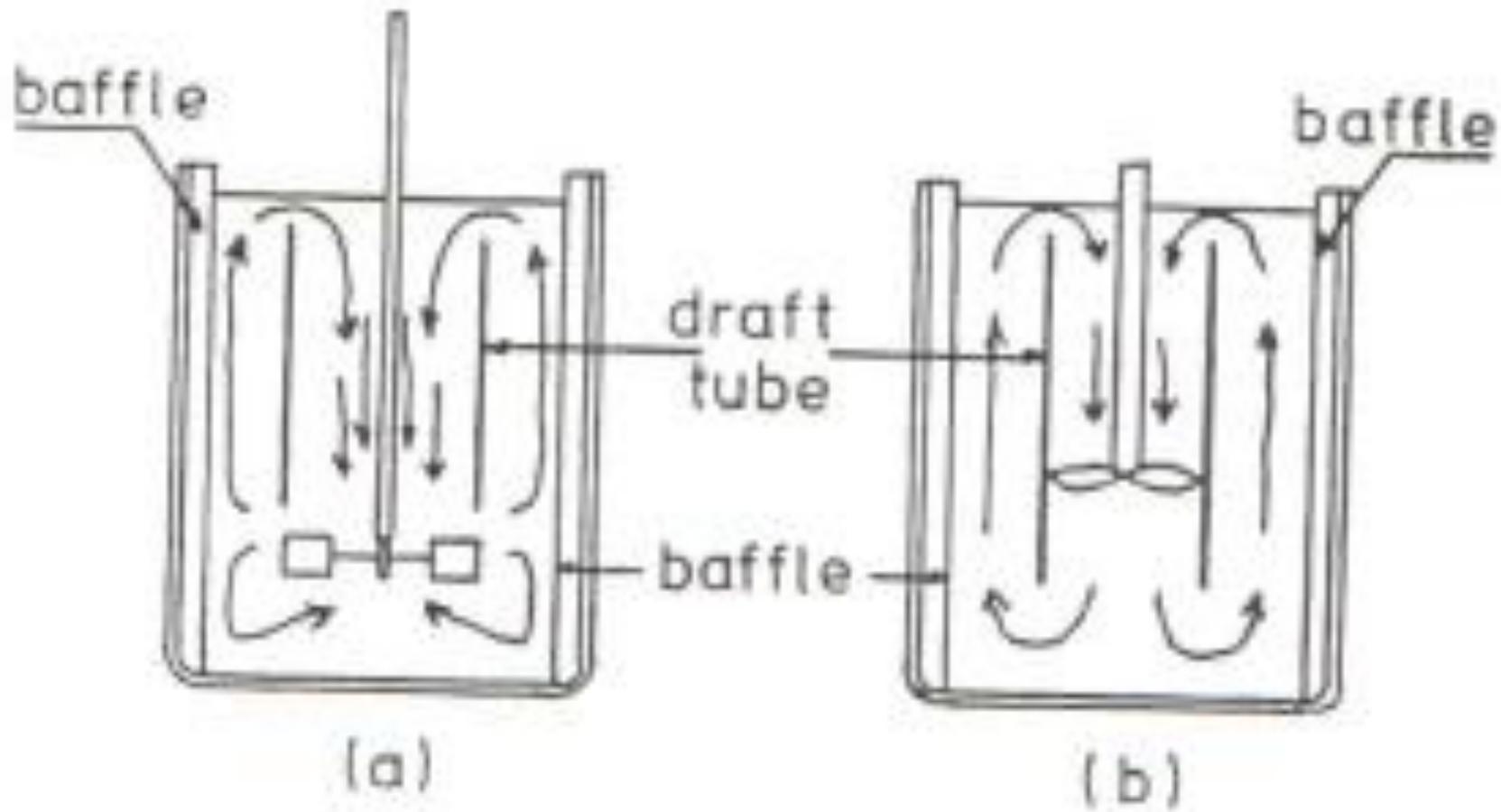
- Driving force (program)
- Phase diagram

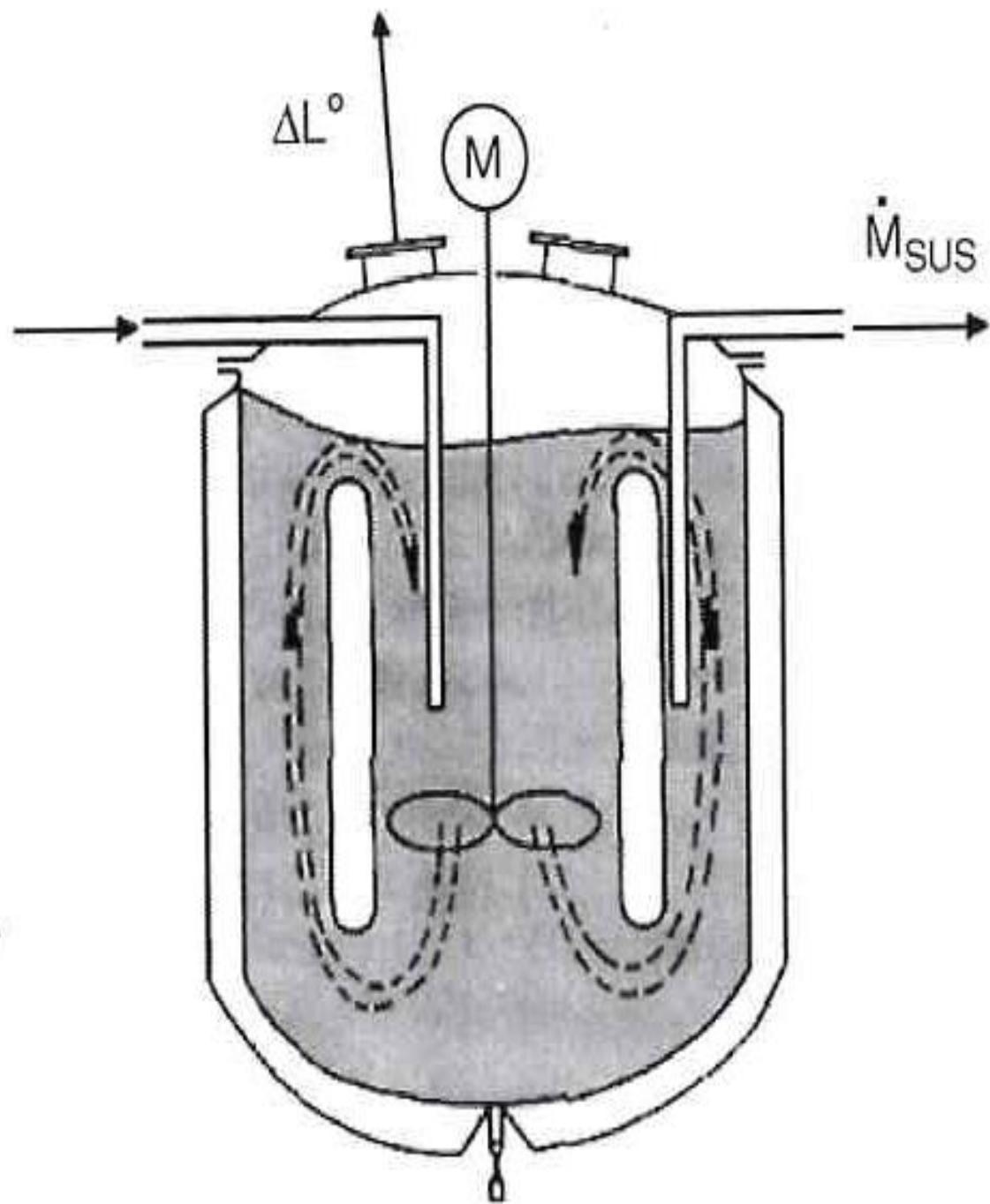
## ❖ Kinetics:

- Nucleation (place, how, when)
- Retention time
- Impurities

# Metastable zone







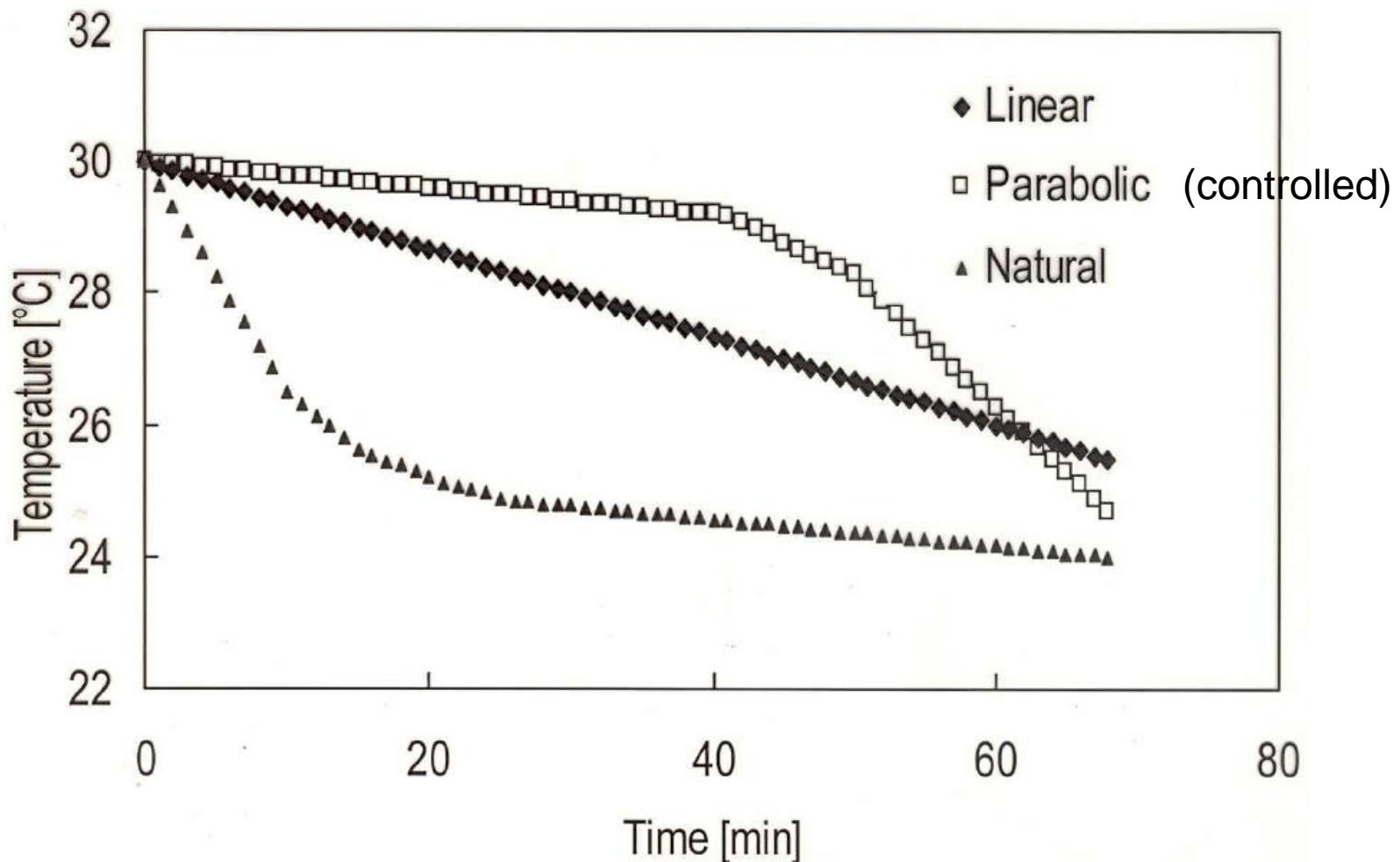
# Batch crystallization

- How to control ?
  - cooling profiles
  - seeding

<b>Classification</b>	<b>Cooling rate (K/h)</b>
<b>Slow</b>	<b>1-5</b>
<b>Realistic</b>	<b>5-10</b>
<b>Fast</b>	<b>10-15</b>
<b>Crash</b>	<b>&gt; 15</b>

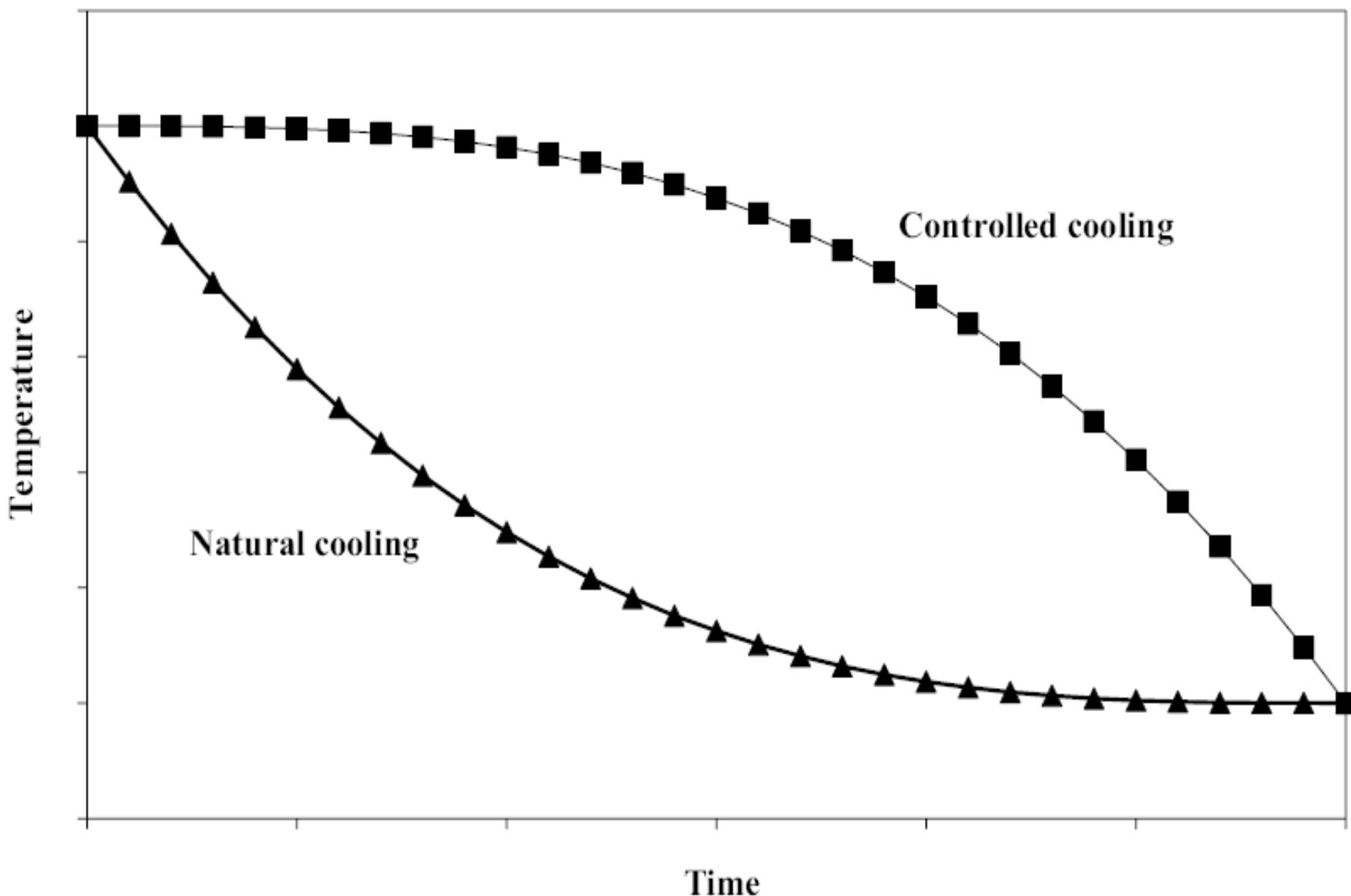
# Cooling profiles

for supersaturated  $K_2SO_4$ -solutions in a seeded batch-crystallizer



# Cooling profiles

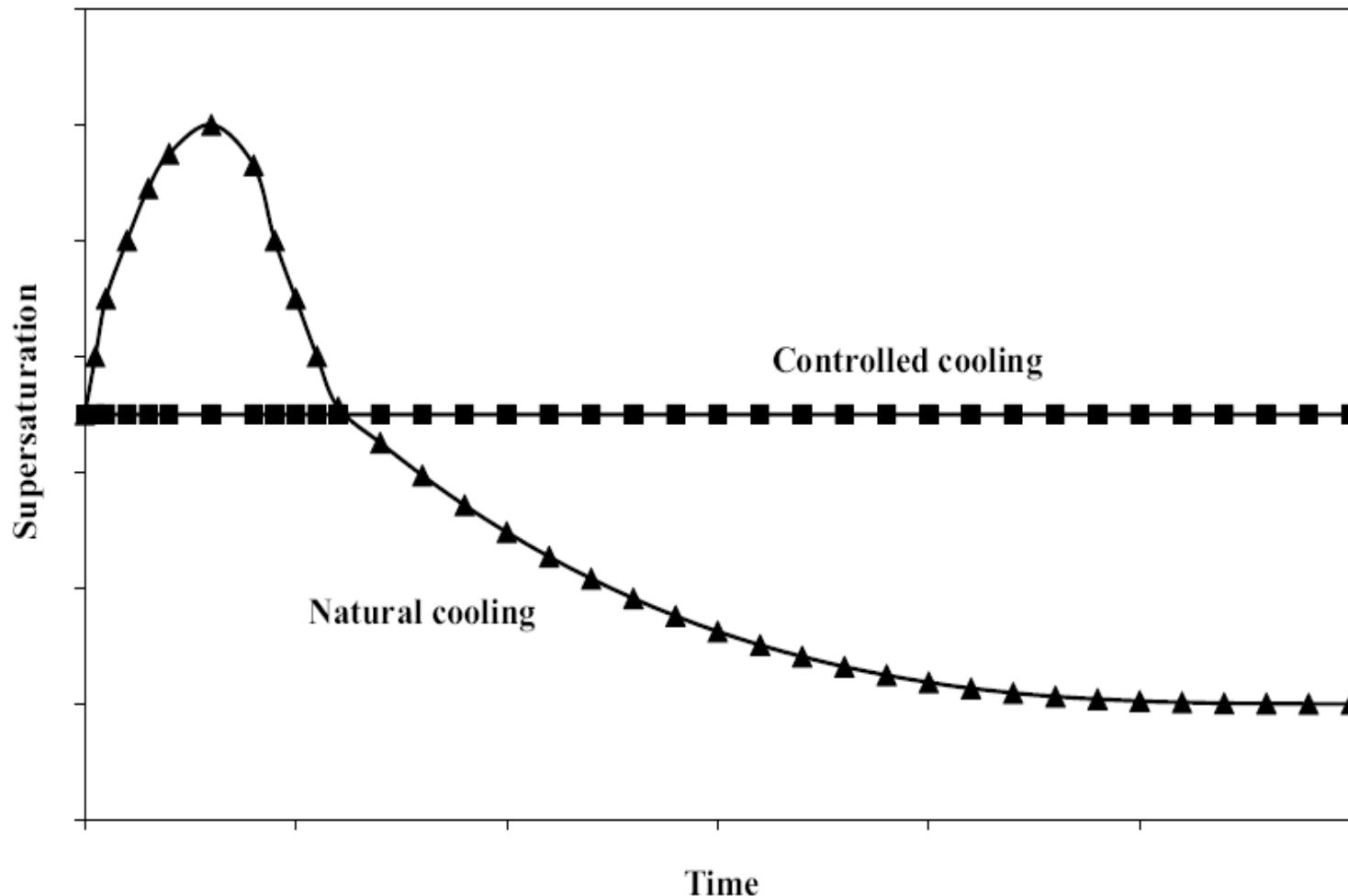
temperature profiles at natural and controlled cooling in batch crystallization



# Cooling profiles

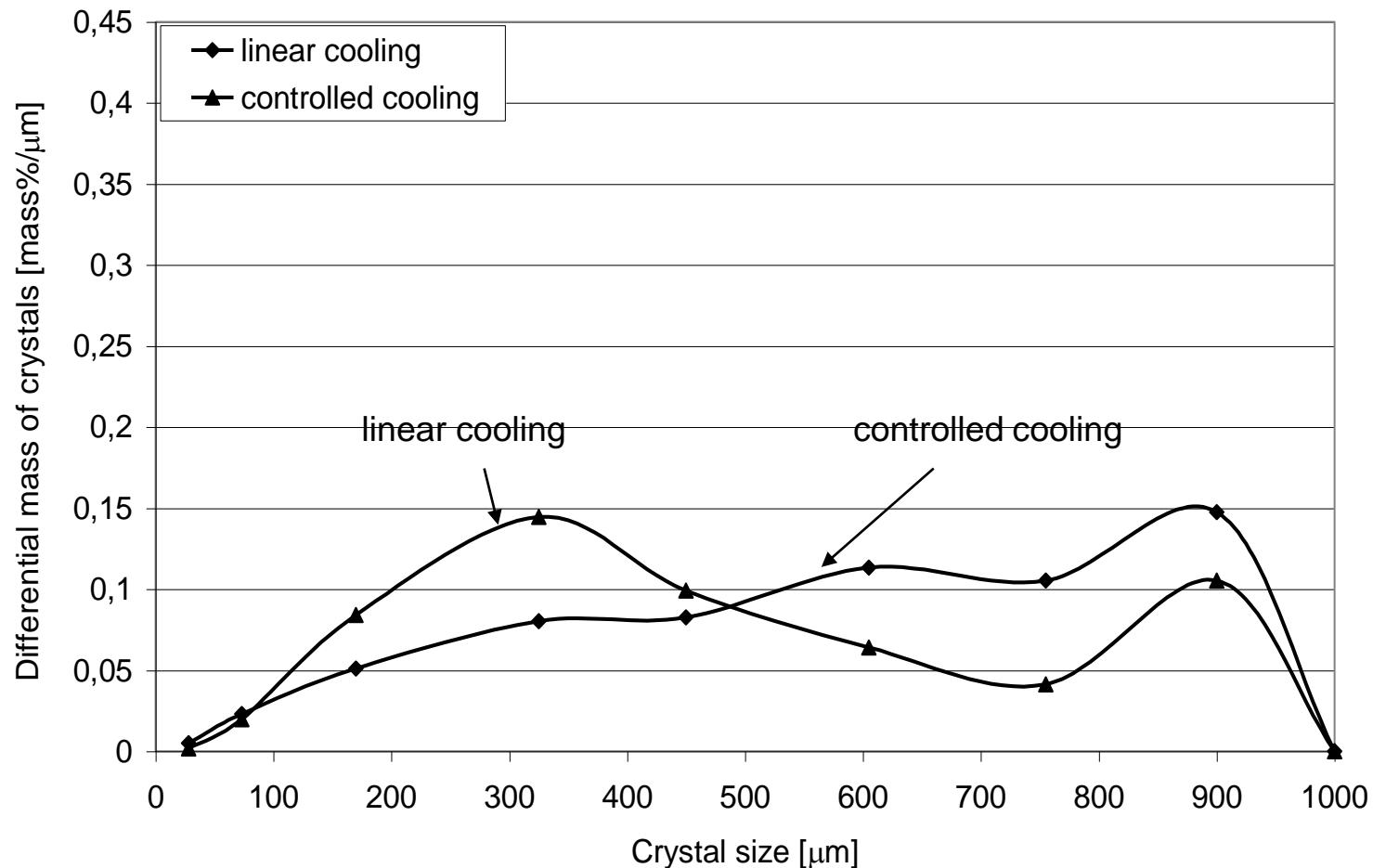
supersaturated profiles at natural and controlled cooling in batch crystallization

---



# Example

Crystal size distribution obtained for different cooling programs without seeding



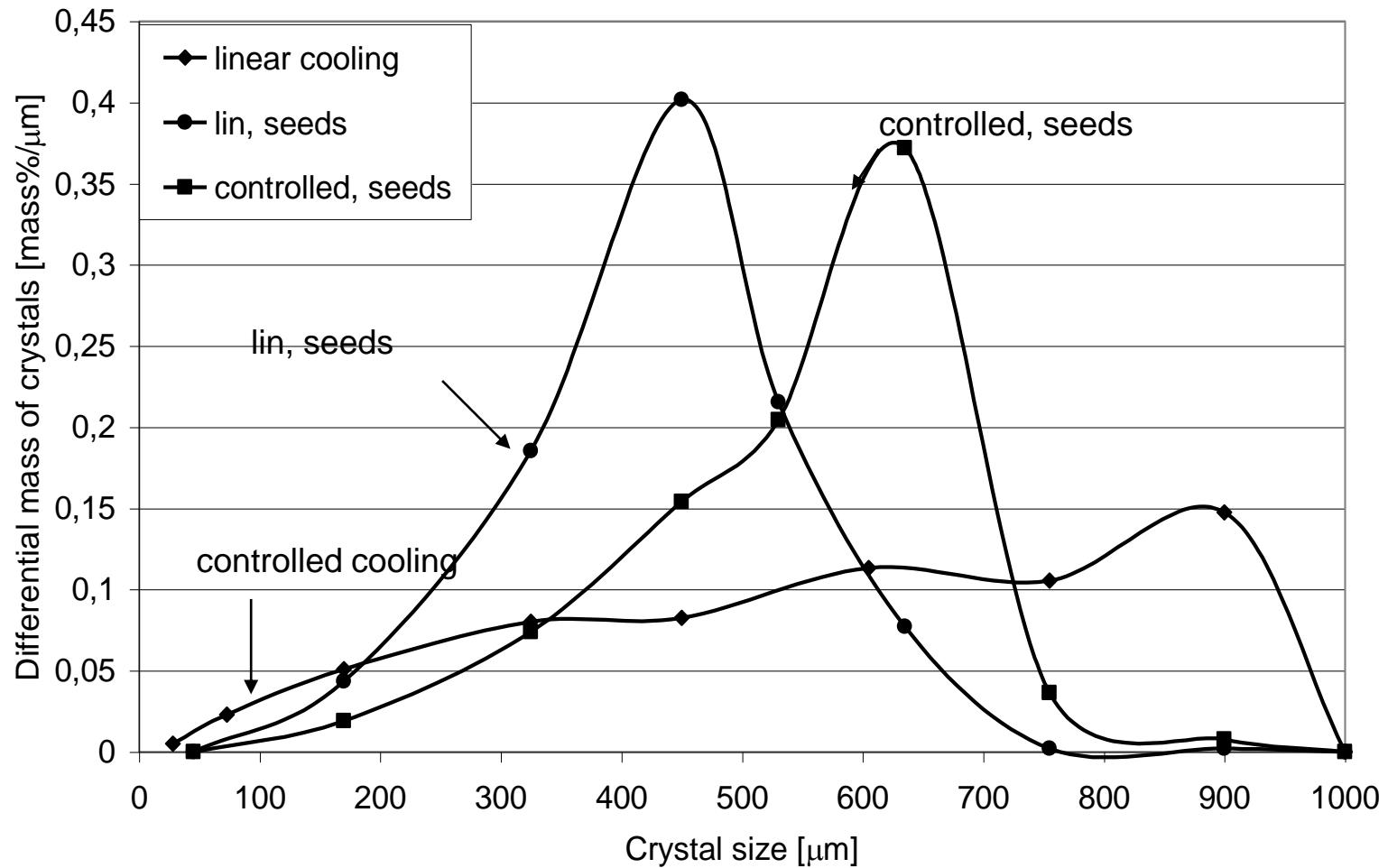
# Example seeding (batch process)

---

- When – at what supersaturation
- How: - seed mass
  - seed size distribution
  - seed quality
- Supersaturation maintaining / changing profile

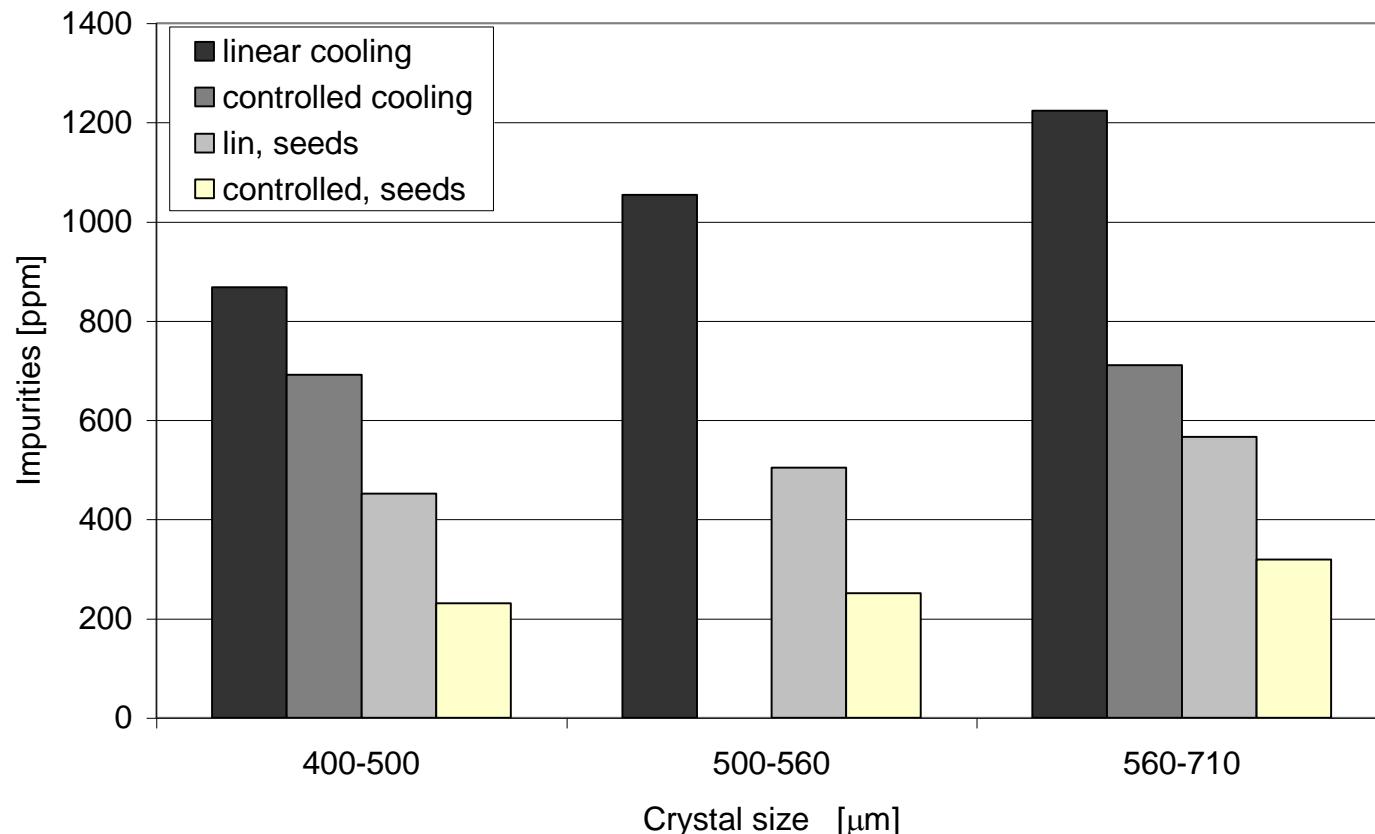
# Example seeding (batch process)

Crystal size distribution: a) different cooling programs, b) with and without seeding



# Example seeding (batch process)

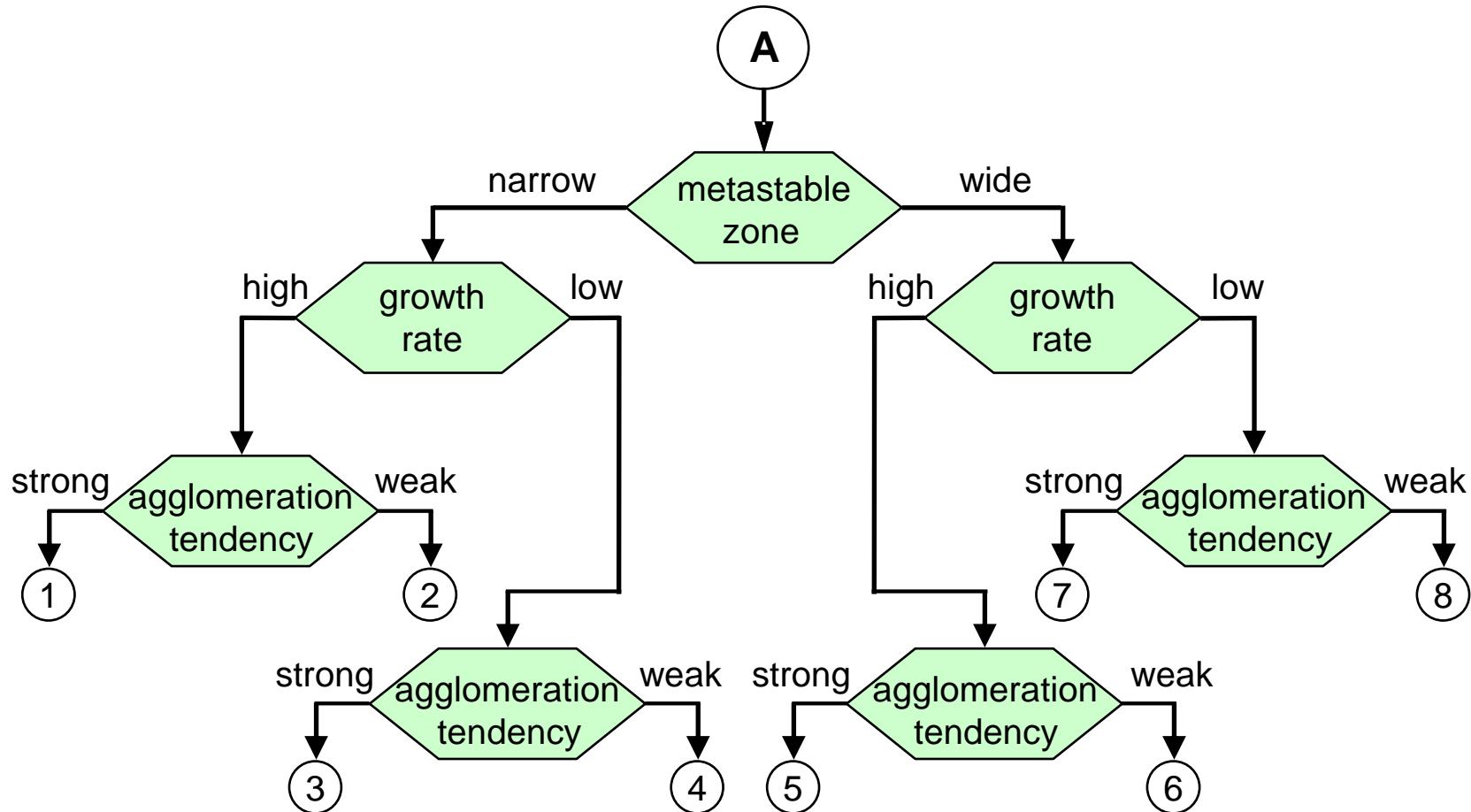
## Water content in crystals for different size classes



# Example

## seeding (batch process)

- Decision tree; target value „unimodal crystal size distribution and purity“ [2]

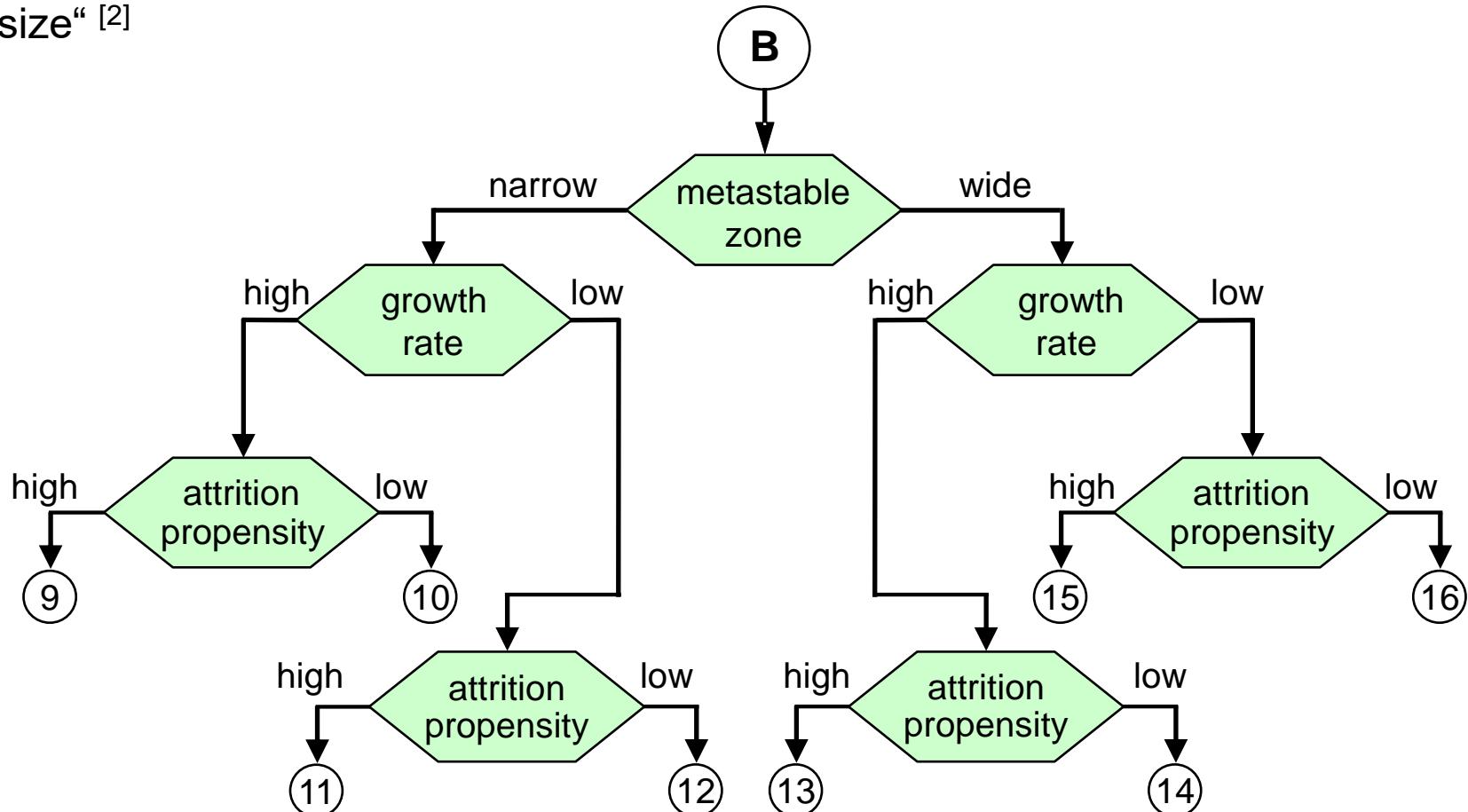


[2] Warstat, A.: *Heuristische Regeln zur Optimierung von Batch-Kühlungskristallisationsprozessen*, PhD-thesis, Martin-Luther-Universität Halle-Wittenberg, online-publication: <http://sundoc.bibliothek.uni-halle.de/dissonline/06/07H060/index.htm>, 2006.

# Example

## seeding (batch process)

- Decision tree; target value „unimodal crystal size distribution and specific crystal size“ [2]



[2] Warstat, A.: *Heuristische Regeln zur Optimierung von Batch-Kühlungskristallisationsprozessen*, PhD-thesis, Martin-Luther-Universität Halle-Wittenberg, online-publication: <http://sundoc.bibliothek.uni-halle.de/dissonline/06/07H060/index.htm>, 2006.

Thank you for your  
attention!

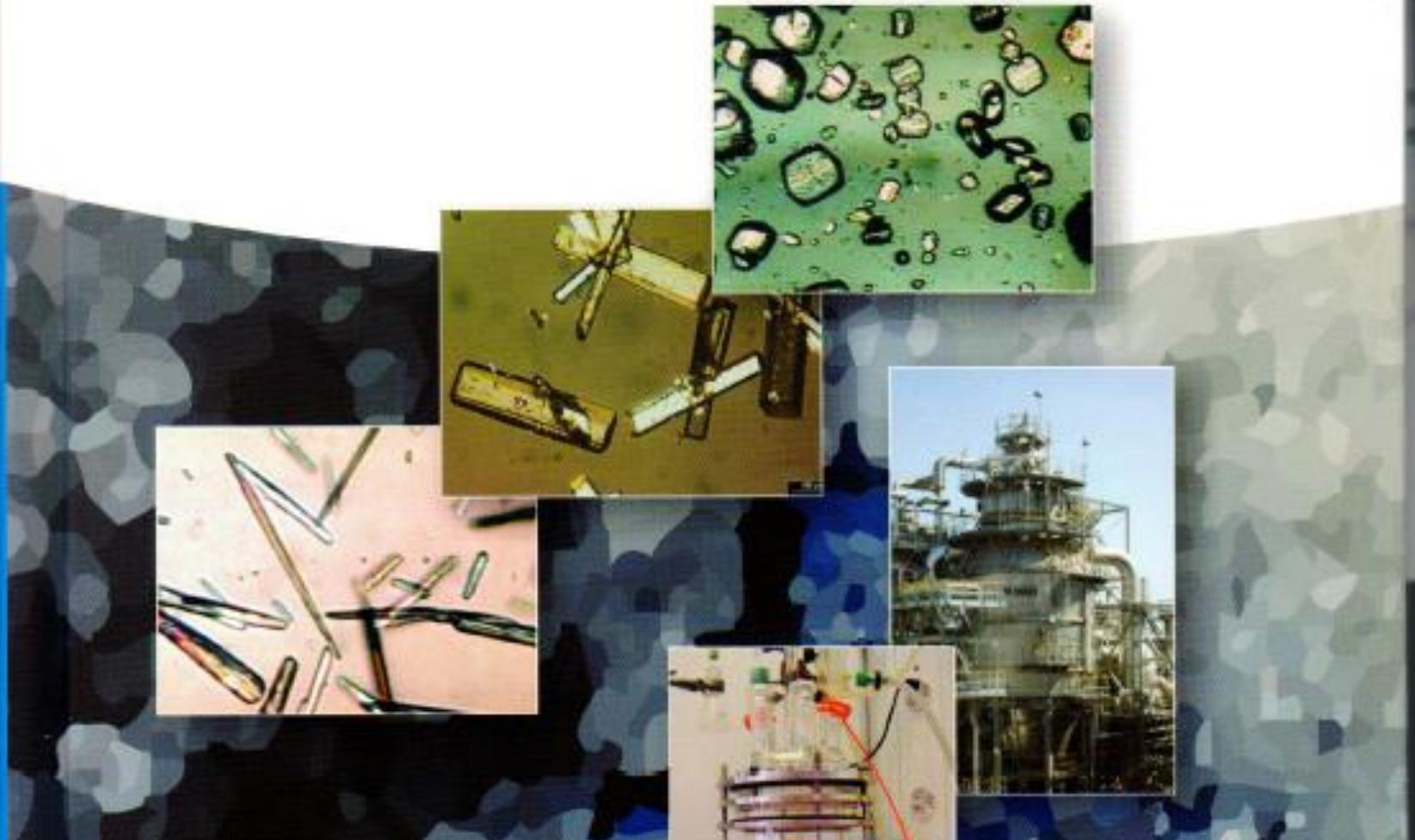
# **Handbook of Industrial Crystallization**

Edited by  
Allan S. Myerson,  
Deniz Erdemir and  
Alfred Y. Lee

**THIRD EDITION**

# Crystallization

Basic Concepts and Industrial Applications



# Industrial Crystallization

S. J. JANČIĆ

and

P. A. M. GROOTSCHOLTEN

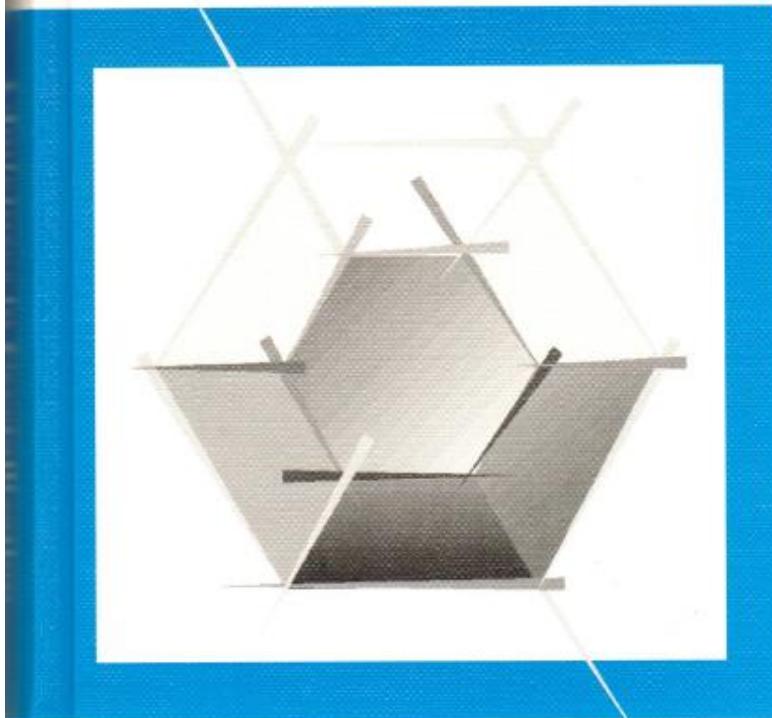
*Delft University of Technology, Laboratory for Process Equipment,  
Delft, The Netherlands*

Delft University Press



Jaroslav Nývlt, Joachim Ulrich

# Admixtures in Crystallization



**CRYSTALLIZATION**

*Second Edition*

**TECHNOLOGY**

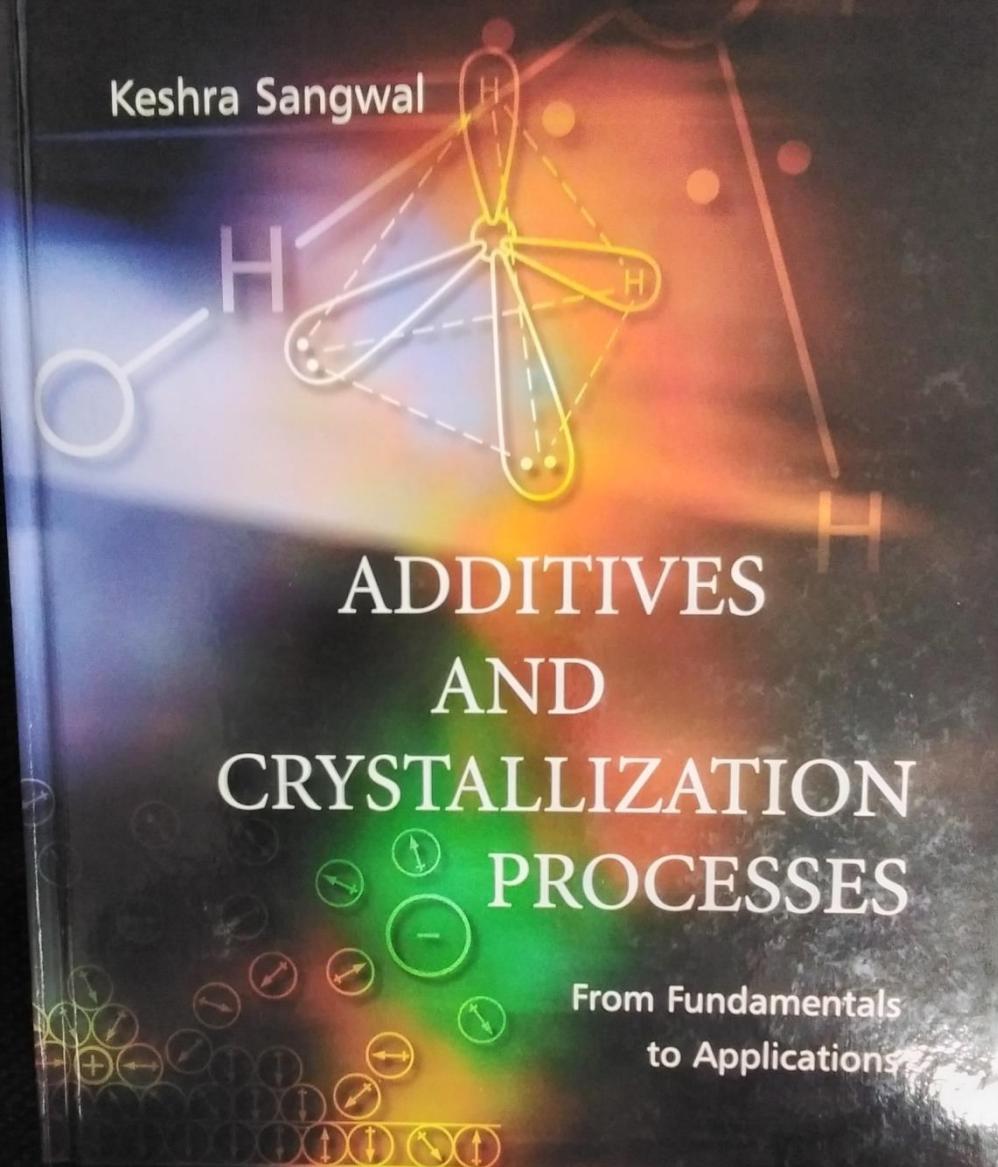
*Revised and Expanded*

**HANDBOOK**

*edited by*

**A. Mersmann**

Keshra Sangwal



# ADDITIVES AND CRYSTALLIZATION PROCESSES

From Fundamentals  
to Applications

WILEY

# **Science and Technology of Crystal Growth**

**J.P. van der Eerden and  
O.S.L. Bruinsma (Eds.)**

Kluwer Academic Publishers

Thank you for your  
attention!

Martin Luther University Halle-Wittenberg  
Center of Engineering Science  
Department of Thermal Separation Processes



# Protein Crystals

-more questions than answeres-

---

Prof. Dr. Dr. h.c. Joachim Ulrich

# Crystals

---

“Crystals are solids in which the atoms are arranged in a periodic repeating pattern that extends in three dimensions.

While all crystals are solids, not all solids are crystals.

Materials that have short-range rather than long-range ordering, like glass, are non-crystalline solids.

A non-crystalline solid is often referred to as an amorphous solid” [MYE02].

# Polymorphism, Hydrates, Solvates

---

Grant [GRA99, Loh06] defines *polymorphism, amorphous solids and solvates* as:

“**Polymorphism** is often characterized as the ability of one drug substance (chemical compound) to exist in two or more crystalline phases that have different arrangements and/or conformations of the molecules in the crystal lattice”.

“**Solvates** are crystalline solid adducts containing either stoichiometric or nonstoichiometric amounts of a solvent incorporated within the crystal structure. If the incorporated solvent is water, the solvates are also commonly known as ***hydrates***”.

---

Grant, D.J.W., Theory and Origin of Polymorphism, In: Polymorphism in Pharmaceutical Solids, edited by Harry G. Brittain, Marcel Dekker Inc., New York, 1999, 1-34, ISBN: 0-8247-0237-9.

Lohani, S., Grant, D.J.W., Thermodynamics of Polymorphs, In: Polymorphism in the Pharmaceutical Industry, edited by Rolf Hilfiker, Wiley-VCH, Weinheim, 2006, 21-41, ISBN: 978-3-527-31146-0.

# Phase diagrams

---

“A phase diagram graphically represents (in two or three dimensions) the equilibria between various phases of a system in a wide range of temperature, pressure and concentration/composition.

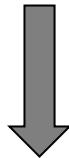
It specifies the equilibrium conditions ( $T$ ,  $p$  and  $x$ ) and the corresponding phase present at this state.

Thus, in case of SLE, the phase diagram also tells about the solid phases occurring in a system, such as polymorphs, solvates or intermediate compounds” [LOR13].

# Introduction

## protein crystallization

special characteristics of protein crystallization<sup>1), 2)</sup>



multi-component system  
complexity / diversity

**often restricted crystallization conditions**  
(limited solubility, limited risk of denaturation, loss of activity)

**very big supersaturation required**

(temperature, buffer pH, solvent composition, crystallizing agent e.g.  
salt, nucleation)

(macromolecules, asymmetry)

**crystal lattice**

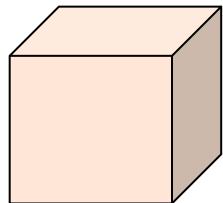
(large number of contacts between the molecules, crystal channels)

<sup>1)</sup> McPherson A.: Crystallization of biological macromolecules; *Cold Spring Harbor Laboratory Press, Cold Spring* 1998.

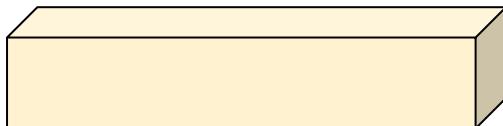
<sup>2)</sup> Banga A.K.: Therapeutic peptides and proteins; second edition, *CRC Press* 2006.

# production conditions of different lysozyme crystal morphologies

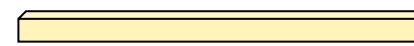
Tetragonal<sup>5)</sup>



HTO<sup>5)</sup>



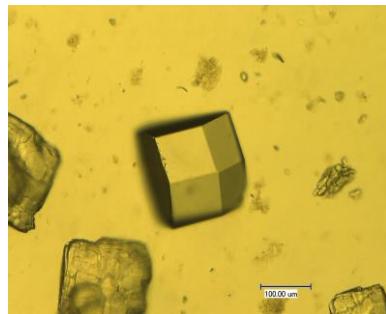
LTO<sup>5)</sup>



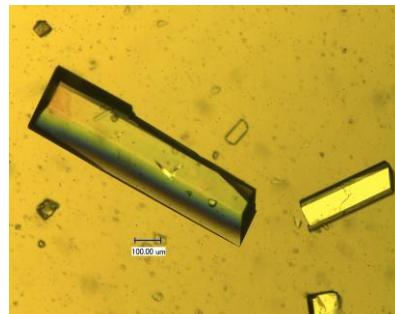
Low Temperature Orthorhombic

High Temperature Orthorhombic

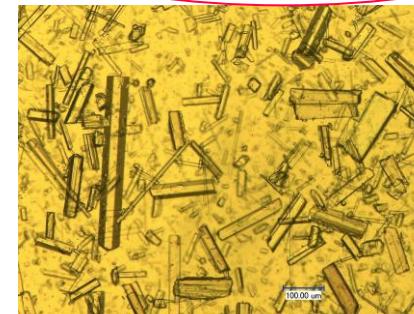
acetate buffer pH5,  
50 mg/mL,  
4 wt% NaCl, 4 °C



acetate buffer pH5,  
115 mg/mL,  
6 wt% NaCl, 37 °C



glycine buffer pH9.6,  
50 mg/mL,  
4 wt% NaCl, 20 °C



→ different crystallization conditions → different lysozyme crystal morphologies

<sup>5)</sup> AlDababihbeh, N. *PhD Thesis*, Department of Chemical & Biological Engineering, Illinois Institute of Technology, 2010.

# analysis of lysozyme crystals

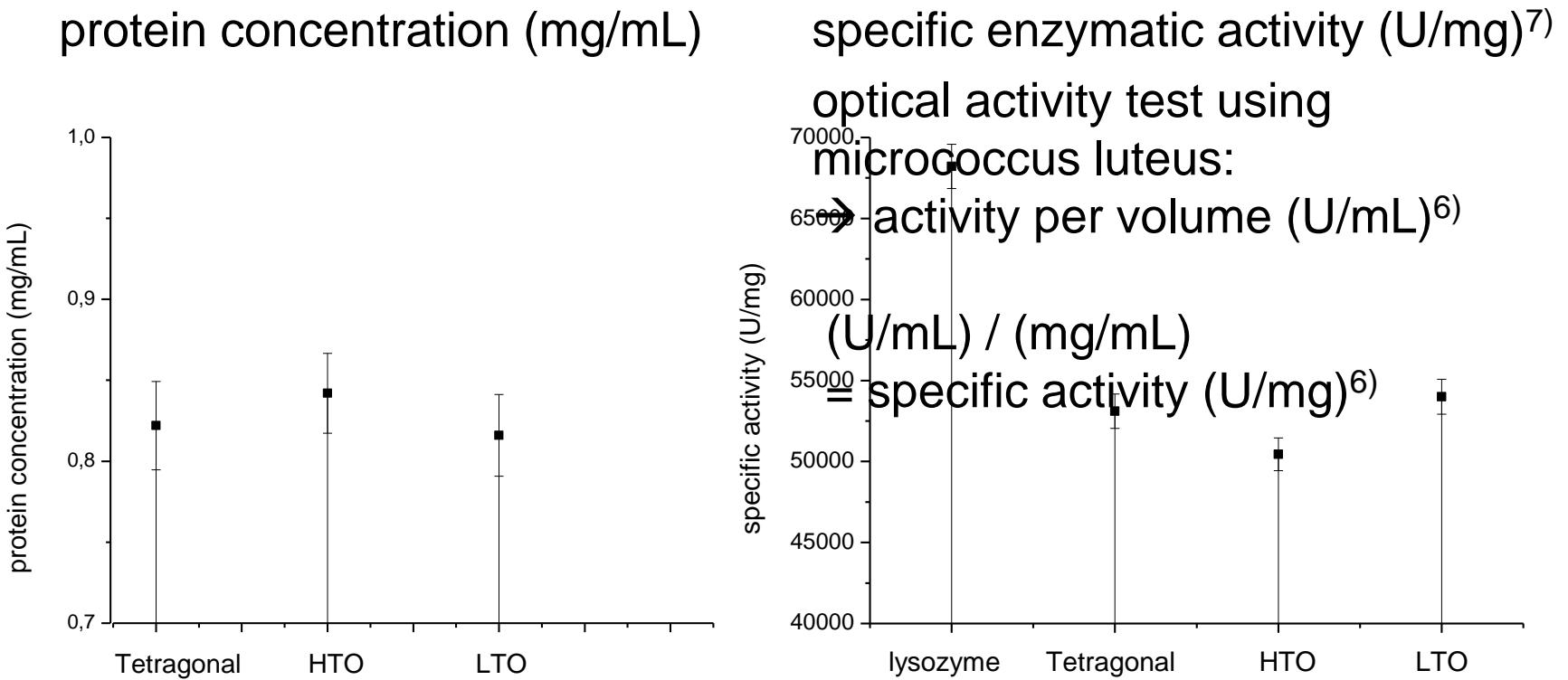
## 4 main components

---

- protein concentration
- 1) lysozyme (protein)
  - activity
  - XRPD (powder x-ray diffraction)
- 2) buffer solution (high solvent content)
  - dyeing / coloring
  - pH
- 3) free + bound water (solvent content)
  - TGA (thermo gravimetric analysis)
- 4) NaCl (crystallizing agent)
  - conductivity
  - silver nitrate (precipitation)
  - EDX (energy dispersive x-ray spectroscopy)
  - XRPD

# 1) lysozyme (protein)

protein concentration + enzymatic activity



→ highest protein content: HTO > Tetragonal > LTO

→ specific activity: LTO > Tetragonal > HTO

<sup>6)</sup> Löffler G.: *Basiswissen Biochemie*, 5. Auflage, Springer 2003

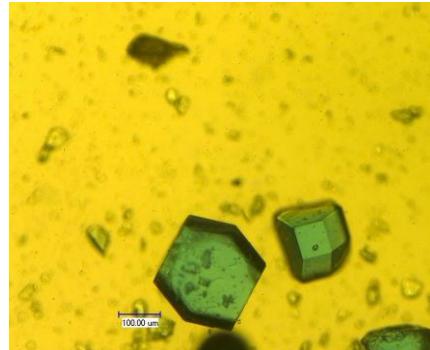
<sup>7)</sup> Shugar D.: *Biochimica et Biophysica Acta* 8 (1952) 302-309

## 2) buffer solution (free water) dyeing / coloring

Tetragonal, HTO and LTO lysozyme crystals

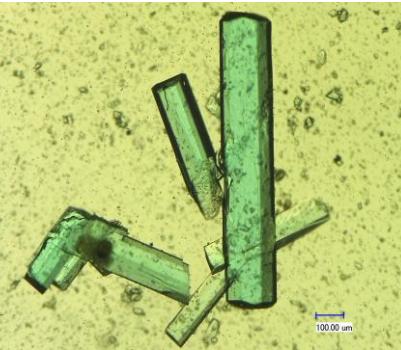
+ methylene blue

Tetragonal

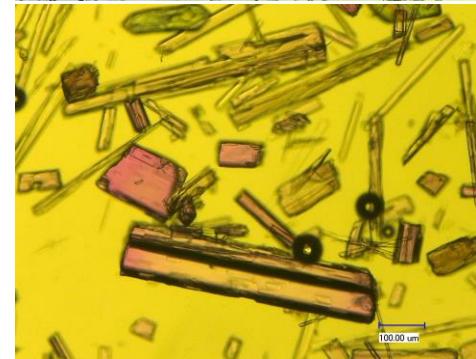


after 24h

HTO



LTO



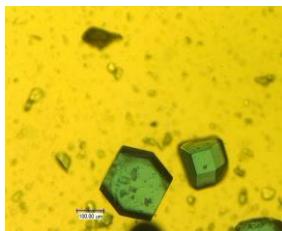
→ buffer solution inside the crystals

+ phenolphthalein after 24h

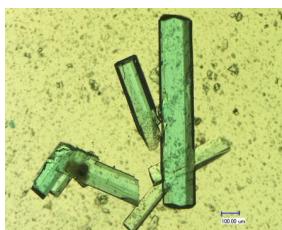
Müller, C., How to describe protein crystals correctly? –case study of lysozyme crystals-, Dissertation, Martin-Luther-Universität Halle-Wittenberg, 2012, <http://141.48.65.178/hs/content/titleinfo/1177647>.

## 2) buffer solution (free water) dyeing / coloring

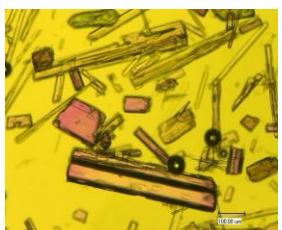
Tetragonal



HTO



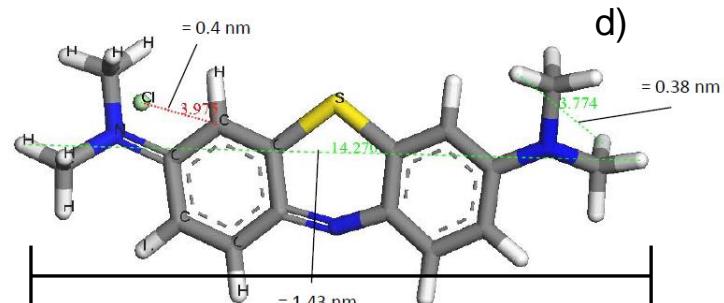
LTO



why?  
→ size and shape of the dye molecule  
and crystal pores

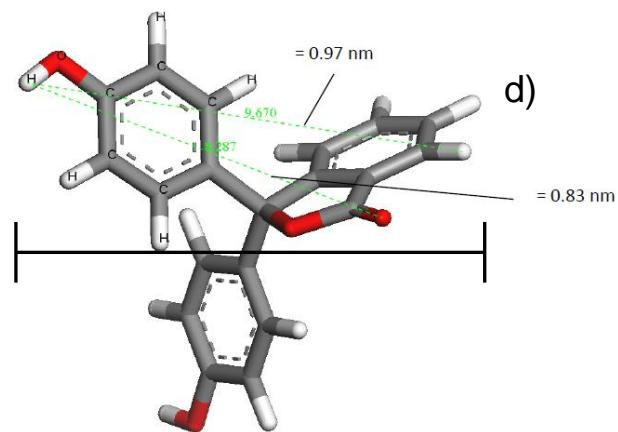
methylene blue

1.43 nm



phenolphthalein

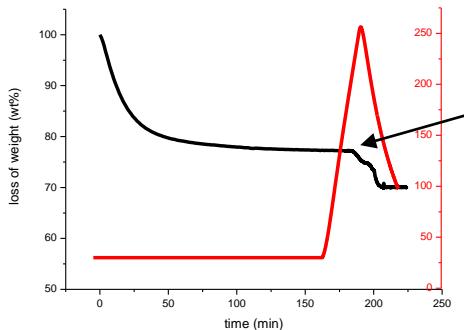
0.97 nm



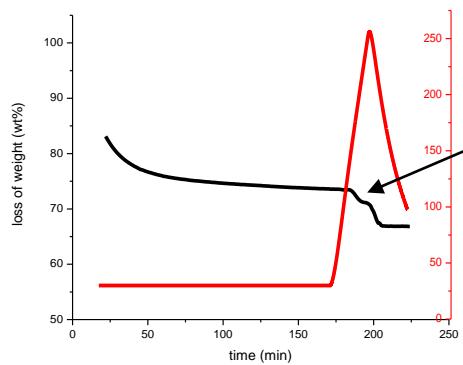
<sup>d</sup>) Accelyrs Software Inc., Material Studio 4.0, San Diego USA 2005

### 3) free (buffer)+ bound water TGA<sup>e)</sup>

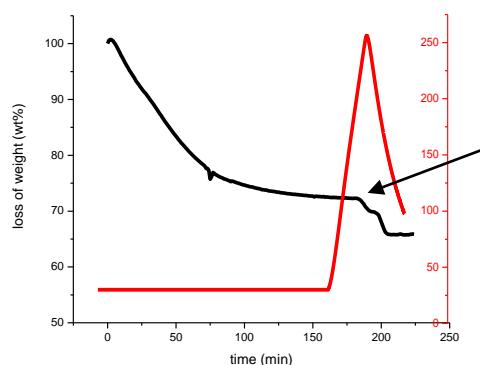
Tetragonal



HTO



LTO



1. step: free water molecules (buffer in the void spaces)

2. step: bonded water molecules (crystal lattice)

decomposition

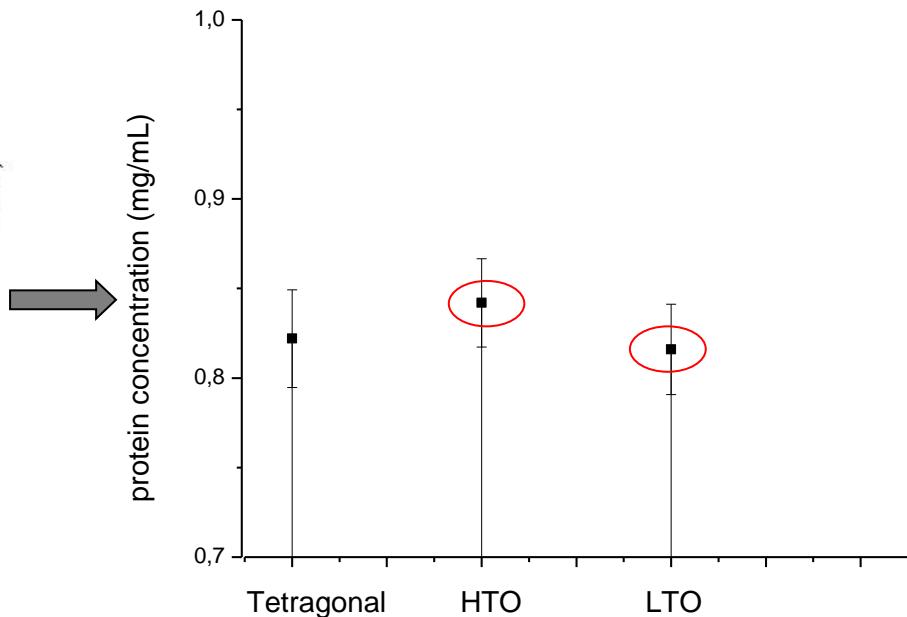
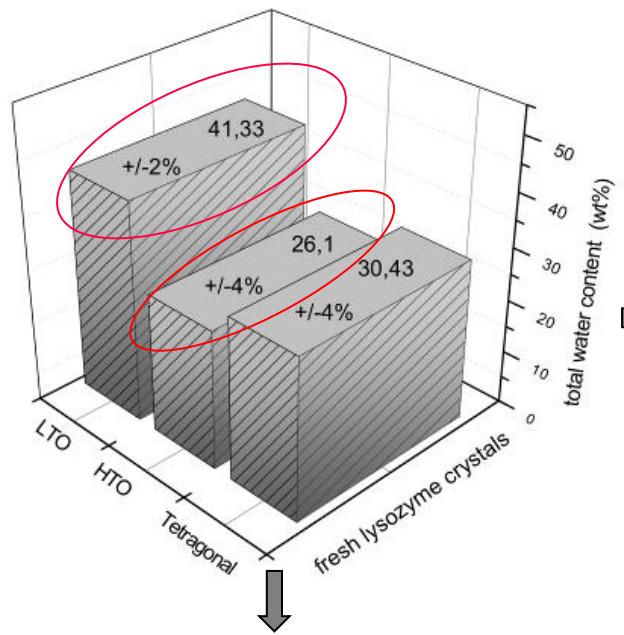
→ two “types“ of water (free and bound)

<sup>e)</sup> TGA \_ Thermogravimetric analysis

<sup>8)</sup> Petrova et al.: *Crystallography Reports*, 52, 2 (2007), 275-279

### 3) free (buffer) + bound water TGA<sup>e)</sup> results

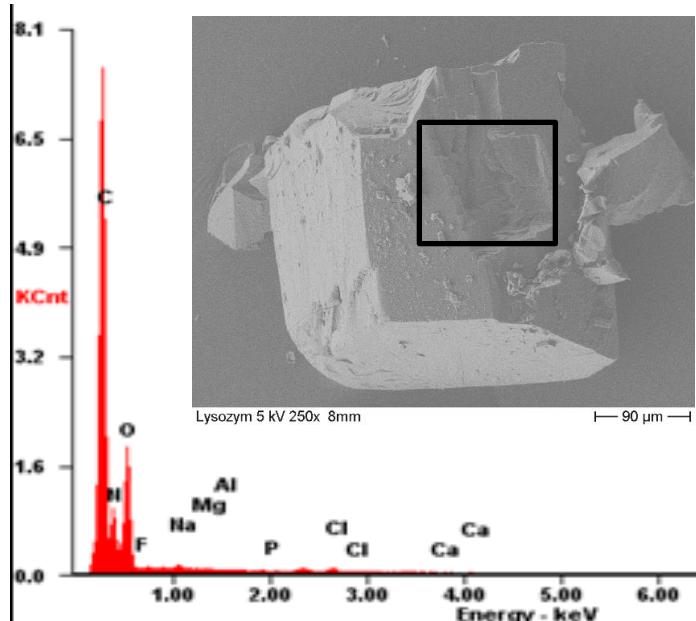
1. + 2. step: loss of water  
→ total water content of fresh  
lysozyme crystals by TGA



→ total water content varies  
→ LTO > Tetragonal > HTO

# 4) NaCl (crystallizing agent) EDX<sup>f)</sup>

➤ Tetragonal:



surface sample

Element	wt%	at wt%
C	63.90	70.16
N	15.50	14.59
O	16.40	13.51
F	00.07	00.05
<b>Na</b>	<b>00.39</b>	<b>00.22</b>
Mg	00.00	00.00
Al	00.11	00.05
P	00.00	00.00
S	01.53	00.63
<b>Cl</b>	<b>02.00</b>	<b>00.74</b>
Ca	00.11	00.04

interior sample

Element	wt%	at wt%
C	63.53	70.54
N	14.88	14.17
O	15.12	12.60
F	00.09	00.06
<b>Na</b>	<b>00.58</b>	<b>00.34</b>
Mg	00.03	00.02
Al	00.03	00.01
P	00.02	00.01
S	02.38	00.99
<b>Cl</b>	<b>03.28</b>	<b>01.23</b>
Ca	00.06	00.02

- Tetragonal lysozyme crystals contain NaCl
- no homogeneity
- same is assumed for HTO and LTO

<sup>f)</sup>EDX \_ Energy dispersive X-ray Spectroscopy by REM Jeol SM 7401 F with the EDX System genesis of EDAX

## 4) crystallizing agent

---

In the paper:

„*Growth Inhibition of Protein Crystals: A study of Lysozyme Polymorphs*“  
of Heijna, M.C.R., van Enckevort, W.J.P., Vlieg., E. [Hej08],

the following sentence is to be found:

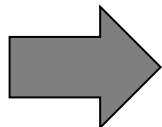
,**Note:**

***The various possible crystal structures of lysozyme are not polymorphs  
in the strictest sense of the word, because  
the salts are incorporated in the crystal and thus induce different  
compositions.***

# analysis of lysozyme crystals - conclusion

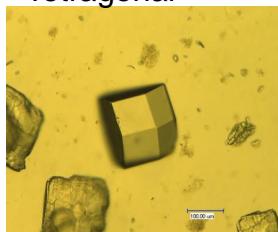
4 main components

lysozyme crystals

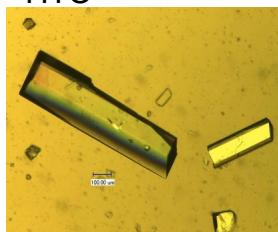


**4 components**

Tetragonal



HTO



LTO



no polymorphism

→ ≠ crystallization conditions – Tetragonal,  
HTO and LTO morphologies show  
**variations in the component fractions**

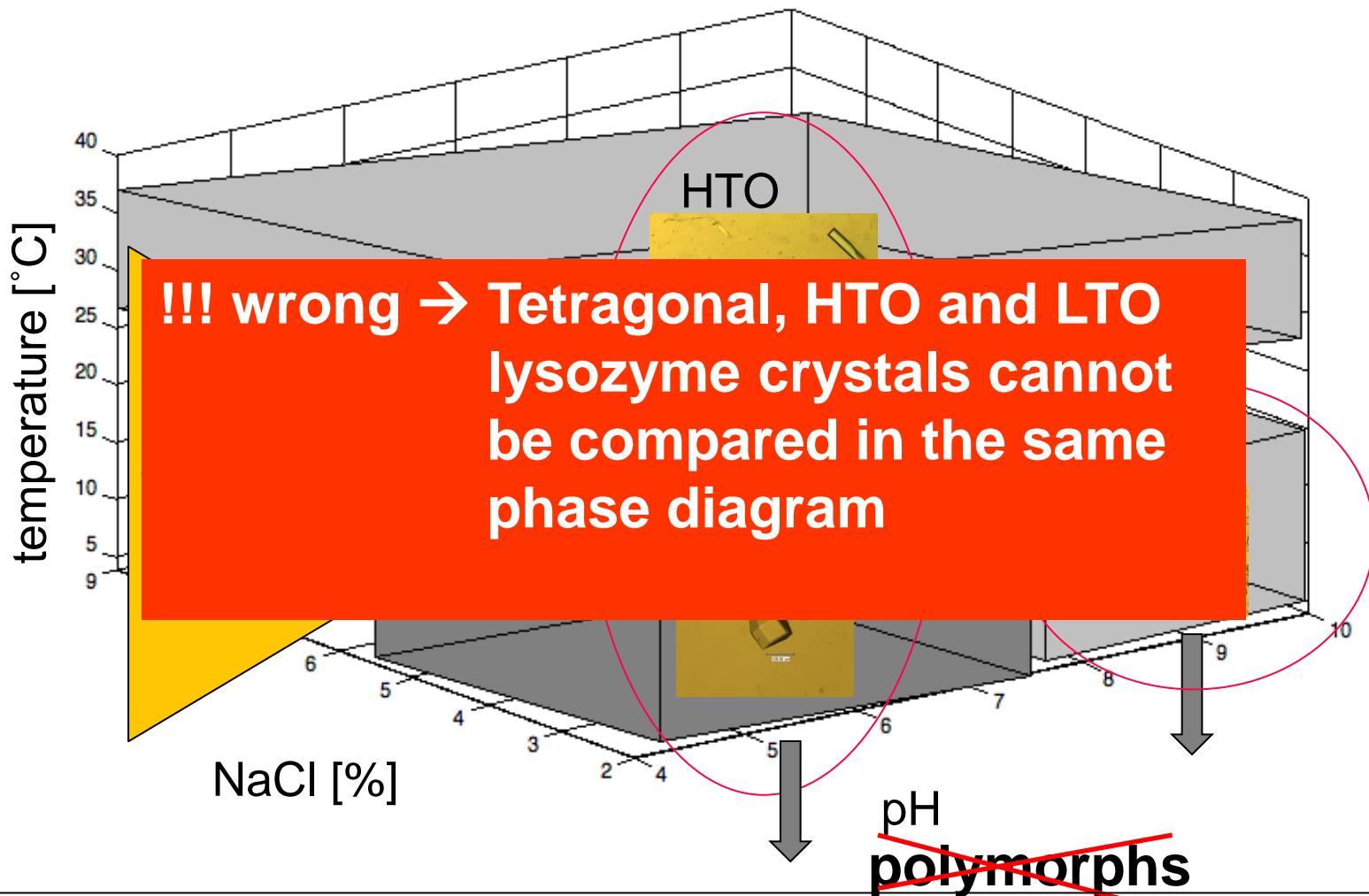
phase diagram

Tetragonal - HTO → “pseudo“- solvates

→ chemically a different solvate

# solubility of lysozyme crystals

## phase diagram<sup>5)</sup>



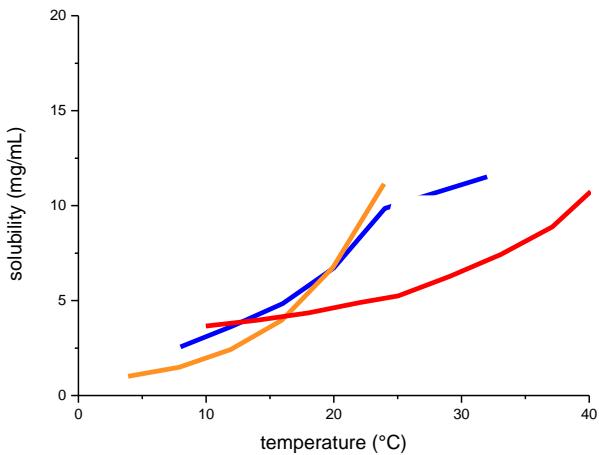
<sup>5)</sup>N. AlDabaihbeh: PhD Thesis, Department of Chemical & Biological Engineering, Illinois Institute of Technology, 2010  
Müller, C., How to describe protein crystals correctly? –case study of lysozyme crystals-, Dissertation, Martin-Luther-Universität Halle-Wittenberg, 2012., <http://141.48.65.178/hs/content/titleinfo/1177647>

# solubility of lysozyme crystals

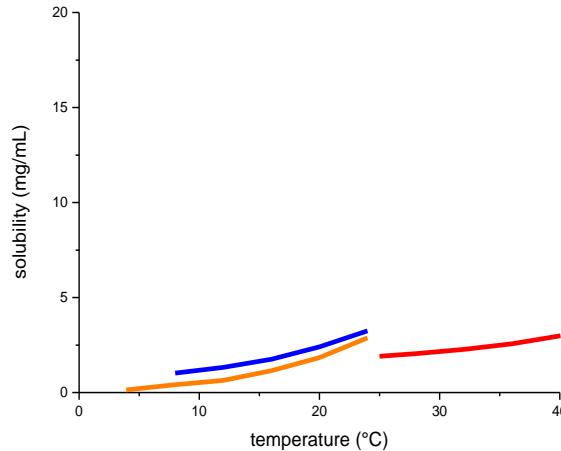
→ new LTO solubility data

- Tetragonal
- - HTO
- · LTO

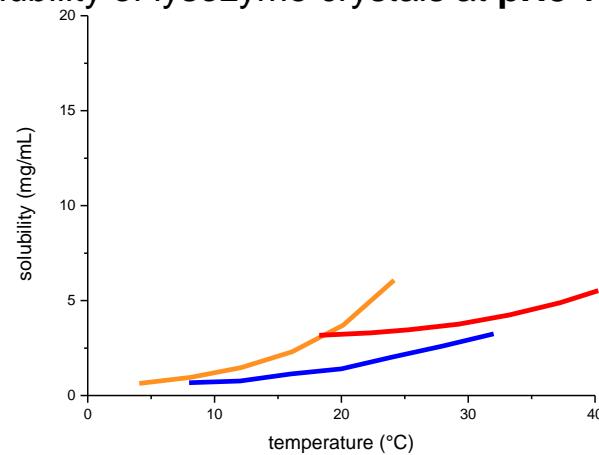
solubility of lysozyme crystals at pH5.7 + 3 wt%



solubility of lysozyme crystals at pH5.7 + 7 wt%



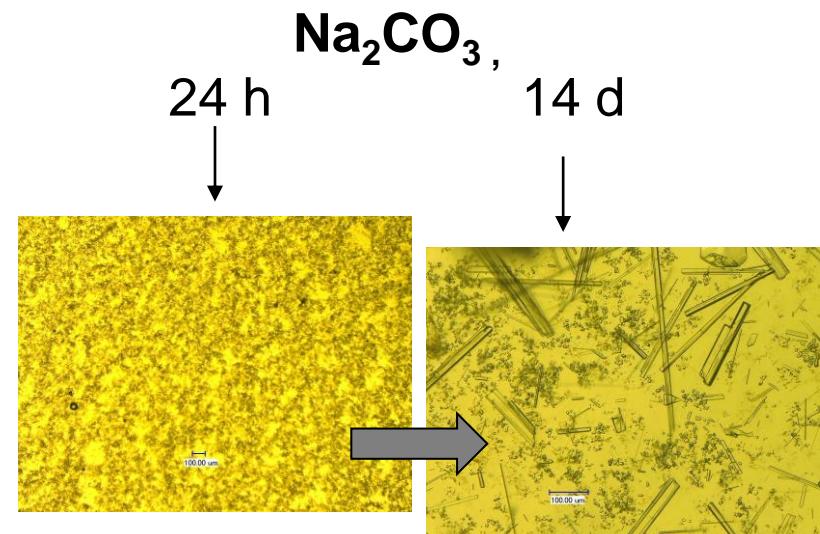
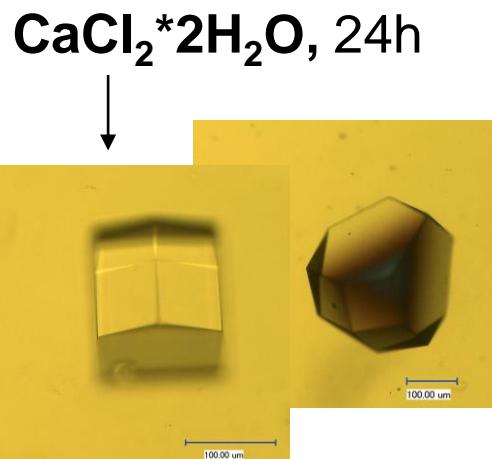
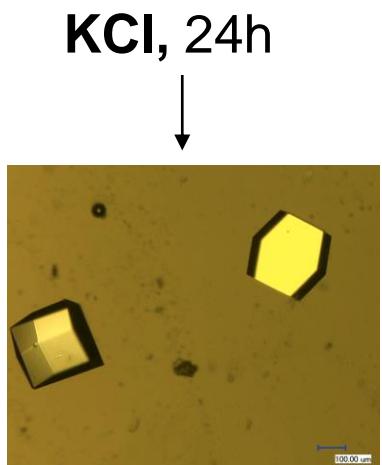
solubility of lysozyme crystals at pH8 + 3 wt%



# production conditions of different lysozyme crystal morphologies

## Tetragonal

acetate buffer pH5,  
50 mg/mL,  
4 wt% salt, 4°C



Orthorhombic

Tetragonal

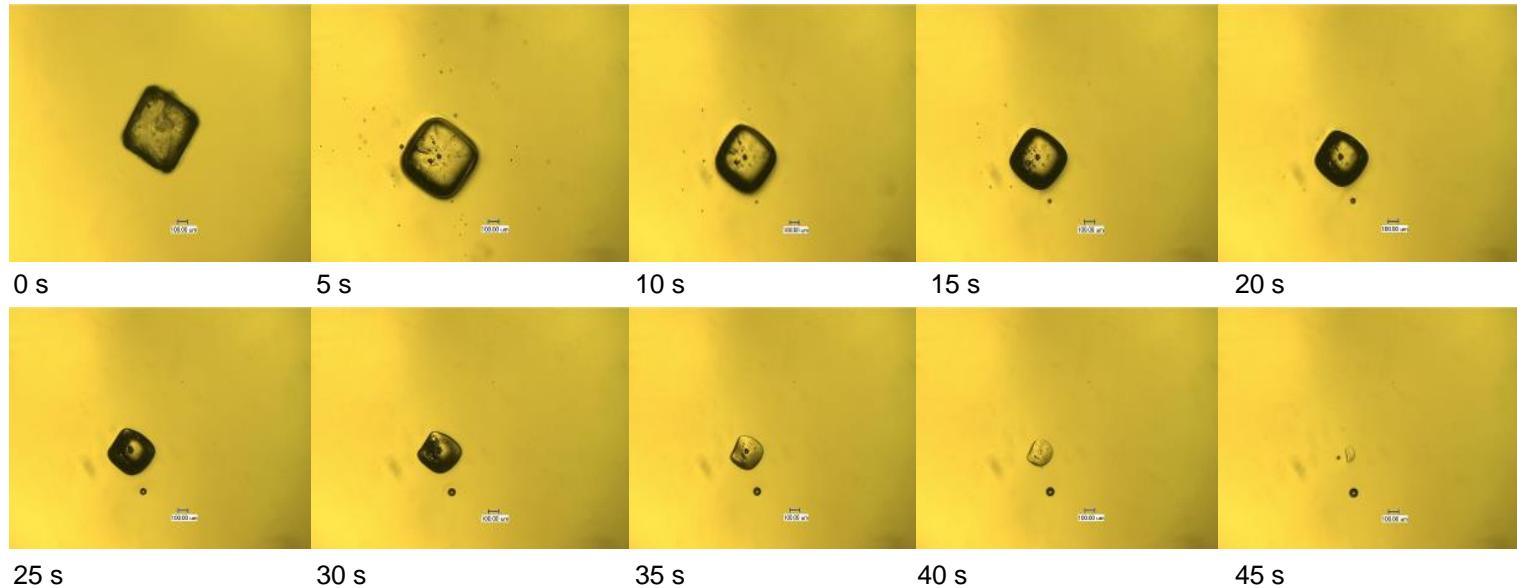
Tetragonal

→ type of salt has high impact on crystal outcome

# dissolution of lysozyme crystals

## dissolution behavior of NaCl

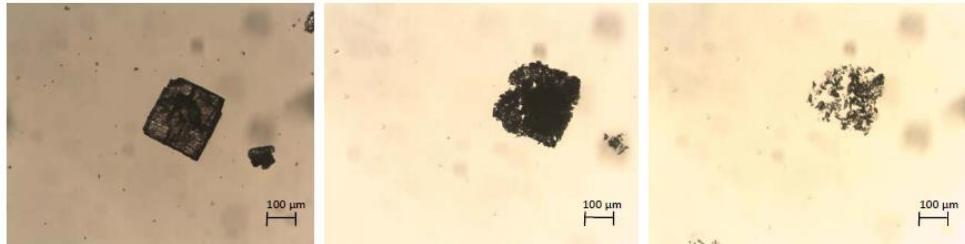
- known dissolution behavior of NaCl crystals in distilled water at room temperature



# dissolution of lysozyme crystals

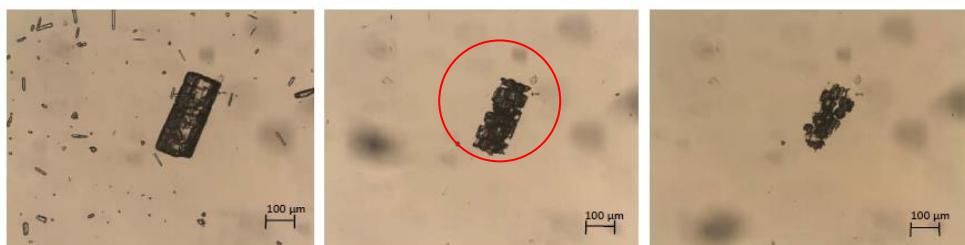
## dissolution behavior

Tetragonal



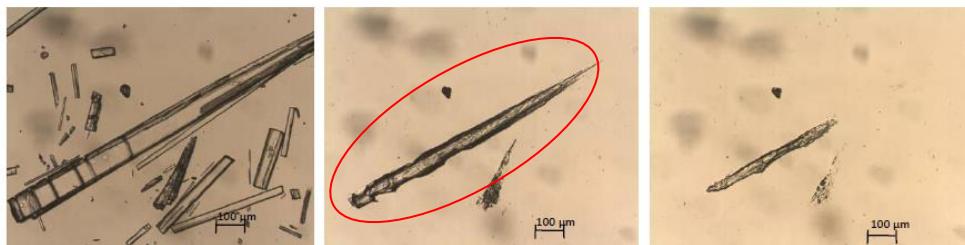
10 s                  10 h                  40 h

HTO



10 s                  2 h                  8 h

LTO



10s                  10h                  18h

→ fresh lysozyme crystals  
in sodium phosphate  
buffer pH8 + 2 wt%  
NaCl at 16 °C

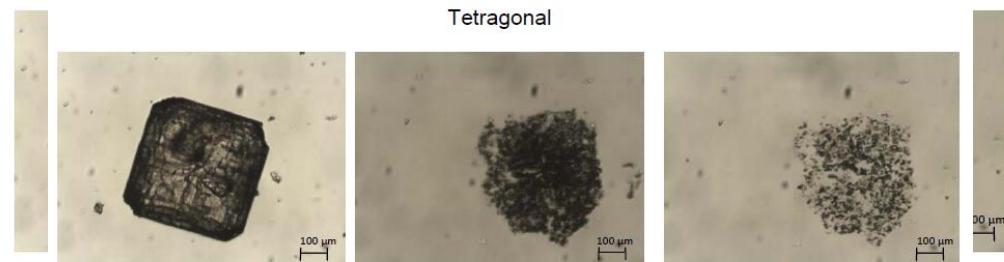
→ HTO falls apart in  
irregular particles

→ LTO changes its  
dissolution behavior  
again – no fragments

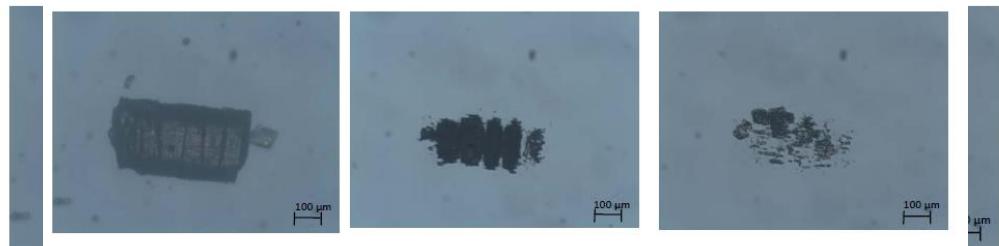
# dissolution of lysozyme crystals

## dissolution phenomenon

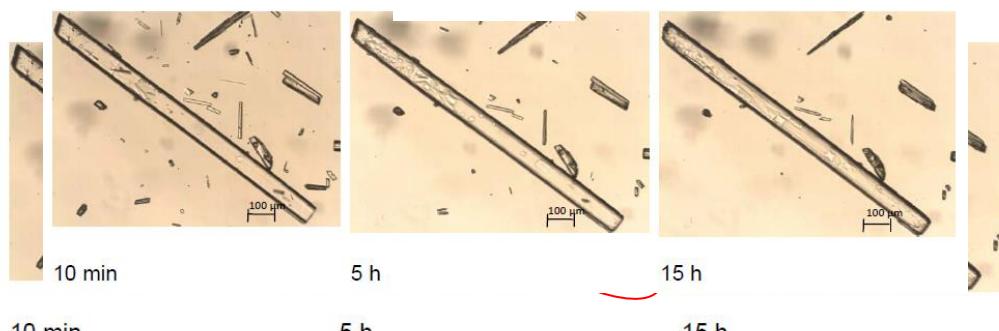
Tetragonal



10 10 min 48 h 84 h HTO



10 10 min 35 h 92 h LTO

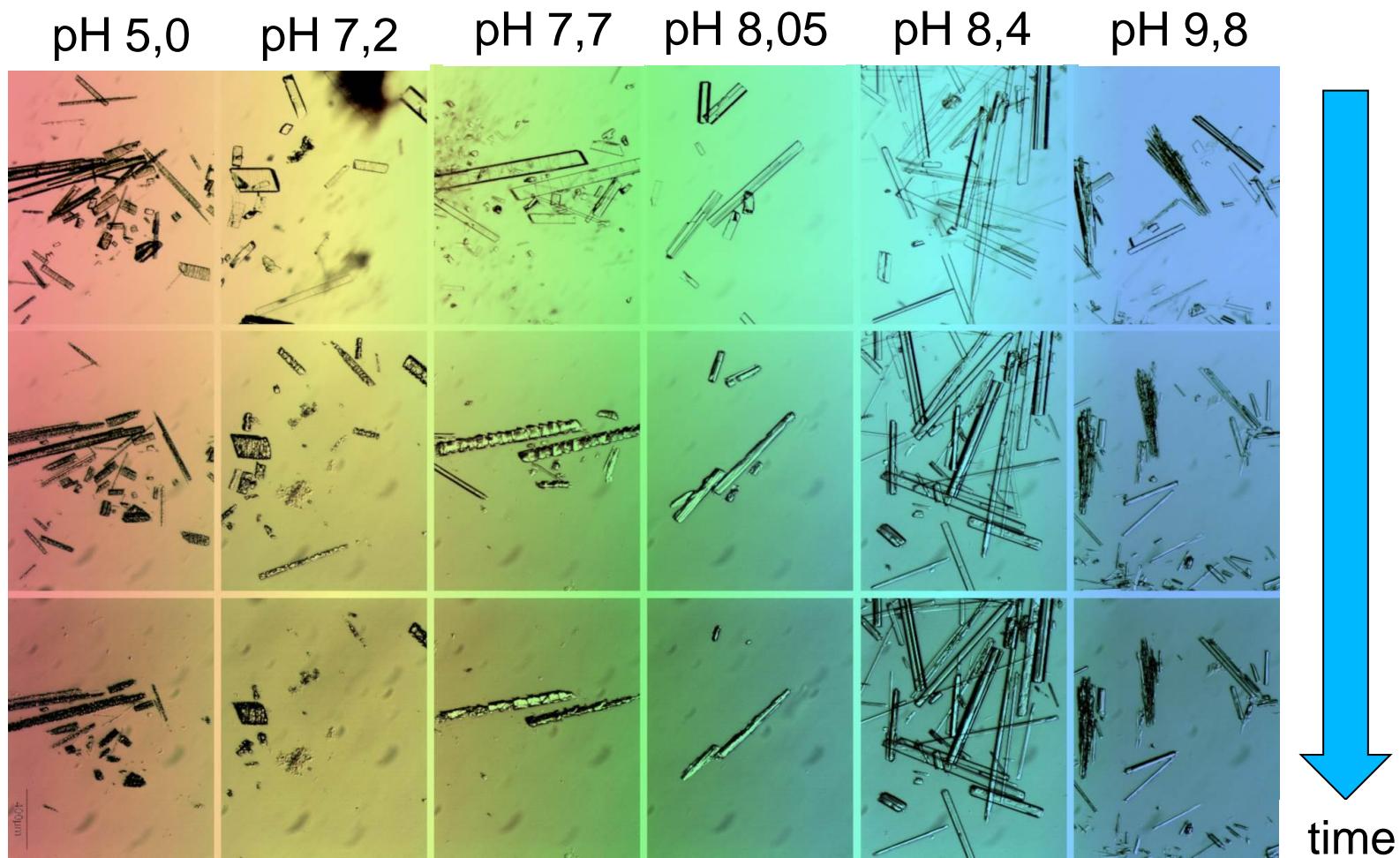


10 min 5 h 15 h

→ fresh lysozyme in glycine buffer pH10 + 7 wt%  
→ ~~Lysozyme~~ glass fall apart during dissolution

→ ~~HTO~~ going and dissolution  
dissolution changes into dissolution shape fragments  
the HTO and LTO lysozyme crystals  
→ LTO seems to not dissolve

## dissolution behaviour versus pH-Value



# Summary

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- It is clear that the established terms form industrial crystallization do not fit the phenomena to be found in protein crystallization!
  - Having a look at the dissolution phenomena shows quite clearly that there are not well considered phenomena existing.
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Thank you for your  
attention!